

# Heron's Formula

**EXERCISE - 12.1**

1. Let each side of the equilateral triangle be  $a$ .

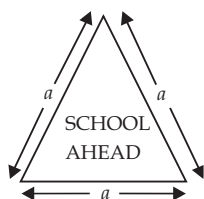
Semi-perimeter of the triangle,  $s = \frac{a+a+a}{2} = \frac{3a}{2}$

Area of the triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{s(s-a)(s-a)(s-a)} = \sqrt{s(s-a)^3}$$

$$= \sqrt{\frac{3a}{2} \left( \frac{3a}{2} - a \right)^3} = \sqrt{\frac{3a}{2} \times \left( \frac{a}{2} \right)^3}$$

$$= \sqrt{\frac{3a^4}{16}} = \frac{\sqrt{3}}{4} a^2 \text{ sq. units.}$$



Now, its perimeter is 180 cm.

$$\therefore a + a + a = 180 \text{ cm}$$

$$\Rightarrow 3a = 180 \Rightarrow a = \frac{180}{3} = 60 \text{ cm}$$

$$\text{Thus, area of the triangle} = \frac{\sqrt{3}}{4} a^2 = \frac{\sqrt{3}}{4} (60)^2 = 900\sqrt{3} \text{ cm}^2$$

2. The sides of the triangular wall are

Let  $a = 122 \text{ m}$ ,  $b = 120 \text{ m}$ ,  $c = 22 \text{ m}$

Semi-perimeter,

$$s = \frac{a+b+c}{2} = \frac{122+120+22}{2} = \frac{264}{2} = 132 \text{ m}$$

The area of triangular side wall

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{132(132-122)(132-120)(132-22)}$$

$$= \sqrt{132 \times 10 \times 12 \times 110}$$

$$= \sqrt{12 \times 11 \times 10 \times 12 \times 11 \times 10} = 1320 \text{ m}^2$$

Rent for 1 year (i.e., 12 months) per  $\text{m}^2 = ₹ 5000$

$$\therefore \text{Rent for 3 months per } \text{m}^2 = ₹ 5000 \times \frac{3}{12}$$

$$\Rightarrow \text{Rent for 3 months for } 1320 \text{ m}^2$$

$$= 5000 \times \frac{3}{12} \times 1320 = 5000 \times 3 \times 110 = ₹ 16,50,000.$$

3. Sides of the wall are 15 m, 11 m and 6 m.

Let  $a = 15 \text{ m}$ ,  $b = 11 \text{ m}$ ,  $c = 6 \text{ m}$

$$\text{Semi-perimeter, } s = \frac{a+b+c}{2} = \frac{15+11+6}{2} = \frac{32}{2} = 16 \text{ m}$$

Area of the triangular wall =  $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{16(16-15)(16-11)(16-6)}$$

$$= \sqrt{16 \times 1 \times 5 \times 10} = \sqrt{2 \times 400} = 20\sqrt{2} \text{ m}^2$$

Thus, the required area painted in colour is  $20\sqrt{2} \text{ m}^2$ .

4. Let the sides of the triangle be  $a = 18 \text{ cm}$ ,  $b = 10 \text{ cm}$  and  $c$ .

Perimeter =  $a + b + c = 42 \text{ cm}$

$$\Rightarrow c = 42 - (18 + 10) = 14 \text{ cm}$$

Now, semi-perimeter,  $s = \frac{42}{2} = 21 \text{ cm}$

Area of a triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{21(21-18)(21-10)(21-14)}$$

$$= \sqrt{21 \times 3 \times 11 \times 7}$$

$$= \sqrt{3 \times 7 \times 3 \times 11 \times 7} = 21\sqrt{11} \text{ cm}^2$$

Thus, the required area of the triangle is  $21\sqrt{11} \text{ cm}^2$ .

5. Perimeter of the triangle = 540 cm

$$\therefore \text{Semi-perimeter, } s = \frac{540}{2} = 270 \text{ cm}$$

The sides of the triangle are in the ratio of 12 : 17 : 25.

Let  $a = 12x \text{ cm}$ ,  $b = 17x \text{ cm}$ ,  $c = 25x \text{ cm}$

$$\therefore 12x + 17x + 25x = 540$$

$$\Rightarrow 54x = 540 \Rightarrow x = 10$$

$$\therefore a = 12 \times 10 = 120 \text{ cm}, b = 17 \times 10 = 170 \text{ cm} \text{ and}$$

$$c = 25 \times 10 = 250 \text{ cm}$$

Area of the triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{270(270-120)(270-170)(270-250)}$$

$$= \sqrt{270 \times 150 \times 100 \times 20}$$

$$= \sqrt{3 \times 3 \times 3 \times 10 \times 3 \times 5 \times 10 \times 10 \times 2 \times 2 \times 5}$$

$$= \sqrt{10^2 \times 10^2 \times 3^2 \times 3^2 \times 5^2 \times 2^2}$$

$$= 10 \times 10 \times 3 \times 3 \times 5 \times 2 = 9000 \text{ cm}^2$$

6. Equal sides of the triangle are 12 cm each.

Let the third side be  $x \text{ cm}$ .

Now, perimeter = 30 cm

$$\Rightarrow 12 + 12 + x = 30$$

$$\Rightarrow x = 6$$

$$\therefore \text{Semi-perimeter, } s = \frac{30}{2} = 15 \text{ cm}$$

Area of the triangle =  $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{15(15-12)(15-12)(15-6)}$$

$$= \sqrt{15 \times 3 \times 3 \times 9} = \sqrt{5 \times 3 \times 3 \times 3 \times 3 \times 3}$$

$$= 3 \times 3 \times \sqrt{5 \times 3} = 9\sqrt{15} \text{ cm}^2$$

Thus, the required area of the triangle is  $9\sqrt{15} \text{ cm}^2$ .

