

# Linear Equations in Two Variables

## EXERCISE - 4.1

1. Let the cost of a note book = ₹  $x$   
and the cost of a pen = ₹  $y$

According to the condition, we have

$$[\text{Cost of a notebook}] = 2 \times [\text{Cost of a pen}]$$

$$\text{i.e. } (x) = 2 \times (y) \Rightarrow x = 2y \Rightarrow x - 2y = 0$$

Thus, the required linear equation is  $x - 2y = 0$ .

2. (i) We have,  $2x + 3y = (9.35)$

$$\Rightarrow 2x + 3y + (-9.35) = 0$$

Comparing it with  $ax + by + c = 0$ , we get  $a = 2$ ,  $b = 3$   
and  $c = -9.35$ .

(ii) We have,  $x - \frac{y}{5} - 10 = 0$

$$\Rightarrow x + \left(-\frac{1}{5}\right)y + (-10) = 0$$

Comparing it with  $ax + by + c = 0$ , we get

$$a = 1, b = -\frac{1}{5} \text{ and } c = -10$$

(iii) We have,  $-2x + 3y = 6$

$$\Rightarrow (-2)x + 3y + (-6) = 0$$

Comparing it with  $ax + by + c = 0$ , we get  $a = -2$ ,  $b = 3$   
and  $c = -6$ .

(iv) We have,  $x = 3y \Rightarrow x + (-3)y + 0 = 0$

Comparing it with  $ax + by + c = 0$ , we get  $a = 1$ ,  
 $b = -3$  and  $c = 0$ .

(v) We have,  $2x = -5y \Rightarrow 2x + 5y + 0 = 0$

Comparing it with  $ax + by + c = 0$ , we get  $a = 2$ ,  
 $b = 5$  and  $c = 0$ .

(vi) We have,  $3x + 2 = 0 \Rightarrow 3x + 0y + 2 = 0$

Comparing it with  $ax + by + c = 0$ , we get  $a = 3$ ,  
 $b = 0$  and  $c = 2$ .

(vii) We have,  $y - 2 = 0 \Rightarrow 0x + 1y + (-2) = 0$

Comparing it with  $ax + by + c = 0$ , we get  $a = 0$ ,  
 $b = 1$  and  $c = -2$ .

(viii) We have,  $5 = 2x \Rightarrow 5 - 2x = 0$

$$\Rightarrow -2x + 0y + 5 = 0 \Rightarrow (-2)x + 0y + 5 = 0$$

Comparing it with  $ax + by + c = 0$ , we get  $a = -2$ ,  
 $b = 0$  and  $c = 5$ .

## EXERCISE - 4.2

1. Option (iii) is true. For every value of  $x$ , we get a corresponding value of  $y$  and vice-versa. Therefore, the linear equation has infinitely many solutions.

2. (i)  $2x + y = 7$

$$\text{When } x = 0, 2(0) + y = 7 \Rightarrow 0 + y = 7 \Rightarrow y = 7$$

$\therefore$  Solution is  $(0, 7)$ .

$$\text{When } x = 1, 2(1) + y = 7 \Rightarrow y = 7 - 2 \Rightarrow y = 5$$

$\therefore$  Solution is  $(1, 5)$ .

$$\text{When } x = 2, 2(2) + y = 7 \Rightarrow y = 7 - 4 \Rightarrow y = 3$$

$\therefore$  Solution is  $(2, 3)$ .

$$\text{When } x = 3, 2(3) + y = 7 \Rightarrow y = 7 - 6 \Rightarrow y = 1$$

$\therefore$  Solution is  $(3, 1)$ .

Thus, the four solutions are  $(0, 7)$ ,  $(1, 5)$ ,  $(2, 3)$  and  $(3, 1)$ .

(ii)  $\pi x + y = 9$

$$\text{When } x = 0, \pi(0) + y = 9 \Rightarrow y = 9$$

$\therefore$  Solution is  $(0, 9)$ .

$$\text{When } x = 1, \pi(1) + y = 9 \Rightarrow y = 9 - \pi$$

$\therefore$  Solution is  $(1, (9 - \pi))$ .

$$\text{When } x = 2, \pi(2) + y = 9 \Rightarrow y = 9 - 2\pi$$

$\therefore$  Solution is  $(2, (9 - 2\pi))$ .

$$\text{When } x = -1, \pi(-1) + y = 9 \Rightarrow -\pi + y = 9 \Rightarrow y = 9 + \pi$$

$\therefore$  Solution is  $(-1, (9 + \pi))$ .

Thus, the four solutions are  $(0, 9)$ ,  $(1, (9 - \pi))$ ,  $(2, (9 - 2\pi))$   
and  $(-1, (9 + \pi))$ .

(iii)  $x = 4y$

$$\text{When } x = 0, 4y = 0 \Rightarrow y = 0$$

$\therefore$  Solution is  $(0, 0)$ .

$$\text{When } x = 1, 4y = 1 \Rightarrow y = \frac{1}{4}$$

$\therefore$  Solution is  $\left(1, \frac{1}{4}\right)$ .

$$\text{When } x = 4, 4 = 4y \Rightarrow y = \frac{4}{4} = 1 \Rightarrow y = 1$$

$\therefore$  Solution is  $(4, 1)$ .

$$\text{When } x = -4, 4y = -4$$

$$\Rightarrow y = \frac{-4}{4} = -1 \Rightarrow y = -1$$

$\therefore$  Solution is  $(-4, -1)$ .

Thus, the four solutions are  $(0, 0)$ ,  $(1, 1/4)$ ,  $(4, 1)$  and  $(-4, -1)$ .

3. (i)  $(0, 2)$  means  $x = 0$  and  $y = 2$

Putting  $x = 0$  and  $y = 2$  in  $x - 2y = 4$ , we get

$$\text{L.H.S.} = 0 - 2(2) = -4. \text{ But R.H.S.} = 4$$

$\Rightarrow$  L.H.S.  $\neq$  R.H.S.

$\therefore x = 0, y = 2$  is not a solution.

(ii)  $(2, 0)$  means  $x = 2$  and  $y = 0$

Putting  $x = 2$  and  $y = 0$  in  $x - 2y = 4$ , we get

$$\text{L.H.S.} = 2 - 2(0) = 2 - 0 = 2. \text{ But R.H.S.} = 4$$

$\Rightarrow$  L.H.S.  $\neq$  R.H.S.

$\therefore (2, 0)$  is not a solution.

(iii)  $(4, 0)$  means  $x = 4$  and  $y = 0$

Putting  $x = 4$  and  $y = 0$  in  $x - 2y = 4$ , we get

$$\text{L.H.S.} = 4 - 2(0) = 4 - 0 = 4 = \text{R.H.S.}$$

$\therefore (4, 0)$  is a solution.

(iv)  $(\sqrt{2}, 4\sqrt{2})$  means  $x = \sqrt{2}$  and  $y = 4\sqrt{2}$

Putting  $x = \sqrt{2}$  and  $y = 4\sqrt{2}$  in  $x - 2y = 4$ , we get

$$\text{L.H.S.} = \sqrt{2} - 2(4\sqrt{2}) = \sqrt{2} - 8\sqrt{2} = \sqrt{2}(1 - 8) = -7\sqrt{2}$$

But R.H.S. = 4

$\Rightarrow$  L.H.S.  $\neq$  R.H.S.  $\therefore (\sqrt{2}, 4\sqrt{2})$  is not a solution.

(v)  $(1, 1)$  means  $x = 1$  and  $y = 1$

Putting  $x = 1$  and  $y = 1$  in  $x - 2y = 4$ , we get

$$\text{L.H.S.} = 1 - 2(1) = 1 - 2 = -1. \text{ But R.H.S.} = 4$$

$\Rightarrow$  L.H.S.  $\neq$  R.H.S.  $\therefore (1, 1)$  is not a solution.

4. We have  $2x + 3y = k$

Putting  $x = 2$  and  $y = 1$  in  $2x + 3y = k$ , we get

$$2(2) + 3(1) = k \Rightarrow 4 + 3 = k \Rightarrow 7 = k$$

Thus, the required value of  $k$  is 7.

