

Post-Mid Term

SOLUTIONS

1. (c) : We know that angle of incidence = angle of reflection.

$$\therefore \angle AQP = \angle BQR = x \text{ (say) and } \angle PQR = 116^\circ \text{ (Given)}$$

$$\text{Now, } x + 116^\circ + x = 180^\circ$$

$$\Rightarrow 2x = 64^\circ \Rightarrow x = 32^\circ$$

$$\therefore \angle AQP = 32^\circ$$

2. (d) : Given, abscissa of the point = $\frac{1}{2} = 0.5$

$$\text{Ordinate of the point} = \frac{-3}{4} = -0.75$$

\therefore The coordinates of the point are (0.5, -0.75)

3. (b) : The sum of opposite angles of a cyclic quadrilateral is 180° .

4. The decimal representation of an irrational number is neither terminating nor repeating.

5. Here, side of an equilateral triangle = '2a' units.

$$\text{Now, area of equilateral triangle with side '2a' = } \frac{\sqrt{3}}{4} (\text{side})^2$$

$$= \frac{\sqrt{3}}{4} (2a)^2 \text{ sq. units} = \sqrt{3} a^2$$

6. Let the fourth angle be x .

Since, sum of angles of a quadrilateral is 360° .

$$\therefore 120^\circ + 60^\circ + 55^\circ + x = 360^\circ$$

$$\Rightarrow x = 360^\circ - (120^\circ + 60^\circ + 55^\circ)$$

$$\Rightarrow x = 360^\circ - 235^\circ = 125^\circ$$

7. As per given bar graph, the highest bar is of Nick channel while smallest bar is of Disney channel.

Number of children who watched Nick channel = 120

Number of children who watched Disney channel = 60

Hence, the required ratio = $60 : 120 = 1 : 2$

8. Given, $x^2 - 3x - 1 = 0$

$$\Rightarrow x^2 - 3x = 1$$

$$\Rightarrow x(x - 3) = 1$$

$$\Rightarrow x - 3 = 1/x$$

$$\Rightarrow x - 1/x = 3 \quad \dots(i)$$

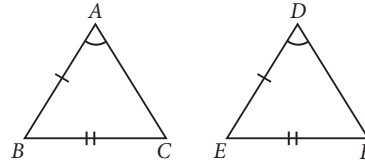
$$\text{Now, } \left(x - \frac{1}{x}\right)^2 = x^2 + \frac{1}{x^2} - 2$$

$$\Rightarrow 3^2 = x^2 + \frac{1}{x^2} - 2$$

$$\Rightarrow 9 + 2 = x^2 + \frac{1}{x^2} \Rightarrow x^2 + \frac{1}{x^2} = 11$$

[Using (i)]

9.



In $\triangle ABC$ and $\triangle DEF$,

$$AB = DE \quad \text{(Given)}$$

$$BC = EF \quad \text{(Given)}$$

and $\angle A = \angle D$, which is not included angle between corresponding equal sides.

Thus, $\triangle ABC$ is not congruent to $\triangle DEF$.

10. Let $\angle R = 3x$ and $\angle S = 2x$

$$\text{Now, } \angle P + \angle Q + \angle R + \angle S = 360^\circ$$

(By angle sum property of a quadrilateral)

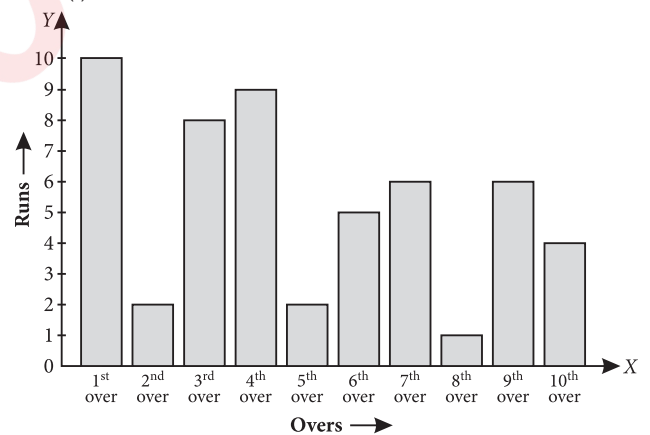
$$\Rightarrow 250^\circ + 3x + 2x = 360^\circ \Rightarrow 5x = 110^\circ \Rightarrow x = 22^\circ$$

$$\therefore \angle R = 3x = 3 \times 22^\circ = 66^\circ$$

$$\angle S = 2x = 2 \times 22^\circ = 44^\circ$$

$$\text{Now, } \angle R - \angle S = 66^\circ - 44^\circ = 22^\circ$$

11. (i)



$$(ii) \text{ Total runs scored} = 10 + 2 + 8 + 9 + 2 + 5 + 6 + 1$$

$$+ 6 + 4 = 53$$

12. Length of the pipe, $h = 30$ cm

$$\text{External radius of the pipe, } R = \frac{35}{2} \text{ cm} = 17.5 \text{ cm}$$

\therefore Thickness of the pipe = 2.5 cm

$$\therefore \text{Internal radius of the pipe, } r = (17.5 - 2.5) \text{ cm} = 15 \text{ cm}$$

Now, curved surface area of the pipe = External curved surface area + Internal curved surface area

$$= 2\pi Rh + 2\pi rh = 2\pi h (R + r)$$

$$= 2 \times \frac{22}{7} \times 30(17.5 + 15) = 2 \times \frac{22}{7} \times 30 \times 32.5$$

$$= \frac{42900}{7} = 6128.57 \text{ cm}^2$$

13. (i) We have, $x = -7 \Rightarrow x + 7 = 0$

$$\Rightarrow 1x + 0 \cdot y + 7 = 0$$

(ii) We have, $y = 3 \Rightarrow y - 3 = 0$

$$\Rightarrow 0 \cdot x + 1y - 3 = 0$$

(iii) We have, $4x = 3 \Rightarrow 4x - 3 = 0 \Rightarrow 4x + 0 \cdot y - 3 = 0$

(iv) We have, $6y = 5 \Rightarrow 6y - 5 = 0 \Rightarrow 0 \cdot x + 6y - 5 = 0$
 $= 325 + 450 + 225 + 150 + 200 + 50 + 125 + 300 + 400 = 2225$

14. Aman, Sahil and Dinesh form an equilateral triangle.

Let the length of each side of the equilateral triangle be $2x$ metres.

Draw $AM \perp SD$.

Since $\triangle ASD$ is equilateral,

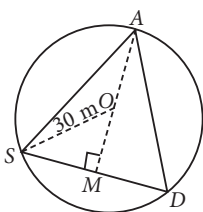
$\therefore AM$ passes through O .

$$\Rightarrow SM = \frac{1}{2}SD = \frac{1}{2}(2x)$$

$$\Rightarrow SM = x$$

Now, in right $\triangle ASM$, we have

$$AM^2 + SM^2 = AS^2$$



$$\Rightarrow AM^2 = AS^2 - SM^2 = (2x)^2 - x^2 = 4x^2 - x^2 = 3x^2$$

$$\Rightarrow AM = \sqrt{3}x$$

Now, $OM = AM - OA = (\sqrt{3}x - 30)$ m

Again, in right $\triangle OSM$, we have

$$OS^2 = SM^2 + OM^2$$

$$30^2 = x^2 + (\sqrt{3}x - 30)^2$$

$$\Rightarrow 900 = x^2 + 3x^2 - 60\sqrt{3}x + 900$$

$$\Rightarrow 4x^2 = 60\sqrt{3}x \Rightarrow 4x = 60\sqrt{3} \Rightarrow x = 15\sqrt{3} \text{ m}$$

Now, $SD = 2x = 2 \times 15\sqrt{3} \text{ m} = 30\sqrt{3} \text{ m}$

Thus, the distance between each of them = $30\sqrt{3} \text{ m}$

15. (i) The bar graph represents the number of vehicles passing through a particular crossing of Gurgaon in different time intervals on a particular day.

(ii) The maximum traffic is between 9-10 hrs. The number of vehicles passed in this hour is 450.

(iii) The minimum traffic is between 13-14 hrs. The number of vehicles passed during this hour is 50.

(iv) The total number of vehicles passing through a crossing during a particular day

$$= 325 + 450 + 225 + 150 + 200 + 50 + 125 + 300 + 400$$

$$= 2225$$

