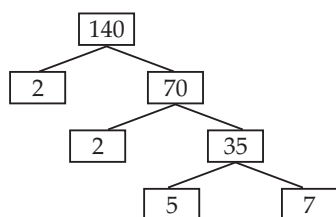


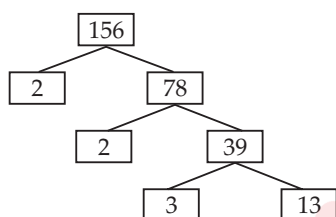
## EXERCISE - 1.1

1. (i) Using factor tree method, we have



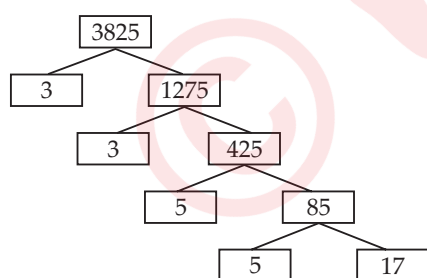
$$\therefore 140 = 2 \times 2 \times 5 \times 7 = 2^2 \times 5 \times 7$$

- (ii) Using factor tree method, we have



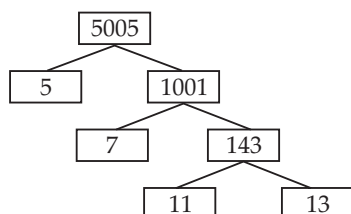
$$\therefore 156 = 2 \times 2 \times 3 \times 13 = 2^2 \times 3 \times 13$$

- (iii) Using factor tree method, we have



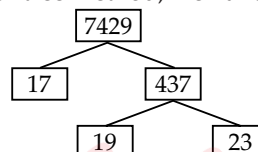
$$\therefore 3825 = 3 \times 3 \times 5 \times 5 \times 17 = 3^2 \times 5^2 \times 17$$

- (iv) Using factor tree method, we have



$$\therefore 5005 = 5 \times 7 \times 11 \times 13$$

- (v) Using factor tree method, we have



$$\therefore 7429 = 17 \times 19 \times 23$$

2. (i) The prime factorisation of 26 and 91 is,  
 $26 = 2 \times 13$  and  $91 = 7 \times 13$

$$\therefore \text{LCM}(26, 91) = 2 \times 7 \times 13 = 182$$

$$\text{HCF}(26, 91) = 13$$

Now,  $\text{LCM} \times \text{HCF} = 182 \times 13 = 2366$  and  $26 \times 91 = 2366$   
*i.e.*,  $\text{LCM} \times \text{HCF} = \text{Product of two numbers.}$

- (ii) The prime factorisation of 510 and 92 is,  
 $510 = 2 \times 3 \times 5 \times 17$  and  $92 = 2 \times 2 \times 23$

$$\therefore \text{LCM}(510, 92) = 2 \times 2 \times 3 \times 5 \times 17 \times 23 = 23460$$

$$\text{HCF}(510, 92) = 2$$

Now,  $\text{LCM} \times \text{HCF} = 23460 \times 2 = 46920$   
 and  $510 \times 92 = 46920$

*i.e.*,  $\text{LCM} \times \text{HCF} = \text{Product of two numbers.}$

- (iii) The prime factorisation of 336 and 54 is,  
 $336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7$  and  $54 = 2 \times 3 \times 3 \times 3$

$$\therefore \text{LCM}(336, 54) = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 7 = 3024$$

$$\text{and } \text{HCF}(336, 54) = 2 \times 3 = 6$$

Now,  $\text{LCM} \times \text{HCF} = 3024 \times 6 = 18144$

$$\text{Also, } 336 \times 54 = 18144$$

Thus,  $\text{LCM} \times \text{HCF} = \text{Product of two numbers.}$

3. (i) The prime factorisation of 12, 15 and 21 is,  
 $12 = 2 \times 2 \times 3$ ,  $15 = 3 \times 5$  and  $21 = 3 \times 7$

$$\therefore \text{HCF}(12, 15, 21) = 3$$

$$\text{LCM}(12, 15, 21) = 2 \times 2 \times 3 \times 5 \times 7 = 420$$

- (ii) We have,  $17 = 1 \times 17$ ,  $23 = 1 \times 23$ ,  $29 = 1 \times 29$

$$\Rightarrow \text{HCF}(17, 23, 29) = 1$$

$$\text{LCM}(17, 23, 29) = 17 \times 23 \times 29 = 11339$$

- (iii) The prime factorisation of 8, 9 and 25 is,  
 $8 = 2 \times 2 \times 2$ ,  $9 = 3 \times 3$  and  $25 = 5 \times 5$

$$\therefore \text{HCF}(8, 9, 25) = 1$$

$$\text{LCM}(8, 9, 25) = 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5 = 1800$$

4. Since,  $\text{LCM} \times \text{HCF} = \text{Product of the numbers}$

$$\therefore \text{LCM} \times 9 = 306 \times 657$$

$$\Rightarrow \text{LCM} = \frac{306 \times 657}{9} = 22338$$

Thus, LCM of 306 and 657 is 22338.

5. Here,  $n$  is a natural number and let  $6^n$  ends with digit 0.

$$\therefore 6^n \text{ is divisible by 5.}$$

But the prime factors of 6 are 2 and 3. i.e.,  $6 = 2 \times 3$

$$\Rightarrow 6^n = (2 \times 3)^n$$

i.e., In the prime factorisation of  $6^n$ , there is no factor 5.

So, by the fundamental theorem of Arithmetic, every composite number can be expressed as a product of primes and this factorisation is unique apart from the order in which the prime factorisation occurs.

$\therefore$  Our assumption that  $6^n$  ends with digit 0, is wrong. Thus, there does not exist any natural number  $n$  for which  $6^n$  ends with zero.

6. We have

$$7 \times 11 \times 13 + 13 = 13((7 \times 11) + 1) = 13(78), \text{ which cannot be a prime number because it has factors 13 and 78.}$$

$$\text{Also, } 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 + 5$$

$$= 5[7 \times 6 \times 4 \times 3 \times 2 \times 1 + 1],$$

which is also not a prime number because it has a factor 5

$$\text{Thus, } 7 \times 11 \times 13 + 13 \text{ and}$$

$$7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 + 5 \text{ are composite numbers.}$$

7. Time taken by Sonia to drive one round of the field  
= 18 minutes

Time taken by Ravi to drive one round of the field  
= 12 minutes

LCM of 18 and 12 gives the exact number of minutes after which they meet again at the starting point.

$$\text{Now, } 18 = 2 \times 3 \times 3 \text{ and } 12 = 2 \times 2 \times 3$$

$$\therefore \text{ LCM of 18 and 12} = 2 \times 2 \times 3 \times 3 = 36$$

Thus, they will meet again at the starting point after 36 minutes.

### EXERCISE - 1.2

1. Let  $\sqrt{5}$  be a rational number.

So, we can find integers  $a$  and  $b$  ( $b \neq 0$  and  $a, b$  are co-prime) such that  $\sqrt{5} = \frac{a}{b}$

$$\Rightarrow \sqrt{5} \cdot b = a \quad \dots(i)$$

Squaring both sides, we get

$$5b^2 = a^2$$

$$\Rightarrow 5 \text{ divides } a^2 \Rightarrow 5 \text{ divides } a \quad \dots(ii)$$

So, we can write  $a = 5m$ , where  $m$  is an integer.

$\therefore$  Putting  $a = 5m$  in (i), we get

$$\sqrt{5}b = 5m$$

$$\Rightarrow 5b^2 = 25m^2 \quad [\text{Squaring both sides}]$$

$$\Rightarrow b^2 = 5m^2$$

$$\Rightarrow 5 \text{ divides } b^2 \Rightarrow 5 \text{ divides } b \quad \dots(iii)$$

From (ii) and (iii), we have,  $a$  and  $b$  have 5 as a common factor which contradicts the fact that  $a$  and  $b$  are co-prime.

$\therefore$  Our supposition that  $\sqrt{5}$  is rational, is wrong.

Hence,  $\sqrt{5}$  is irrational.

2. Let  $3 + 2\sqrt{5}$  be a rational number.

$\therefore$  We can find two co-prime integers  $a$  and  $b$  such that

$$3 + 2\sqrt{5} = \frac{a}{b}, \text{ where } b \neq 0$$

$$\therefore \frac{a}{b} - 3 = 2\sqrt{5} \Rightarrow \frac{a-3b}{b} = 2\sqrt{5} \Rightarrow \frac{a-3b}{2b} = \sqrt{5} \quad \dots(i)$$

$\therefore a$  and  $b$  are integers,

$$\therefore \frac{a-3b}{2b} \text{ is rational}$$

So,  $\sqrt{5}$  is rational.

But this contradicts the fact that  $\sqrt{5}$  is irrational.

$\therefore$  Our supposition is wrong.

Hence,  $3 + 2\sqrt{5}$  is irrational.

$$3. (i) \text{ We have } \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2} = \frac{1}{2} \cdot \sqrt{2}$$

Let  $\frac{1}{\sqrt{2}}$  be rational,

$$\therefore \frac{1}{2}(\sqrt{2}) \text{ is rational}$$

$$\text{Let } \frac{1}{2}(\sqrt{2}) = \frac{a}{b}, \text{ such that } a \text{ and } b \text{ are co-prime integers}$$

and  $b \neq 0$ .

$$\therefore \sqrt{2} = \frac{2a}{b} \quad \dots(i)$$

Since, the division of two integers is rational.

$$\therefore \frac{2a}{b} \text{ is rational.}$$

From (i),  $\sqrt{2}$  is rational number, which contradicts the fact that  $\sqrt{2}$  is irrational.

$\therefore$  Our assumption is wrong.

$$\text{Thus, } \frac{1}{\sqrt{2}} \text{ is irrational.}$$

(ii) Let  $7\sqrt{5}$  is rational.

$\therefore$  We can find two co-prime integers  $a$  and  $b$  such that

$$7\sqrt{5} = \frac{a}{b}, \text{ where } b \neq 0$$

$$\text{Now, } 7\sqrt{5} = \frac{a}{b} \Rightarrow \sqrt{5} = \frac{a}{7b}, \text{ which is a rational number.}$$

[ $\because a$  and  $b$  are integers.]

$$\Rightarrow \sqrt{5} \text{ is a rational number.}$$

This contradicts the fact that  $\sqrt{5}$  is an irrational number.

$\therefore$  Our assumption is wrong.

Thus, we conclude that  $7\sqrt{5}$  is irrational.

(iii) Let  $6 + \sqrt{2}$  is rational.

$\therefore$  We can find two co-prime integers  $a$  and  $b$  such that

$$6 + \sqrt{2} = \frac{a}{b}, \text{ where } b \neq 0$$

$$\therefore \frac{a}{b} - 6 = \sqrt{2} \Rightarrow \sqrt{2} = \frac{a-6b}{b}, \text{ which is rational}$$

$\Rightarrow \sqrt{2}$  is rational which contradicts the fact that  $\sqrt{2}$  is an irrational number.

$\therefore$  Our supposition is wrong.

Hence,  $6 + \sqrt{2}$  is an irrational number.

