# **Quadratic Equations**

CHAPTER **4** 

### **SOLUTIONS**

**1.** (b) : Given  $\alpha$  and  $\beta$  be roots of the equation  $kx^2 + bx + c = 0.$ We have,  $\alpha = \frac{-b + \sqrt{b^2 - 12c}}{\epsilon}$  and  $\beta = \frac{-b - \sqrt{b^2 - 12c}}{\epsilon}$ *.*..  $2k = 6 \implies k = 3$ (b) : We have,  $9x^2 + 3px + 4 = 0$ 2. Here, *a* = 9, *b* = 3*p* and *c* = 4.  $D = b^2 - 4ac = (3p)^2 - 4(9)(4) = 9p^2 - 144$ *:*.. The equation has real and equal roots, so D = 0 $\Rightarrow \quad 9p^2 - 144 = 0 \Rightarrow p^2 = \frac{144}{9} \Rightarrow p^2 = 16$  $\Rightarrow p = \pm 4$ 3. (d): We have,  $m^2 x^2 + 2mcx = (a^2 - c^2) - x^2$  $\Rightarrow (m^2 + 1)x^2 + 2mcx - a^2 + c^2 = 0$ Here,  $A = m^2 + 1$ , B = 2mc and  $C = -a^2 + c^2$ .  $D = B^{2} - 4AC = 4m^{2}c^{2} - 4(m^{2} + 1)(c^{2} - a^{2})$ •  $= 4m^2c^2 - 4m^2c^2 + 4a^2m^2 - 4c^2 + 4a^2 = 4(a^2 - c^2 + a^2m^2)$ Since, the equation has equal roots, so D = 0 $\Rightarrow 4(a^2 - c^2 + a^2 m^2) = 0 \Rightarrow c^2 = a^2 (1 + m^2)$ (b): Let  $x = \sqrt{20 + \sqrt{20 + \sqrt{20 + ...\infty}}} \Rightarrow x = \sqrt{20 + x}$ 4. Squaring on both sides, we get  $x^2 = 20 + x \Longrightarrow x^2 - x - 20 = 0$  $\Rightarrow$   $(x-5)(x+4) = 0 \Rightarrow x = 5 \text{ or } x = -4$ But *x* is a positive quantity.  $\therefore x = 5$ **(b)** : Given,  $a^2x^2 - (a^2b^2 + 1)x + b^2 = 0$ 5.  $\Rightarrow a^{2}x^{2} - a^{2}b^{2}x - x + b^{2} = 0 \Rightarrow a^{2}x(x - b^{2}) - 1(x - b^{2}) = 0$  $\Rightarrow (a^2x - 1) (x - b^2) = 0$  $\Rightarrow a^2x - 1 = 0 \text{ or } x - b^2 = 0 \Rightarrow x = 1/a^2 \text{ or } x = b^2$  $\therefore$  1/*a*<sup>2</sup>, *b*<sup>2</sup> are the required roots. (b) : We have,  $21x^2 - 2x + 1/21 = 0$ 6.  $\Rightarrow \quad 441 x^2 - 42x + 1 = 0$ Here, *a* = 441, *b* = -42 and *c* = 1.  $D = b^2 - 4ac = (-42)^2 - 4(441)(1) = 1764 - 1764 = 0$ *.*.. Hence, both roots are real and repeated. We have,  $x(x + 2c) = -ab \Rightarrow x^2 + 2cx + ab = 0$ 7. ...(i) (i) has real and unequal roots, so  $D = b^2 - 4ac > 0$  $\Rightarrow 4c^2 - 4ab > 0 \Rightarrow c^2 > ab$ 

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Also, we have  $x^2 - 2(a + b)x + 2c^2 + a^2 + b^2 = 0$  ...(ii) Here,  $D = 4(a + b)^2 - 4(2c^2 + a^2 + b^2)$  $= 4(a^2 + b^2 + 2ab - 2c^2 - a^2 - b^2) = 8(ab - c^2) < 0$  [::  $c^2 > ab$ ] So, (ii) has no real roots. 8. For equal roots, discriminant = 0

$$\therefore \quad (k+1)^2 - 4(k+4) \ (1) = 0$$

- $\Rightarrow k^{2} + 2k + 1 4k 16 = 0 \Rightarrow k^{2} 2k 15 = 0$
- $\Rightarrow (k-5)(k+3) = 0 \Rightarrow k = 5 \text{ or } k = -3$

9. Given, x = 1 is root of the given equation, so it will satisfy the given equation.

: 
$$a(1)^2 - 5(a - 1) \times 1 - 1 = 0$$

$$\Rightarrow a - 5a + 5 - 1 = 0 \Rightarrow -4a = -4 \Rightarrow a = \frac{-4}{-4} = 1$$

**10.** We have, 
$$p^2q^2x^2 - q^2x - p^2x + 1 = 0$$

$$\Rightarrow (p^{2}x - 1) (q^{2}x - 1) = 0 \Rightarrow x = \frac{1}{p^{2}} \text{ or } x = \frac{1}{q^{2}}$$

**11.** Let the numbers be x and (x + 4).

According to the question, x(x + 4) = 45

$$\Rightarrow \quad x^2 + 4x - 45 = 0 \Rightarrow x^2 + 9x - 5x - 45 = 0$$

 $\Rightarrow \quad x(x+9) - 5(x+9) = 0$ 

$$\Rightarrow (x+9) (x-5) = 0 \Rightarrow x+9 = 0 \text{ or } x-5 = 0$$

$$\Rightarrow x = -9 \text{ or } x = 5$$

- If *x* = –9, numbers are –9, –9 + 4 *i.e.*, –9, –5
- If *x* = 5, numbers are 5, 5 + 4 *i.e.*, 5, 9
- **12.** Let the number be *x*.

According to question,  $x + 2x^2 = 21$ 

$$\Rightarrow \quad 2x^2 + x - 21 = 0 \Rightarrow 2x^2 - 6x + 7x - 21 = 0$$

$$\Rightarrow 2x(x-3) + 7(x-3) = 0$$

$$\Rightarrow (x-3)(2x+7) = 0 \Rightarrow x = 3 \text{ or } x = \frac{-7}{2}$$

**13.** The given quadratic equation is  $3x^2 + 7x + k = 0$  ...(i) Here, a = 3, b = 7 and c = k.

:. 
$$D = b^2 - 4ac = (7)^2 - 4(3) (k) = 49 - 12k$$

: Equation (i) has real and equal roots, so D = 0.

$$\Rightarrow 49 - 12k = 0 \Rightarrow 12k = 49 \Rightarrow k = \frac{49}{12}$$

**14.** The given quadratic equation is 
$$x(x - 4) + p = 0 \implies x^2 - 4x + p = 0$$

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Here, *a* = 1, *b* = -4 and *c* = *p*. For real and equal roots :  $D = b^2 - 4ac = 0$  $\Rightarrow (-4)^2 - 4(1)(p) = 0$  $\Rightarrow$  16 - 4p = 0  $\Rightarrow$  4p = 16  $\Rightarrow$  p = 4 **15.** Since 2 is a root of the equation  $x^2 + kx + 12 = 0$ . :.  $(2)^{2} + k(2) + 12 = 0 \implies 4 + 2k + 12 = 0 \implies 2k + 16 = 0$  $\Rightarrow k = -16/2 \Rightarrow k = -8$ Putting k = -8 in the equation  $x^2 + kx + q = 0$ , we get  $x^2 - 8x + q = 0$ ...(i) The equation (i) will have equal roots, if discriminant = 0 $\Rightarrow$   $(-8)^2 - 4(1)q = 0$  $\Rightarrow 64 - 4q = 0 \Rightarrow q = 64/4 \Rightarrow q = 16$ **16.** We have,  $x^2 - x + 2 = 0$ Here, *a* = 1, *b* = –1 and *c* = 2 ÷  $D = b^{2} - 4ac = (-1)^{2} - 4 \times 1 \times 2 = 1 - 8 = -7 < 0$ The given quadratic equation does not have real *.*:. roots. 17. (i) (a) : To have no real roots, discriminant  $(D = b^2 - 4ac)$  should be < 0. (a)  $D = 7^2 - 4(-4)(-4) = 49 - 64 = -15 < 0$ (b)  $D = 7^2 - 4(-4)(-2) = 49 - 32 = 17 > 0$ (c)  $D = 5^2 - 4(-2)(-2) = 25 - 16 = 9 > 0$ (d)  $D = 6^2 - 4(3)(2) = 36 - 24 = 12 > 0$ (ii) (b): To have rational roots, discriminant  $(D = b^2 - 4ac)$  should be > 0 and also a perfect square. (a)  $D = 1^2 - 4(1)(-1) = 1 + 4 = 5$ , which is not a perfect square. (b)  $D = (-5)^2 - 4(1)(6) = 25 - 24 = 1$ , which is a perfect square. (c)  $D = (-3)^2 - 4(4)(-2) = 9 + 32 = 41$ , which is not a perfect square. (d)  $D = (-1)^2 - 4(6)(11) = 1 - 264 = -263$ , which is not a perfect square. (iii) (c) : To have irrational roots, discriminant  $(D = b^2 - 4ac)$  should be > 0 but not a perfect square. (a)  $D = 2^2 - 4(3)(2) = 4 - 24 = -20 < 0$ (b)  $D = (-7)^2 - 4(4)(3) = 49 - 48 = 1 > 0$  and also a perfect square. (c)  $D = (-3)^2 - 4(6)(-5) = 9 + 120 = 129 > 0$  and not a perfect square. (d)  $D = 3^2 - 4(2)(-2) = 9 + 16 = 25 > 0$  and also a perfect

square.

(iv) (d): To have equal discriminant roots,  $(D = b^2 - 4ac)$  should be = 0.

(a)  $D = (-3)^2 - 4(1)(4) = 9 - 16 = -7 < 0$ 

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- (b)  $D = (-2)^2 4(2)(1) = 4 8 = -4 < 0$
- (c)  $D = (-10)^2 4(5)(1) = 100 20 = 80 > 0$
- (d)  $D = 6^2 4(9)(1) = 36 36 = 0$

(v) (a) : To have two distinct real roots, discriminant (D  $= b^2 - 4ac$ ) should be > 0.

(a)  $D = 3^2 - 4(1)(1) = 9 - 4 = 5 > 0$ 

(b) 
$$D = 3^2 - 4(-1)(-3) = 9 - 12 = -3 < 0$$

(c)  $D = 8^2 - 4(4)(4) = 64 - 64 = 0$ 

- (d)  $D = 6^2 4(3)(4) = 36 48 = -12 < 0$
- **18.** (i) Roots of the quadratic equation are 2 and –3.
- The required quadratic equation is ...  $(x-2)(x+3) = 0 \Longrightarrow x^2 + x - 6 = 0$

the given equation.

$$\therefore 2\left(-\frac{1}{2}\right)^2 + k\left(-\frac{1}{2}\right) + 1 = 0 \Rightarrow 1 - k + 2 = 0 \Rightarrow k = 3$$
(iii) We have,  $16x^2 - 9 = 0$  ...(i)  

$$\Rightarrow x^2 = \frac{9}{16} \Rightarrow x = \frac{\pm 3}{4}$$

$$\Rightarrow \text{ Roots of (i) are } \frac{3}{4} \text{ and } \frac{-3}{4}.$$
(iv) The given equation is  $(x - 2)^2 + 19 = 0$   

$$\Rightarrow x^2 - 4x + 4 + 19 = 0 \Rightarrow x^2 - 4x + 23 = 0$$
(v) If one root of a quadratic equation is irrational, then  
its other root is also irrational and also its conjugate *i.e.*,  
if one root is  $p + \sqrt{q}$ , then its other root is  $p - \sqrt{q}$ .  
19. (i) We have,  $6x^2 + x - 2 = 0$   

$$\Rightarrow 6x^2 - 3x + 4x - 2 = 0$$

$$\Rightarrow 6x^2 - 3x + 4x - 2 = 0$$

$$\Rightarrow (3x + 2)(2x - 1) = 0$$

$$\Rightarrow x = \frac{1}{2}, \frac{-2}{3}$$
(ii)  $2x^2 + x - 300 = 0$   

$$\Rightarrow 2x^2 - 24x + 25x - 300 = 0$$

$$\Rightarrow (x - 12)(2x + 25) = 0$$

$$\Rightarrow x = 12, \frac{-25}{2}$$
(iii)  $x^2 - 8x + 16 = 0$   

$$\Rightarrow (x - 4)^2 = 0 \Rightarrow (x - 4) (x - 4) = 0 \Rightarrow x = 4, 4$$
(iv)  $6x^2 - 13x + 5 = 0$   

$$\Rightarrow 6x^2 - 3x - 10x + 5 = 0 \Rightarrow (2x - 1)(3x - 5) = 0$$

$$\Rightarrow x = \frac{1}{2}, \frac{5}{3}$$
(v)  $100x^2 - 20x + 1 = 0$   

$$\Rightarrow (10x - 1)^2 = 0 \Rightarrow x = \frac{1}{10}, \frac{1}{10}$$

(ii) We have,  $2x^2 + kx + 1 = 0$ 

Since, -1/2 is the root of the equation, so it will satisfy

20. (i) (d) (ii) (b)

- (iii) (a) : x(x+3) + 7 = 5x 11
- $\Rightarrow x^2 + 3x + 7 = 5x 11$
- $\Rightarrow$   $x^2 2x + 18 = 0$  is a quadratic equation.
- **(b)**  $(x-1)^2 9 = (x-4)(x+3)$
- $\Rightarrow x^2 2x 8 = x^2 x 12$
- $\Rightarrow$  x 4 = 0 is not a quadratic equation.
- (c)  $x^2(2x+1) 4 = 5x^2 10$
- $\Rightarrow 2x^3 + x^2 4 = 5x^2 10$
- $\Rightarrow 2x^3 4x^2 + 6 = 0$  is not a quadratic equation.
- (d) x(x-1)(x+7) = x(6x-9)
- $\Rightarrow x^3 + 6x^2 7x = 6x^2 9x$
- $\Rightarrow x^3 + 2x = 0$  is not a quadratic equation.

#### (iv) (d) (v) (d)

**21.** Let  $\triangle ABC$  is the given triangle.

Let base, BC = x cm, then altitude, AB = (x + 8) cm

By Pythagoras theorem, we have  $(AB)^2 + (BC)^2 = (AC)^2$  $\Rightarrow (x + 8)^2 + x^2 = 40^2$ 

- $\rightarrow$  (x+6) + x = 40
- $\Rightarrow x^2 + 64 + 16x + x^2 = 1600$
- $\Rightarrow 2x^2 + 16x 1536 = 0$
- $\Rightarrow \quad x^2 + 8x 768 = 0$
- $\Rightarrow x^{2} + 32x 24x 768 = 0 \Rightarrow x(x + 32) 24(x + 32) = 0$

40 cm

 $\Rightarrow$   $(x + 32)(x - 24) = 0 \Rightarrow x = -32 \text{ or } x = 24$ 

- But side of a triangle can't be negative.
- $\therefore x = 24$
- **22.** Let the first part be x, then the second part will be 12 x.

According to the given condition,

- $x^{2} + (12 x)^{2} = 74 \Rightarrow x^{2} + 144 + x^{2} 24x 74 = 0$  $\Rightarrow 2x^{2} - 24x + 70 = 0 \Rightarrow x^{2} - 12x + 35 = 0$  $\Rightarrow x^{2} - 7x - 5x + 35 = 0 \Rightarrow x(x - 7) - 5(x - 7) = 0$
- $\Rightarrow (x 7) (x 5) = 0 \Rightarrow x 7 = 0 \text{ or } x 5 = 0$
- $\Rightarrow x = 7 \text{ or } x = 5$
- $\therefore$  Two parts of 12 are 7 and 5.

**23.** Let one number be *x*, then other number will be *x* - 7. According to question,  $x(x - 7) = 408 \Rightarrow x^2 - 7x - 408 = 0$   $\Rightarrow x^2 - 24x + 17x - 408 = 0 \Rightarrow x(x - 24) + 17(x - 24) = 0$   $\Rightarrow (x - 24)(x + 17) = 0 \Rightarrow x = 24 \text{ or } x = -17 \text{ (rejected)}$ Thus, one number is 24 and other number is 17. Sum of numbers = 24 + 17 = 41 **24.** Given,  $4x^2 - 2(c + 1)x + (c + 4) = 0$ Here, A = 4, B = -2(c + 1) and C = c + 4Now,  $D = B^2 - 4AC$ 

Now, 
$$D = B = 4AC$$
  
=  $\{-2(c+1)\}^2 - 4 \times 4 \times (c+4) = 4(c^2 + 2c + 1) - 16(c+4)$   
=  $4c^2 + 8c + 4 - 16c - 64 = 4c^2 - 8c - 60$ 

For equal roots, D = 0 $\therefore 4c^2 - 8c - 60 = 0 \Rightarrow c^2 - 2c - 15 = 0$  $\Rightarrow$   $(c+3)(c-5) = 0 \Rightarrow c = -3 \text{ or } c = 5$ 25. Given,  $\frac{1}{2a+b+2x} = \frac{1}{2a} + \frac{1}{b} + \frac{1}{2x}$  $\frac{1}{2a+b+2x} - \frac{1}{2x} = \frac{1}{2a} + \frac{1}{b}$  $\Rightarrow$  $\frac{2x-2a-b-2x}{b+2a} = \frac{b+2a}{b+2a}$ 2x(2a+b+2x)2ah  $\frac{-(2a+b)}{2x(2a+b+2x)} = \frac{b+2a}{2ab} \implies \frac{-1}{x(2a+b+2x)} = \frac{1}{ab}$  $2x^{2} + 2ax + bx + ab = 0 \implies 2x(x + a) + b(x + a) = 0$  $\Rightarrow$   $(x+a)(2x+b) = 0 \Rightarrow x = -a$  or  $x = \frac{-b}{2}$ 26. Given,  $\frac{6}{x} - \frac{2}{x-1} = \frac{1}{x-2} \Rightarrow \frac{6x-6-2x}{x(x-1)} = \frac{1}{x-2}$  $\frac{4x-6}{x^2-x} = \frac{1}{x-2} \implies 4x^2 - 6x - 8x + 12 = x^2 - x$  $\Rightarrow$  4x<sup>2</sup> - 14x + 12 = x<sup>2</sup> - x  $\Rightarrow 3x^2 - 13x + 12 = 0 \Rightarrow 3x^2 - 9x - 4x + 12 = 0$  $\Rightarrow 3x(x-3) - 4(x-3) = 0 \Rightarrow (x-3)(3x-4) = 0$  $\Rightarrow$  x - 3 = 0 or 3x - 4 = 0

#### OR

Let the number of persons in 1<sup>st</sup> condition is x and in 2<sup>nd</sup> condition is (x + 15). Amount to be divided = ₹ 6500 According to the question,  $\frac{6500}{6500} - \frac{6500}{6500} = 30$ 

According to the question, 
$$\frac{x}{x} - \frac{x+15}{x+15}$$

$$\Rightarrow \quad \frac{6500x + 97500 - 6500x}{x(x+15)} = \frac{30}{1}$$

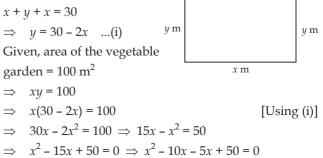
 $\Rightarrow$  x = 3 or x = 4/3

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$$\Rightarrow \quad 30x^2 + 450x = 97500 \Rightarrow 30x^2 + 450x - 97500 = 0$$

- $\Rightarrow \quad x^2 + 15x 3250 = 0 \Rightarrow x^2 + 65x 50x 3250 = 0$
- $\Rightarrow \quad x(x+65) 50(x+65) = 0 \Rightarrow (x+65) (x-50) = 0$
- $\Rightarrow x + 65 = 0 \text{ or } x 50 = 0 \Rightarrow x = -65 \text{ or } x = 50$
- : Number of persons cannot be negative
- $\therefore$  Original number of persons = 50.

**27.** Let the length of one side of garden be *x* m and other side be *y* m. Then, <u>x m</u>



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 $\Rightarrow (x - 10) (x - 5) = 0 \Rightarrow x = 5 \text{ or } 10$ When x = 5, then  $y = 30 - 2 \times 5 = 20$  [Using (i)] When x = 10, then  $y = 30 - 2 \times 10 = 10$  [Using (i)] Hence, the dimensions of the vegetable garden are

5 m and 20 m or 10 m and 10 m.

#### OR

Let *x* be the total number of students of the class.

Number of students opted for visiting an old age home  $=\frac{3}{8}x$ .

Number of students opted for having a nature walk = 16. Number of students opted for tree plantation in the school =  $\sqrt{x}$ .

According to the given condition,

$$\frac{3}{8}x = 16 + \sqrt{x} \implies 3x = 128 + 8\sqrt{x}$$
  

$$\implies 3y^2 = 128 + 8y, \text{ where } \sqrt{x} = y$$
  

$$\implies 3y^2 - 8y - 128 = 0 \implies 3y^2 - 24y + 16y - 128 = 0$$
  

$$\implies 3y(y - 8) + 16(y - 8) = 0 \implies (y - 8) (3y + 16) = 0$$
  

$$\implies y - 8 = 0 \text{ or } 3y + 16 = 0$$
  

$$\implies y = 8 \text{ or } y = -\frac{16}{3} \implies \sqrt{x} = 8 \quad \left[ \because \sqrt{x} \neq -\frac{16}{3} \right]$$
  

$$\implies x = 64$$

Hence, the total number of students of the class is 64.28. Let the numerator of the fraction = *x* 

Then denominator of the fraction = 2x + 1

$$\therefore$$
 Fraction =  $\frac{x}{2x+1}$  and its reciprocal =  $\frac{2x+1}{x}$ 

According to given condition,  $\frac{x}{2x+1} + \frac{2x+1}{x} = 2\frac{16}{21}$  $\Rightarrow \frac{x^2 + 4x^2 + 1 + 4x}{2x^2 + x} = \frac{58}{21} \Rightarrow \frac{5x^2 + 1 + 4x}{2x^2 + x} = \frac{58}{21}$ 

- $\Rightarrow 116x^2 + 58x = 105x^2 + 84x + 21$
- $\Rightarrow 116x^2 + 58x 105x^2 84x 21 = 0$

$$\Rightarrow 11x^2 - 26x - 21 = 0 \Rightarrow 11x^2 - 33x + 7x - 21 = 0$$

- $\Rightarrow \quad 11x(x-3) + 7(x-3) = 0 \Rightarrow (x-3) (11x+7) = 0$
- $\Rightarrow x 3 = 0 \text{ or } 11x + 7 = 0 \Rightarrow x = 3 \text{ or } x = -7/11$
- $\therefore \quad x = 3$  (Neglecting negative value)

:. Fraction =  $\frac{x}{2x+1} = \frac{3}{6+1} = \frac{3}{7}$ 

**29.** Let the original price of the toy =  $\mathbf{E} x$ 

Then the reduced price of the toy =  $\overline{\mathbf{x}}$  (x – 2) According to the question,

 $\frac{360}{x-2} - \frac{360}{x} = 2 \quad \left( \because \text{ Number of toys} = \frac{\text{Total amount}}{\text{Price of 1 toy}} \right)$ 

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$$\Rightarrow \frac{360x - 360x + 720}{x(x-2)} = 2 \Rightarrow \frac{720}{x(x-2)} = \frac{2}{1}$$

$$\Rightarrow x(x-2) = 360$$

$$\Rightarrow x^2 - 2x - 360 = 0 \Rightarrow x^2 - 20x + 18x - 360 = 0$$

$$\Rightarrow x(x-20) + 18(x-20) = 0 \Rightarrow (x-20) (x+18) = 0$$

$$\Rightarrow x = 20 \text{ or } x + 18 = 0$$

$$\Rightarrow x = 20 \text{ or } x + 18 = 0$$

$$\Rightarrow x = 20 \text{ or } x = -18$$

$$\therefore x = 20 \qquad [\because \text{Price cannot be negative}]$$

$$\therefore \text{ Original price of the toy = ₹ 20$$
30. Given,  $(2p+1)x^2 - (7p+2)x + (7p-3) = 0$  ...(i)  

$$\therefore \text{ Roots are equal.} \therefore D = 0$$

$$\Rightarrow (-(7p+2))^2 - 4(2p+1)(7p-3) = 0$$

$$\Rightarrow 49p^2 + 4 + 28p - 4(14p^2 + 7p - 6p - 3) = 0$$

$$\Rightarrow 49p^2 + 28p + 4 - 56p^2 - 4p + 12 = 0$$

$$\Rightarrow 7p^2 - 24p - 16 = 0 \Rightarrow 7p^2 + 4p - 28p - 16 = 0$$

$$\Rightarrow p(7p+4) - 4(7p+4) = 0 \Rightarrow (p-4)(7p+4) = 0$$

$$\Rightarrow p = 4 \text{ or } p = \frac{-4}{7}$$
When  $p = 4$ , (i) becomes  $9x^2 - 30x + 25 = 0$ 

$$\Rightarrow (3x)^2 - 2(3x)(5) + (5)^2 = 0$$

$$\Rightarrow (3x-5)^2 = 0 \Rightarrow x = \frac{5}{3}, \frac{5}{3}$$
When  $p = \frac{-4}{7}$ , (i) becomes  

$$\frac{-x^2}{7} + 2x - 7 = 0 \Rightarrow x^2 - 14x + 49 = 0$$

$$\Rightarrow (x - 7)^2 = 0 \Rightarrow x = 7, 7$$
Thus, equal roots of given equation are either 5/3 or 7.  
31. Let the denominator of the fraction = x  

$$\therefore \text{ Numerator of the fraction = x - 4}$$

$$\Rightarrow \text{ Fraction } = \frac{x-4}{x}$$
According to question,  

$$\frac{x-4}{x+1} = \frac{x-4}{x} - \frac{1}{18} \Rightarrow \frac{x-4}{x} - \frac{x-4}{x+1} = \frac{1}{18}$$

$$\Rightarrow (x-4) \left[\frac{1}{x} - \frac{1}{18} \Rightarrow \frac{x-4}{x} - \frac{x-4}{x+1} = \frac{1}{18}$$

$$\Rightarrow 18(x-4) = x(x+1) \Rightarrow 18x - 72 = x^2 + x$$

$$\Rightarrow x^2 - 17x + 72 = 0 \Rightarrow x^2 - 9x - 8x + 72 = 0$$

$$\Rightarrow x = 8 \text{ or } x = 9$$
Hence, the fraction  $\frac{x-4}{x}$  is  $\frac{5}{9}$ .  
32. Let breadth of rectangular park = (x + 3)m
Now, area of rectangular park = (x + 3)m  
Now, area of rectangular park = (x + 3)m

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Given, base of triangular park = Breadth of the rectangular park

Base of triangular park = x m *.*..

and also it is given that altitude of triangular park = 12 m

$$\therefore \quad \text{Area of triangular park} = \frac{1}{2} \times x \times 12 = 6x \text{ m}^2$$

According to the question,

Area of rectangular park = 4 + Area of triangular park

$$\Rightarrow x^2 + 3x = 4 + 6x \Rightarrow x^2 + 3x - 6x - 4 = 0$$

$$\Rightarrow x^2 - 3x - 4 = 0 \Rightarrow x^2 - 4x + x - 4 = 0$$

- $\Rightarrow$   $x(x-4) + 1(x-4) = 0 \Rightarrow (x-4)(x+1) = 0$
- x 4 = 0 or  $x + 1 = 0 \Rightarrow x = 4$  or x = -1 $\rightarrow$

Since, breadth cannot be negative.

*.*.. x = 4

Hence, breadth of the rectangular park = 4 mand length of the rectangular park = x + 3 = 4 + 3 = 7 m.

#### OR

Let the length of piece of cloth = x m Increased length of piece of cloth = (x + 5)mTotal cost of piece of cloth = ₹ 200 According to the question,

 $\left[ \because \text{ Rate per metre} = \frac{\text{Total cost}}{\text{Length}} \right]$ 200 200 = 2  $\frac{x}{x+5}$ 200x + 1000 - 200x = 2

$$\Rightarrow \frac{200x + 1000 - 20}{x(x+5)}$$

 $1000 = 2x^2 + 10x \Longrightarrow 2x^2 + 10x - 1000 = 0$ 

$$\Rightarrow x^{2} + 5x - 500 = 0 \Rightarrow x^{2} + 25x - 20x - 500 = 0$$

 $x(x + 25) - 20(x + 25) = 0 \Rightarrow (x + 25)(x - 20) = 0$  $\Rightarrow$ 

$$\Rightarrow x + 25 = 0 \text{ or } x - 20 = 0 \Rightarrow x = -25 \text{ or } x = 20$$

But, length can never be negative.

Length of cloth = 20 m*.*.. and rate per metre =  $\underbrace{\underbrace{200}}_{20} = \underbrace{\underbrace{10}}_{20}$ .

33 Let the number of students in the group in the beginning be *x*.

Total internet service charges for *x* students = ₹ 4800

Internet service charges for each student =  $₹ \frac{4800}{r}$ *.*.. It is given that 4 more students join the group.

The number of students in group for internet service ... = (x + 4)

Now, the internet service charges for each student =₹ 4800

According to question, 
$$\frac{4800}{x} - \frac{4800}{x+4} = 200$$

$$\Rightarrow \quad \frac{4800x + 19200 - 4800x}{x(x+4)} = 200$$

$$\Rightarrow 19200 = 200(x^{2} + 4x) \Rightarrow 96 = x^{2} + 4x$$
  

$$\Rightarrow x^{2} + 4x - 96 = 0 \Rightarrow x^{2} + 12x - 8x - 96 = 0$$
  

$$\Rightarrow x(x + 12) - 8(x + 12) = 0 \Rightarrow (x - 8) (x + 12) = 0$$
  

$$\Rightarrow x - 8 = 0 \text{ or } x + 12 = 0 \Rightarrow x = 8 \text{ or } x = -12$$

But number of students cannot be negative

·. x = 8

 $\Rightarrow$ 

Hence, the number of students in the group in the beginning is 8.

#### OR

Let the speed of the train be x km/hour.

When the speed is 9 km/hour more, then the new speed of the train is (x + 9) km/hour.

Time taken by the train with speed x km/hour for ajourney of 180 km =  $\frac{180}{x}$  hours

Time taken by the train with new speed (x + 9) km/hour for a journey of 180 km =  $\frac{180}{(x+9)}$  hours

According to the question,  $\frac{180}{r} - \frac{180}{r+9} = 1$  $\Rightarrow 180\left[\frac{1}{x} - \frac{1}{x+9}\right] = 1 \Rightarrow 180\left[\frac{x+9-x}{x(x+9)}\right] = 1$  $\Rightarrow 180 \times 9 = x(x+9) \Rightarrow x^2 + 9x - 1620 = 0$  $\Rightarrow x^{2} + 45x - 36x - 1620 = 0 \Rightarrow x(x + 45) - 36(x + 45) = 0$  $(x + 45) (x - 36) = 0 \Rightarrow x + 45 = 0 \text{ or } x - 36 = 0$ x = -45 or x = 36 $\Rightarrow$ 

But, speed can't be negative.

x = 36*.*..

Hence, the uniform speed of the train is 36 km/hour.

**34.** Let *x* and *y* be the sides of two squares, respectively such that x > y, where x is the side of the first square and *y* is the side of the second square.

Area of the first square + Area of the second square *.*..  $= 640 \text{ m}^2$ 

$$\Rightarrow x^2 + y^2 = 640 \qquad \dots (i)$$

Again, it is given that the difference of their perimeters = 64 m

$$\Rightarrow 4x - 4y = 64 \Rightarrow x = 16 + y \qquad \dots (ii)$$

From (i) and (ii), we have,  $(16 + y)^2 + y^2 = 640$ 

$$\Rightarrow 256 + y^2 + 32y + y^2 = 640 \Rightarrow 2y^2 + 32y - 384 = 0$$

 $\Rightarrow y^2 + 16y - 192 = 0 \Rightarrow y^2 + 24y - 8y - 192 = 0$ 

 $\Rightarrow y(y+24) - 8(y+24) = 0 \Rightarrow (y+24)(y-8) = 0$ 

 $\Rightarrow$  y + 24 = 0 or  $y - 8 = 0 \Rightarrow y = -24$  or y = 8

But, side of a square can't be negative.  $\therefore y = 8$ 

When y = 8, then from (ii), we get x = 16 + 8 = 24.

Hence, the sides of the two squares are 24 m and 8 m respectively.

#### MtG 100 PERCENT Mathematics Class-10

#### OR

Let the speed of Deccan Queen = x km/hrand speed of other train = (x - 20) km/hr Time taken by Deccan Queen =  $\frac{192}{r}$  hr and time taken by other train =  $\frac{192}{(x-20)}$  hr According to the question,  $\frac{192}{(x-20)} - \frac{192}{x} = \frac{48}{60}$  or  $\frac{4}{5}$  $\frac{192x - 192x + 3840}{x(x - 20)} = \frac{4}{5}$  $\Rightarrow$  $5(3840) = 4x(x - 20) \Longrightarrow 19200 = 4x^2 - 80x$  $\Rightarrow$  $4x^2 - 80x - 19200 = 0 \implies x^2 - 20x - 4800 = 0$  $\Rightarrow$  $x^{2} - 80x + 60x - 4800 = 0 \Longrightarrow x(x - 80) + 60(x - 80) = 0$  $\Rightarrow$  $(x - 80) (x + 60) = 0 \Longrightarrow x - 80 = 0 \text{ or } x + 60 = 0$  $\Rightarrow$ x = 80 or x = -60 $\Rightarrow$ 

- As speed can never be negative.  $\therefore x = 80$
- $\therefore$  Speed of Deccan Queen = 80 km/hr.

- **35.** Let the usual speed of the plane be x km/hr.
- $\therefore$  Time taken to travel 1500 km at *x* km/hr

$$=\frac{1500}{x}$$
 hour

Increased speed of the plane = (x + 250) km/hr

 $\therefore$  Time taken to travel 1500 km at (x + 250) km/hr

$$\frac{1500}{x+250}$$
 hour

According to question,

 $\frac{1500}{x} - \frac{1500}{x+250} = \frac{30}{60} \implies 1500 \left(\frac{x+250-x}{x(x+250)}\right) = \frac{1}{2}$   $\implies 2 \times 1500 \times 250 = x^2 + 250x$   $\implies x^2 + 250x - 750000 = 0$   $\implies x^2 + 1000x - 750x - 750000 = 0$   $\implies x (x + 1000) - 750 (x + 1000) = 0$   $\implies x = 750 \text{ or } x = -1000 \text{ (But speed can't be negative)}$  $\therefore x = 750$ 

Hence, usual speed of the plane is 750 km/hr.

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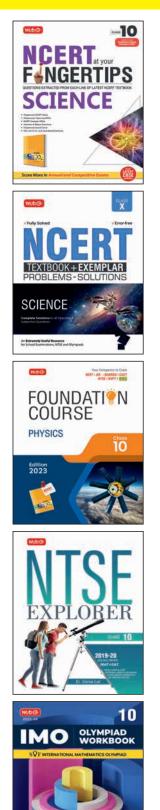
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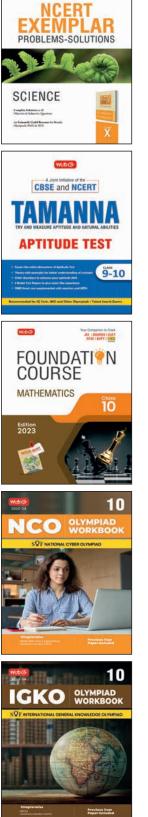
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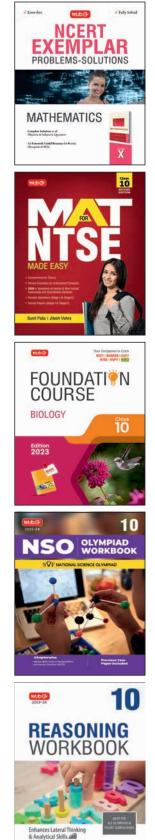
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