

Arithmetic Progressions

SOLUTIONS

1. (c): Since, $\frac{1}{x+2}$, $\frac{1}{x+3}$, $\frac{1}{x+5}$ are in A.P. $\therefore \quad \frac{1}{x+3} - \frac{1}{x+2} = \frac{1}{x+5} - \frac{1}{x+3}$ $\Rightarrow \quad \frac{x+2-x-3}{(x+3)(x+2)} = \frac{x+3-x-5}{(x+5)(x+3)}$ $\Rightarrow \quad \frac{-1}{(x+3)(x+2)} = \frac{-2}{(x+5)(x+3)} \quad \Rightarrow \quad \frac{-1}{x+2} = \frac{-2}{x+5}$ \Rightarrow -x - 5 = -2x - 4 \Rightarrow -x + 2x = -4 + 5 \Rightarrow x = 1(d) : Given A.P. is $5, \frac{19}{4}, \frac{9}{2}, \frac{17}{4}, \dots$ Here, a = 5, $d = \frac{19}{4} - 5 = -\frac{1}{4}$ \therefore 10th term, $a_{10} = a + (10 - 1)d$ $=5+9\left(-\frac{1}{4}\right)=\frac{20-9}{4}=\frac{11}{4}$ (d): Since, alternate terms of an A.P. also forms an A.P. 3. So, (x - y) - (x + y) = (2x + 3y) - (x - y) \Rightarrow $-2y = x + 4y \Rightarrow -2y - 4y = x \Rightarrow x = -6y$ (c) : Given A.P. is 25, 50, 75, 100, 4. Here, a = 25, d = 25 and $a_k = 1000$ Now, $a_k = 1000$ $a + (k - 1)d = 1000 \Rightarrow 25 + (k - 1)25 = 1000$ $25 + 25k - 25 = 1000 \Longrightarrow 25k = 1000 \Longrightarrow k = 40$ \Rightarrow (d) : Let *d* be the same common difference of two 5. A.P.s. Given, first term of 1^{st} A.P., a = 8First term of 2^{nd} A.P., $a_1 = 3$ Now, 30^{th} term of 1^{st} A.P. = a + 29d = 8 + 29dAlso, 30^{th} term of 2^{nd} A.P. = $a_1 + 29d = 3 + 29d$ Required difference = (8 + 29d) - (3 + 29d) = 5÷. Given, A.P. is $\sqrt{27}$, $\sqrt{48}$, $\sqrt{75}$,... 6. *i.e.*, A.P. is $3\sqrt{3}$, $4\sqrt{3}$, $5\sqrt{3}$,... Clearly, first term, $a = 3\sqrt{3}$ Second term, $a + d = 4\sqrt{3}$ Common difference, $d = 4\sqrt{3} - 3\sqrt{3} = \sqrt{3}$ *.*•. Since, $\frac{7}{2}$, *a*, 3 are three consecutive terms of an A.P. 7. So, $a - \frac{7}{8} = 3 - a \implies 2a = 3 + \frac{7}{8}$

 $\Rightarrow \quad 2a = \frac{24+7}{8} = \frac{31}{8} \Rightarrow a = \frac{31}{16}$ Given, common difference, d = -68. Let *a* be the first term of the A.P. Given, $a_0 = 5$ \Rightarrow $a + (9 - 1) \times (-6) = 5 \Rightarrow a - 48 = 5 \Rightarrow a = 53$ Hence, first term of A.P. is 53. Given, common difference, d = 3 be the first term of 9. the A.P. Now, $a_{15} - a_9 = [a + (15 - 1)d] - [a + (9 - 1)d]$ $=14d - 8d = 6d = 6 \times 3 = 18$ [$\therefore d = 3$] **10.** Let *d* be the common difference of the A.P. Given, first term = a and nth term, $a_n = b$ $\Rightarrow a + (n-1)d = b \Rightarrow (n-1)d = b - a \Rightarrow d = \frac{b-a}{n-1}$ 11. $\therefore \frac{1}{yz}, \frac{1}{zx}$ and $\frac{1}{xy}$ are in A.P. $\Rightarrow \frac{1}{zx} - \frac{1}{yz} = \frac{1}{xy} - \frac{1}{zx} \Rightarrow \frac{y - x}{xyz} = \frac{z - y}{xyz}$ \Rightarrow $y - x = z - y \Rightarrow y = \frac{x + z}{2}$ \therefore *x*, *y* and *z* are in A.P. **12.** Given that, a = 4 and $d = \frac{4}{3}$. $S_n = \frac{n}{2} [2a + (n-1)d]$ •.• :. $S_{22} = \left(\frac{22}{2}\right) \left[(2)(4) + (22-1)\left(\frac{4}{3}\right) \right] = (11)(8+28) = 396$ **13.** Given, $a_n = 2n + 5$ \therefore $a_1 = 2(1) + 5 = 7, a_2 = 2(2) + 5 = 9,$ $a_3 = 2(3) + 5 = 11, a_4 = 2(4) + 5 = 13$ $S_4 = a_1 + a_2 + a_3 + a_4 = 7 + 9 + 11 + 13 = 40$ *.*... **14.** Let *a* and *d* are respectively the first term and common difference of the given A.P.

CHAPTER

Given,
$$a_4 = a + 3d = 11$$
 ...(i)
Also, $a_5 + a_7 = 34$ [Given]
 $\Rightarrow [a + 4d] + [a + 6d] = 34$

 \Rightarrow 2a + 10d = 34 \Rightarrow 2(11 - 3d) + 10d = 34 [Using (i)]

 $\Rightarrow 22 - 6d + 10d = 34 \Rightarrow 4d = 12 \Rightarrow d = 3$

15. The first 10 multiples of 3 are 3, 6, 9, 12, 15, 18, 21, 24, 27, 30.

It is an A.P. with first term, a = 3 and common difference, d = 3.

 \therefore Sum of first 10 multiplies of 3 = S_{10}

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$$= \frac{10}{2} \{2 \times 3 + (10 - 1) \times 3\} \qquad \left[\because S_n = \frac{n}{2} \{2a + (n - 1)d\} \right]$$

= 5(6 + 27) = 5 × 33 = 165
16. Here A.P. is $\sqrt{6}, \sqrt{24}, \sqrt{54}, \sqrt{96}, \dots$ then
 $a = \sqrt{6}, d = \sqrt{24} - \sqrt{6} = 2\sqrt{6} - \sqrt{6} = \sqrt{6}.$
 $\because S_n = \frac{n}{2} [2a + (n - 1)d] = \frac{n}{2} [2\sqrt{6} + (n - 1)\sqrt{6}]$
 $= \frac{n}{2} [\sqrt{6} \ n + \sqrt{6}] = \frac{\sqrt{6n(n + 1)}}{2}$

17. Here the smallest 3-digit number divisible by 7 is 105. So, the number of bacteria taken into consideration is 105, 112, 119,, 994

So, first term (a) = 105, d = 7 and last term = 994

(i) (c) : $t_5 = a + 4d = 105 + 28 = 133$

(ii) (b): Let *n* samples be taken under consideration.

 \therefore Last term = 994

 $\Rightarrow a + (n-1)d = 994 \Rightarrow 105 + (n-1)7 = 994 \Rightarrow n = 128$

(iii) (a) : Total number of bacteria in first 10 samples

= $S_{10} = \frac{10}{2} [2(105) + 9(7)] = 1365$

(iv) (a) : t_7 from end = $(128 - 7 + 1)^{\text{th}}$ term from beginning = 122^{th} term = 105 + 121(7) = 952

(v) (c) : $t_{50} = 105 + 49 \times 7 = 448$

18. Geeta's A.P. is -5, -2, 1, 4, ...

Here, first term $(a_1) = -5$ and common difference $(d_1) = -2 + 5 = 3$

Similarly, Madhuri's A.P. is 187, 184, 181, ... Here first term $(a_2) = 187$ and common difference $(d_2) = 184 - 187 = -3$

(i) $t_{34} = a_2 + 33d_2 = 187 + 33(-3) = 88$

- (ii) Required sum = 3 + (-3) = 0
- (iii) $t_{19} = a_1 + 18d_1 = (-5) + 18(3) = 49$

(iv)
$$S_{10} = \frac{n}{2} [2a_1 + (n-1)d_1] = \frac{10}{2} [2(-5) + 9(3)] = 85$$

(v) Let n^{th} terms of the two A.P.'s be equal. $\therefore -5 + (n-1)3 = 187 + (n-1)(-3)$ $\Rightarrow 6(n-1) = 192 \Rightarrow n = 33$

19. Number of pairs of shoes in 1^{st} , 2^{nd} , 3^{rd} row, ... are 3, 5, 7, ...

So, it forms an A.P. with first term a = 3, d = 5 - 3 = 2

(i) (d): Let *n* be the number of rows required. $\therefore S_n = 120$

$$\Rightarrow \frac{n}{2}[2(3)+(n-1)2]=120$$

 $\Rightarrow n^2 + 2n - 120 = 0 \Rightarrow n^2 + 12n - 10n - 120 = 0$ $\Rightarrow (n + 12) (n - 10) = 0 \Rightarrow n = 10$ So, 10 rows required to put 120 pairs.

(ii) (b): No. of pairs in 17^{th} row = $t_{17} = 3 + 16(2) = 35$ No. of pairs in 10^{th} row = $t_{10} = 3 + 9(2) = 21$ \therefore Required difference = 35 - 21 = 14

(iii) (c) : Here *n* = 15

 $\therefore t_{15} = 3 + 14(2) = 3 + 28 = 31$

(iv) (a) : No. of pairs in 30^{th} row = $t_{30} = 3 + 29(2) = 61$

(v) (c) : No. of pairs in 5th row =
$$t_5 = 3 + 4(2) = 11$$

No. of pairs in 8th row = $t_8 = 3 + 7(2) = 17$

 $\therefore \text{ Required sum} = 11 + 17 = 28$

20. Here $S_n = 0.1n^2 + 7.9n$

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(i)
$$S_{n-1} = 0.1(n-1)^2 + 7.9(n-1)$$

= $0.1n^2 + 7.7n - 7.8$

ii)
$$S_1 = t_1 = a = 0.1(1)^2 + 7.9(1) = 8 \text{ cm}$$

= Diameter of core

So, radius of the core = 4 cm

(iii) $S_2 = 0.1(2)^2 + 7.9(2) = 16.2$

(iv) Required diameter = $t_2 = S_2 - S_1 = 16.2 - 8 = 8.2$ cm

(v) As $d = t_2 - t_1 = 8.2 - 8 = 0.2$ cm

So, thickness of tissue = $0.2 \div 2 = 0.1$ cm = 1 mm

21. Here, first term *a* = 7

Common difference, d = 13 - 7 = 6

Let the given A.P. contains n terms, then

 $a_n = 187$ (:: Given) $\Rightarrow a + (n-1)d = 187$ $\Rightarrow 7 + (n-1)6 = 187 \Rightarrow (n-1)6 = 180$

 \Rightarrow $n-1=30 \Rightarrow n=30+1=31$

Thus, the given A.P. contains 31 terms.

Here n = 31 (odd number)

$$\therefore \quad \text{Middle term} = \frac{1}{2}(n+1)^{\text{th}}.$$

$$=\frac{1}{2}(31+1)^{\text{th}} = \left(\frac{1}{2} \times 32\right)^{\text{th}} = 16^{\text{th}}$$

Hence, middle term, $a_{16} = a + 15d = 7 + 15 \times 6 = 7 + 90 = 97$

22. The given A.P. is 27, 23, 19,..., -65.

Here, first term, a = 27, common difference, d = 23 - 27 = -4, last term, l = -65

Now, n^{th} term from the end = l - (n - 1)d

:. 11^{th} term from the end = -65 -(11 - 1)(-4) = -65 -(10) (-4) = -65 + 40 = -25

Hence, the 11^{th} term from the end is -25.

OR

Given, A.P. is 115, 110, 105, ...

Here, a = 115, d = 110 - 115 = -5Let n^{th} term of the given A.P. be the first negative term. *i.e.*, $a_n < 0 \Rightarrow a + (n - 1)d < 0$

 \Rightarrow 115 + (*n* - 1)(-5) < 0

 $\Rightarrow \quad 115-5n+5 < 0 \Rightarrow 120-5n < 0$

 $\Rightarrow \quad 5n \ge 120 \Rightarrow n \ge 24 \Rightarrow n \ge 25$

 \therefore 25th term of the given A.P. will be the first negative term.

23. Let a = 2 be the first term and d be the common difference of the A.P.

Given, 10th term of the A.P. is 47.

$$\therefore a_{10} = 2 + (10 - 1)d \qquad [\because a_n = a + (n - 1)d]$$

$$\Rightarrow 47 = 2 + 9d \Rightarrow 9d = 45 \Rightarrow d = 5$$
Now, $S_{15} = \frac{15}{2}[2a + (15 - 1)d] \qquad [\because S_n = \frac{n}{2}[2a + (n - 1)d]]$

$$= \frac{15}{2}[2 \times 2 + 14 \times 5] = \frac{15}{2}[4 + 70] = \frac{15}{2} \times 74 = 15 \times 37 = 555$$

Hence, the sum of 15 terms of the given A.P. is 555.

24. Given A.P. is 3, 7, 11, 15, Here, *a* = 3, *d* = 7 – 3 = 4 Let sum of *n* terms is 406.

$$∴ S_n = \frac{n}{2} [2a + (n-1)d]$$

$$⇒ 406 = \frac{n}{2} [2(3) + (n-1)(4)]$$

- $\Rightarrow \quad 406 = n[1+2n] \Rightarrow 2n^2 + n 406 = 0$
- $\Rightarrow \quad 2n^2 + 29n 28n 406 = 0$
- $\Rightarrow n(2n+29) 14(2n+29) = 0 \Rightarrow (n-14)(2n+29) = 0$
- \Rightarrow *n* = 14 [Since, *n* can't be a fraction]

25. Given, $S_n = 2n^2 + 3n$

- We know that, $a_n = S_n S_{n-1}$
- $\therefore \quad a_{16} = S_{16} S_{15} = [2(16)^2 + 3(16)] [2(15)^2 + 3(15)] = [2(256) + 3(16)] [2(225) + 3(15)] = [512 + 48] [450 + 45] = 560 495 = 65$

26. Sum of all natural numbers from 1 to 1000 which are not divisible by $5 = (Sum of all natural numbers from 1 to 1000, <math>S_n) - (Sum of all natural numbers from 1 to 1000 which are divisible by <math>5, S_n')$

Now, all the natural numbers from 1 to 1000 are 1, 2, 3, ..., 1000, which is an A.P. where *a* = 1, *l* = 1000 and *n* = 1000

$$\therefore \quad S_n = \frac{n}{2} [a+l] \\ = \frac{1000}{2} [1+1000] = 500 \times 1001 = 500500 \qquad \dots (i)$$

Again, all the natural numbers from 1 to 1000 which are divisible by 5 are 5, 10, 15,, 1000, which is also an A.P. where, first term, a = 5, last term, l = 1000 and common difference, d = 5

$$\begin{array}{ll} \therefore & a_n = a + (n-1)d \implies 1000 = 5 + (n-1)5 \\ \Rightarrow & 5n = 1000 \Rightarrow n = 200 \\ \therefore & S'_n = \frac{n}{2}[a+l] = \frac{200}{2}[5+1000] = 100 \times 1005 = 100500 \\ & \dots (ii) \end{array}$$

:. Required sum = $S_n - S'_n = 500500 - 100500 = 400000$

27. Given, *a* = 100

Let d be the common difference of the A.P.

According to the question,

100 + (100 + d) + (100 + 2d) + (100 + 3d) + (100 + 4d) + (100 + 5d) = 5[(100 + 6d) + (100 + 7d) + (100 + 8d) + (100 + 9d) + (100 + 10d) + (100 + 11d)]

- $\Rightarrow 600 + 15d = 5(600 + 51d)$
- $\Rightarrow 120 + 3d = 600 + 51d \Rightarrow -48d = 480 \Rightarrow d = -10$

28. Let *a* and *d* be the first term and common difference of the A.P.

$$S_n = \frac{n}{2} [2a + (n-1)d]$$
Consider, $S_{10} - S_5 = \frac{10}{2} [2a + 9d] - \frac{5}{2} [2a + 4d]$

$$= 5(2a + 9d) - 5(a + 2d)$$

$$= 5[2a + 9d - a - 2d] = 5(a + 7d) \qquad \dots (i)$$
Also, $S_n = \frac{15}{2} [2a + 14d] = 15(a + 7d) = 2[5(a + 7d)]$

Also,
$$S_{15} = \frac{15}{2}[2a + 14d] = 15(a + 7d) = 3[5(a + 7d)]$$

= 3 ($S_{10} - S_5$) (From (i))

OR

Let *a* be the first term and *d* be the common difference of given A.P. Then

$$(p+q)^{\text{th}}$$
 term, $a_{p+q} = a + (p+q-1)d$...(i)

and
$$(p-q)^{\text{ut}}$$
 term, $a_{p-q} = a + (p-q-1)d$...(ii)

:. Sum of $(p+q)^{\text{tn}}$ and $(p-q)^{\text{tn}}$ terms = $a_{p+q} + a_{p-q}$ = [a + (p+q-1)d] + [a + (p-q-1)d] [Using (i) and (ii)] = 2a + (p+q-1+p-q-1)d

= $2a + (2p - 2)d = 2 \times [a + (p - 1)d] = 2 \times p^{\text{th}}$ term of the A.P. 29. Given, A.P. is 8, 10, 12,...

Here, first term, a = 8 and common difference (d) = 10 - 8 = 2If the given A.P. has a total 60 terms, then

$$a_{60} = a + 59d$$
 [: $a_n = a + (n - 1)d$]
= $8 + 59 \times 2 = 8 + 118 = 126$

Sum of the last 10 terms of the given A.P.
=
$$a_{51} + a_{52} + ... + a_{60} = (a + 50d) + (a + 51d) + ... + 126$$

= $(8 + 100) + (8 + 102) + ... + 126 = 108 + 110 + ... + 126$
= $\frac{10}{2}[108 + 126]$ [:: $S_n = \frac{n}{2}$ (First term + Last term)]
= $5 \times 234 = 1170$

30. Let the four parts be (*a* – 3*d*), (*a* – *d*), (*a* + *d*), (*a* + 3*d*). Sum of the numbers = 56

$$\Rightarrow (a - 3d) + (a - d) + (a + d) + (a + 3d) = 56$$

$$\Rightarrow 4a = 56 \Rightarrow a = 14$$

Also, $\frac{(a - 3d)(a + 3d)}{(a - d)(a + d)} = \frac{5}{6}$ [Given] $\Rightarrow \frac{a^2 - 9d^2}{a^2 - d^2} = \frac{5}{6}$

$$\Rightarrow 6(196 - 9d^2) = 5(196 - d^2)$$
 [: $a = 14$]

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 $\Rightarrow 6 \times 196 - 54d^2 = 5 \times 196 - 5d^2$

- $\Rightarrow 49d^2 = 6 \times 196 5 \times 196 \Rightarrow 49d^2 = 196$
- $\Rightarrow d^2 = 4 \Rightarrow d = \pm 2$
- ... Required four parts are
- $(14 3 \times 2), (14 2), (14 + 2), (14 + 3 \times 2)$
- or [(14 3(-2)], (14 + 2), (14 2), [(14 + 3(-2)]].
- *i.e.*, 8, 12, 16, 20 or 20, 16, 12, 8

31. The given sequence is 12000, 16000, 20000,, which is an A.P.

Here first term, a = 12000, common difference, d = 4000, $S_n = 1000000$

Let the man saves ₹ 1000000 in n years.

Now,
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

 $\Rightarrow \quad 1000000 = \frac{n}{2} [2 \times 12000 + (n-1)4000]$

$$\Rightarrow \quad 1000 = \frac{n}{2} [24 + 4n - 4] \Rightarrow 1000 = \frac{n}{2} \times 4(n+5)$$

- \Rightarrow 500 = n^2 + 5n \Rightarrow n^2 + 5n 500 = 0
- $\Rightarrow n^2 + 25n 20n 500 = 0 \Rightarrow (n + 25)(n 20) = 0$
- \Rightarrow *n* = 20 (as *n* can't be negative)
- Man saves ₹ 1000000 in 20 years. *.*..

OR

Total amount of ten prizes = ₹1600 Let the value of first prize be $\overline{\mathbf{x}}$ According to the question, prizes are *x*, *x* – 20, *x* – 40 … to 9 terms Here, a = x, d = -20 and n = 10

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

⇒ 1600 = $\frac{10}{2} [2x + (10-1)(-20)] = 10(x - 1)(-20)$

 \Rightarrow 160 = x - 90 \Rightarrow x = 160 + 90 = 250

Hence, amount of each prize (in ₹) are 250, 230, 210, ..., 70.

90)

...(i)

32. Let a and d are respectively the first term and common difference of an A.P.:, a, a + d, a + 2d,...

Given, 14th term of an A.P. is twice its 8th term.

$$\therefore \quad a_{14} = 2a_8 \Rightarrow a + (14 - 1)d = 2[a + (8 - 1)d]$$

$$\Rightarrow a + 13d = 2a + 14d \Rightarrow 2a - a = (13 - 14)d$$
$$\Rightarrow a = -d$$

$$\Rightarrow a = -a$$

Also, $a_c = -8$

Also,
$$a_6 = -8$$
 (Given)
 $\Rightarrow a + (6-1)d = -8 \Rightarrow -d + 5d = -8$ [Using (i)]

$$\Rightarrow 4d = -8 \Rightarrow d = -2$$

From (i), a = -(-2) = 2

Therefore, the A.P. is 2, 2 + (-2), 2 + 2(-2), 2 + 3(-2),...*i.e.*, 2, 0, -2, -4,...

∴
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

∴ $S_{20} = \frac{20}{2} [2 \times 2 + (20-1)(-2)]$
 $= 10[4 - 38] = 10(-34) = -340$

33. Here, 8 and 20 are the first term and common difference respectively of an A.P.

:
$$S_n = \frac{n}{2} [2(8) + (n-1)20] = 8n + 10n^2 - 10n$$

= $10n^2 - 2n$...(i)

Also, -30 and 8 are the first term and common difference respectively of another A.P.

$$S_{2n} = \frac{2n}{2} [2(-30) + (2n-1)8]$$

= -60n + 16n² - 8n = 16n² - 68n ...(ii)
According to the question, $S_n = S_{2n}$

$$\Rightarrow 16n^2 - 68n = 10n^2 - 2n$$
 [From (i) and (ii)]

- $\Rightarrow 16n^2 10n^2 68n + 2n = 0$
- $\Rightarrow 6n^2 66n = 0 \Rightarrow 6n(n 11) = 0$

$$\Rightarrow \text{ Either } n - 11 = 0 \text{ or } n = 0 \Rightarrow n = 11 \text{ or } n = 0$$

n = 0 is not possible. •.•

Hence, value of *n* is 11.

OR

Consider the sequence, 2, 5, 8, 11, ..., x, which is an A.P. Here, a = 2, d = 3, $a_n = x$

$$\therefore \quad a_n = a + (n-1)d \Rightarrow x = 2 + (n-1)3$$

$$\Rightarrow \quad x = 2 + 3n - 3 \Rightarrow x + 1 = 3n \Rightarrow \quad n = \frac{x+1}{3}$$

$$\therefore \quad S_n = \frac{n}{2}[a+1] \Rightarrow 345 = \frac{x+1}{3\times 2}[2+x][\text{Given}, S_n = 345]$$

$$(x + 1)(x + 2) = 2070 \Rightarrow x^2 + 3x - 2068 = 0$$

$$\Rightarrow x = \frac{-3 \pm \sqrt{9 + 8272}}{2} = \frac{-3 \pm \sqrt{8281}}{2} = \frac{-3 \pm 91}{2} = 44, -47$$

Since, the given A.P. is an increasing A.P. with a = 2 and d = 3, so x can't be negative.

 $\therefore x = 44$

=

 \Rightarrow

34. Let a = 8 years be the first term of the A.P.

i.e., age of the youngest boy participating in a painting competition.

Common difference, d i.e., age difference of the participants = 4 months (given)

$$=\frac{4}{12}$$
 year $=\frac{1}{3}$ year

Let *n* be the total number of participants in the painting competition and S_n denotes the sum of ages of all the participants. Then, $S_n = 168$ years (given)

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 168 = \frac{n}{2} \left[2 \times 8 + (n-1) \left(\frac{1}{3}\right) \right]$$

$$\Rightarrow 336 = n \left[16 + (n-1) \left(\frac{1}{3}\right) \right]$$

$$\Rightarrow 336 \times 3 = n [48 + (n-1)] \Rightarrow 1008 = 48n + n(n-1)$$

$$\Rightarrow 1008 = 48n + n^2 - n \Rightarrow n^2 + 47n - 1008 = 0$$

$$\Rightarrow n^2 + 63n - 16n - 1008 = 0 \Rightarrow n(n+63) - 16(n+63) = 0$$

$$\Rightarrow (n-16) (n+63) = 0$$

Either n - 16 = 0 or n + 63 = 0 \rightarrow

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 \Rightarrow Either n = 16 or n = -63

$$\Rightarrow$$
 n = 16, rejecting *n* = -63 as *n* can't be negative.

 \therefore Age of eldest participant is a_{16} .

Now,
$$a_{16} = 8 + (16 - 1) \times \frac{1}{3}$$
 [: $a_n = a + (n - 1)d$]
= $8 + \frac{15}{3} = 8 + 5 = 13$ years

Hence, the total number of participants are 16 and the age of the eldest participant is 13 years.

35. Original cost of house = ₹2200000

Amount paid in cash = ₹400000

Balance to be paid = ₹(2200000 – 400000) = ₹1800000 Amount paid in each installment = ₹100000

 \therefore Number of installments = 18

Interest paid with 1st installment = $1800000 \times \frac{10}{100}$ = ₹ 180000

Interest paid with 2nd installment = $1700000 \times \frac{10}{100}$ = ₹ 170000

and so on

Interest paid with last installment = $100000 \times \frac{10}{100}$ = ₹ 10000

Total interest paid = (180000 + 170000 + + 10000), which is an A.P. with first term, *a* = 180000,

last term, *l* = 10000.

$$= \frac{18}{2} [180000 + 10000] \qquad \left[\because S_n = \frac{n}{2} (a+l) \right]$$

= 9[190000] = ₹ 1710000

 \therefore Total cost of house for Ronit

= ₹ (2200000 + 1710000) = ₹ 3910000

OR

Since, the A.P. consists of 37 terms, so 19th term is the middle term.

Let $a_{19} = a$ and d be the common difference of the A.P. The A.P. is ; a - 18d, a - 17d,..., a - d, a, a + d,..., a + 17d, a + 18d

Sum of the three middle most terms = 225

$$\Rightarrow (a - d) + a + (a + d) = 225$$

$$\Rightarrow 3a = 225 \Rightarrow a = 75$$
 ...(i)
Sum of the three last terms = 429

$$\Rightarrow (a + 18d) + (a + 17d) + (a + 16d) = 429 \Rightarrow 3a + 51d = 429 \Rightarrow a + 17d = 143$$

$$\Rightarrow 17d = 143 - a = 143 - 75$$
 (Using (i))

$$\Rightarrow 17d = 68 \Rightarrow d = \frac{68}{17} = 4$$

Now, first term = $a - 18d = 75 - 18 \times 4 = 3$

:. The A.P. is 3, 7, 11, ..., 147.

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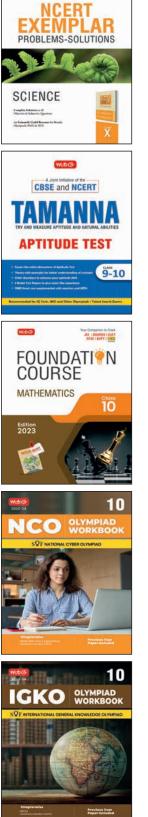
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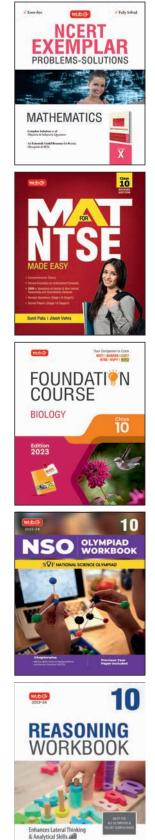
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