# Some Applications of Trigonometry

60 m



### **SOLUTIONS**

#### **EXERCISE - 9.1**

Here, AB is the pole and AC is the rope tied to the point C on the ground.

In right  $\triangle ABC$ ,

$$\frac{AB}{AC} = \sin 30^{\circ} \implies \frac{AB}{AC} = \frac{1}{2} \implies \frac{AB}{20} = \frac{1}{2}$$

$$\Rightarrow$$
  $AB = 20 \times \frac{1}{2} = 10 \text{ m}$ 

Thus, the required height of the pole is 10 m.

Let the tree *OP* is broken at *A* and its top is touching the ground at *B*.

Now, in right  $\triangle AOB$ ,

$$\frac{AO}{OB} = \tan 30^{\circ}$$

$$\Rightarrow \frac{AO}{8} = \frac{1}{\sqrt{3}}$$

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$$\Rightarrow AO = \frac{8}{\sqrt{3}} \text{ m}$$

Also, 
$$\frac{AB}{OB} = \sec 30^{\circ}$$

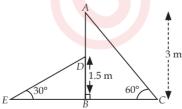
$$\Rightarrow \frac{AB}{8} = \frac{2}{\sqrt{3}} \Rightarrow AB = \frac{2 \times 8}{\sqrt{3}} = \frac{16}{\sqrt{3}} \text{ m}$$

Now, height of the tree OP = OA + AP = OA + AB

$$[\cdot,\cdot] AP = AB$$

$$= \frac{8}{\sqrt{3}} + \frac{16}{\sqrt{3}} = \frac{24}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 8\sqrt{3} \text{ m}$$

In the figure, DE is the slide for younger children, whereas AC is the slide for elder children.



In right  $\triangle ABC$ ,

$$\therefore \frac{AB}{AC} = \sin 60^{\circ}$$

$$\Rightarrow \frac{3}{AC} = \frac{\sqrt{3}}{2} \Rightarrow AC = \frac{2 \times 3}{\sqrt{3}} = 2\sqrt{3} \text{ m}$$
Again, in right  $\triangle BDE$ ,

$$\frac{DE}{BD} = \csc 30^{\circ} = 2$$

$$\Rightarrow \frac{DE}{1.5} = 2 \Rightarrow DE = 2 \times 1.5 = 3 \text{ m}$$

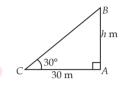
Thus, the lengths of slides are 3 m and  $2\sqrt{3}$  m.

In right  $\triangle ABC$ , AB = height of the tower and point Cis 30 m away from the foot of the tower.

$$AC = 30 \text{ m}$$

Now, 
$$\frac{AB}{AC} = \tan 30^{\circ} \implies \frac{h}{30} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow h = \frac{30}{\sqrt{3}} = \frac{30}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 10\sqrt{3}$$



Thus, the required height of the tower is  $10\sqrt{3}$  m.

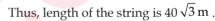
Let OB =Length of the string

AB = 60 m = Height of the kite.In right  $\triangle AOB$ ,

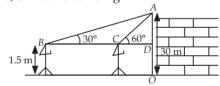
$$\frac{OB}{AB} = \csc 60^{\circ}$$

$$\Rightarrow \frac{OB}{60} = \frac{2}{\sqrt{3}}$$

$$\Rightarrow OB = \frac{2 \times 60}{\sqrt{3}} = \frac{120 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = 40\sqrt{3} \text{ m}$$



Here, *OA* is the building



In right  $\triangle ABD$ ,

$$\frac{AD}{BD} = \tan 30^{\circ} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow$$
 BD = AD $\sqrt{3}$  = 28.5 $\sqrt{3}$  m

$$[:: AD = 30 \text{ m} - 1.5 \text{ m} = 28.5 \text{ m}]$$

Also, in right  $\triangle ACD$ ,

$$\frac{AD}{CD} = \tan 60^\circ = \sqrt{3} \Rightarrow CD = \frac{AD}{\sqrt{3}} = \frac{28.5}{\sqrt{3}} \text{ m}$$

Now, 
$$BC = BD - CD = 28.5\sqrt{3} - \frac{28.5}{\sqrt{2}}$$

$$= 28.5 \left[ \sqrt{3} - \frac{1}{\sqrt{3}} \right] = 28.5 \left[ \frac{3-1}{\sqrt{3}} \right]$$

$$=28.5 \times \frac{2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{28.5 \times 2 \times \sqrt{3}}{3}$$

$$= 9.5 \times 2 \times \sqrt{3} = 19\sqrt{3} \text{ m}$$

Thus, the distance walked by the boy towards the building is  $19\sqrt{3}$  m.

7. Let BC be the building of height 20 m and CD be the tower of height x m.

Let the point *A* be at a distance of *y* m from the foot of the building.

Now, in right  $\triangle ABC$ ,

$$\frac{BC}{AB} = \tan 45^{\circ} = 1$$

$$\Rightarrow \frac{20}{y} = 1 \Rightarrow y = 20 \text{ i.e., } AB = 20 \text{ m.}$$
Now, in right  $\triangle ABD$ ,
$$\frac{BD}{AB} = \tan 60^{\circ}$$

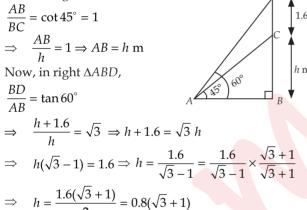
$$\Rightarrow \frac{20+x}{20} = \sqrt{3} \Rightarrow 20+x = 20\sqrt{3}$$

$$\Rightarrow x = 20\sqrt{3} - 20 = 20(\sqrt{3} - 1)$$

Thus, the height of the tower is  $20(\sqrt{3} - 1)$  m.

**8.** In the figure, DC represents the statue of height 1.6 m and BC represents the pedestal of height h m.

Now, in right  $\triangle ABC$ ,



Thus, the height of the pedestal is  $0.8(\sqrt{3} + 1)$  m.

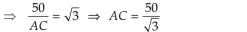
9. In the figure, let  $\overline{AB}$  be the building of height h m and  $\overline{CD}$  be the tower of height 50 m. Now, in right  $\Delta ABC$ ,

$$\frac{AC}{AB} = \cot 30^{\circ} = \sqrt{3}$$

$$\Rightarrow \frac{AC}{h} = \sqrt{3} \Rightarrow AC = h\sqrt{3} \quad ...(1)$$
In right  $\triangle DCA$ ,

 $\frac{DC}{AC} = \tan 60^{\circ}$ 

$$\frac{1}{AC} = \tan 60^{\circ}$$

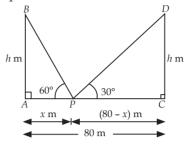


From (1) and (2), we get

$$\sqrt{3}h = \frac{50}{\sqrt{3}} \implies h = \frac{50}{\sqrt{3}} \times \frac{1}{\sqrt{3}} = \frac{50}{3}$$

Thus, the height of the building is  $16\frac{2}{3}$  m.

**10.** In the figure, let AB and CD are the poles of equal height h m and P be the point on the road at a distance of x m from the pole AB.



$$\therefore CP = (80 - x)$$

Now, in right  $\triangle APB$ ,

$$\frac{AB}{AP} = \tan 60^{\circ}$$

$$\Rightarrow \frac{h}{x} = \sqrt{3} \Rightarrow h = x\sqrt{3} \qquad \dots(1)$$

Again in right  $\triangle CPD$ ,

$$\frac{CD}{CP} = \tan 30^{\circ}$$

$$\Rightarrow \frac{h}{(80 - x)} = \frac{1}{\sqrt{3}} \Rightarrow h = \frac{80 - x}{\sqrt{3}} \qquad \dots(2)$$

From (1) and (2), we get

$$\sqrt{3}x = \frac{80 - x}{\sqrt{3}}$$

$$\sqrt{3} \times \sqrt{3} \times x = 80 - x$$

$$\Rightarrow \sqrt{3} \times \sqrt{3} \times x = 80 - x \Rightarrow 3x = 80 - x$$

$$\Rightarrow 3x + x = 80 \Rightarrow 4x = 80 \Rightarrow x = \frac{80}{4} = 20$$

$$CP = 80 - x = 80 - 20 = 60$$

Now, from (1), we have  $h = 20\sqrt{3}$ 

Thus, the required point is 20 m away from the first pole and 60 m away from the second pole and height of each pole is  $20\sqrt{3}$  m.

**11.** In the figure, let AB be the TV tower of height h m and C be the point on the other bank of the canal at a distance of x m from B. D be another point 20 m away from point C.

 $\therefore$  BC = x m and CD = 20 m

Now, in right  $\triangle ABC$ ,

$$\frac{AB}{BC} = \tan 60^{\circ} \implies \frac{h}{x} = \sqrt{3} \implies h = \sqrt{3}x \text{ m} \qquad \dots(1)$$

In right  $\triangle ABD$ ,

50 m

...(2)

$$\frac{AB}{BD} = \tan 30^{\circ}$$

$$\Rightarrow \frac{h}{x+20} = \frac{1}{\sqrt{3}} \Rightarrow h = \frac{x+20}{\sqrt{3}} \text{ m} \qquad ...(2)$$

From (1) and (2), we get

$$\sqrt{3}x = \frac{x+20}{\sqrt{3}} \implies 3x = x+20$$

$$\Rightarrow$$
 3x - x = 20  $\Rightarrow$  2x = 20  $\Rightarrow$  x =  $\frac{20}{2}$  = 10 m

Now, from (1), we get  $h = 10\sqrt{3}$  m

Thus, the height of the tower is  $10\sqrt{3}$  m and width of the canal is 10 m.

**12.** In the figure, let AB be the building of height 7 m. Let BC = AE = x m

Let CD be the height of the cable tower and DE = h m.

 $\therefore$  In right  $\triangle DAE$ ,

$$\frac{DE}{EA} = \tan 60^{\circ} \implies \frac{h}{x} = \sqrt{3}$$

$$\Rightarrow h = \sqrt{3}x$$

Again, in right  $\triangle ABC$ ,

$$\frac{AB}{BC} = \tan 45^{\circ}$$

$$\Rightarrow \quad \frac{7}{x} = 1 \quad \Rightarrow \quad x = 7 \qquad \dots (2)$$

From (1) and (2), we get

$$h = 7\sqrt{3} \Rightarrow DE = 7\sqrt{3}$$

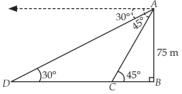
$$\therefore$$
 CD = CE + ED =  $(7 + 7\sqrt{3}) = 7(1 + \sqrt{3})$ 

Thus, the height of the cable tower is  $7(1 + \sqrt{3})$  m.

**13.** In the figure, let *AB* be the light house.

$$\therefore AB = 75 \text{ m}$$

Let the positions of two ships be *C* and *D* such that angle of depression from *A* are 45° and 30° respectively.



Now, in right  $\triangle ABC$ ,

$$\frac{AB}{BC} = \tan 45^{\circ} \Rightarrow \frac{75}{BC} = 1 \Rightarrow BC = 75 \text{ m}$$

Again, in right  $\triangle ABD$ ,

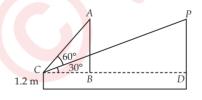
$$\frac{AB}{BD} = \tan 30^{\circ} \implies \frac{75}{BD} = \frac{1}{\sqrt{3}} \implies BD = 75\sqrt{3} \text{ m}$$

Now, the distance between the two ships = CD

$$= BD - BC = 75\sqrt{3} - 75 = 75(\sqrt{3} - 1)$$
m

Thus, the required distance between the ships is  $75(\sqrt{3} - 1)$  m.

**14.** In the figure, let *C* be the position of the girl. *A* and *P* are two positions of the balloon. *CD* is the horizontal line from the eyes of the girl.



Here, PD = AB = 88.2 m - 1.2 m = 87 mIn right  $\triangle ABC$ ,

$$\frac{AB}{BC} = \tan 60^{\circ} \Rightarrow \frac{87}{BC} = \sqrt{3} \Rightarrow BC = \frac{87}{\sqrt{3}} \text{ m}$$

In right  $\Delta PDC$ ,

$$\frac{PD}{CD} = \tan 30^{\circ} \implies \frac{87}{CD} = \frac{1}{\sqrt{3}} \implies CD = 87\sqrt{3} \text{ m}$$

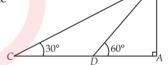
Now, BD = CD - BC

$$=87\sqrt{3}-\frac{87}{\sqrt{3}}=87\left(\sqrt{3}-\frac{1}{\sqrt{3}}\right)=87\times\left(\frac{3-1}{\sqrt{3}}\right)=\frac{2\times87}{\sqrt{3}}$$

$$=\frac{2\times87\times\sqrt{3}}{3}=2\times29\times\sqrt{3}=58\sqrt{3} \text{ m}$$

Thus, the required distance between the two positions of the balloon is  $58\sqrt{3}$  m.

**15.** In the figure, let AB be the tower and C, D be the two positions of the car. In right  $\Delta ABD$ ,



30° \ 60°

$$\Rightarrow \frac{AB}{AD} = \sqrt{3} \Rightarrow AB = \sqrt{3}AD \qquad ...(1)$$

In right  $\triangle ABC$ ,

$$\frac{AB}{AC} = \tan 30^{\circ}$$

 $\frac{AB}{AD} = \tan 60^{\circ}$ 

$$\Rightarrow \frac{AB}{AC} = \frac{1}{\sqrt{3}} \Rightarrow AB = \frac{AC}{\sqrt{3}} \qquad ...(2)$$

From (1) and (2), we get

$$\sqrt{3}AD = \frac{AC}{\sqrt{3}}$$

$$\Rightarrow$$
  $AC = \sqrt{3} \times \sqrt{3} \times AD = 3AD$ 

Now, 
$$CD = AC - AD = 3AD - AD = 2AD$$

Since the distance 2AD is covered in 6 seconds,

The distance AD will be covered in  $\frac{6}{2}$  *i.e.*, 3 seconds.

Thus, the time taken by the car to reach the tower from *D* is 3 seconds.

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