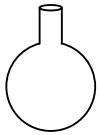


Surface Areas and Volumes

EXAM DRILL

SOLUTIONS

1. (a) : The shape of Surahi is as



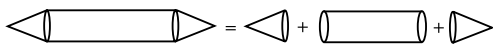
, which is combination of sphere and cylinder.

2. (b) : Let the radius of the cone be r cm.

Since, the height and diameter of the base of the largest right circular cone = Edge of the cube.

$$\therefore 2r = 8 \text{ cm} \Rightarrow r = 4 \text{ cm}$$

3. (c) : The given figure is



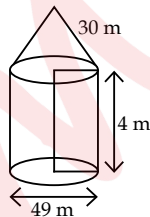
= Cone + Cylinder + Cone
= Two cones and a cylinder

4. (b) : Because the sphere is enclosed in the cylinder, therefore the diameter of sphere is equal to the diameter of cylinder which is $2r$ cm.

5. (a) : Area of canvas required =
Curved surface area of cylinder +
Curved surface area of cone
 $= 2\pi rh + \pi rl$

$$= \pi r[2h + l] = \frac{22}{7} \times \frac{98}{2} [2 \times 4 + 30]$$

$$= 5852 \text{ m}^2$$



6. When, we join two solid hemispheres along their bases of radius r , we get a solid sphere. Also, curved surface area of a hemisphere is $2\pi r^2$.

$$\text{Hence, the curved surface area of new solid} = 2\pi r^2 + 2\pi r^2 = 4\pi r^2.$$

7. Because solid ball is exactly fitted inside the cubical box of side a . So, a is the diameter of the solid ball.

$$\therefore \text{Radius of the ball} = \frac{a}{2} \quad [\because \text{diameter} = 2 \times \text{radius}]$$

$$\text{So, volume of the ball} = \frac{4}{3} \pi \left(\frac{a}{2}\right)^3 = \frac{1}{6} \pi a^3$$

8. (i) Lateral surface area of *Hermika* which is cubical in shape $= 4a^2 = 4 \times (8)^2 = 256 \text{ m}^2$

- (ii) Diameter of cylindrical base = 42 m

$$\therefore \text{Radius of cylindrical base} (r) = 21 \text{ m}$$

Height of cylindrical base (h) = 12 m

$$\therefore \text{Number of bricks used} = \frac{\frac{22}{7} \times 21 \times 21 \times 12}{0.01}$$

$$= 1663200$$

- (iii) Given, diameter of *Anda* which is hemispherical in shape = 42 m

$$\Rightarrow \text{Radius of } Anda (r) = 21 \text{ m}$$

$$\therefore \text{Volume of } Anda = \frac{2}{3} \pi r^3 = \frac{2}{3} \times \frac{22}{7} \times 21 \times 21 \times 21$$

$$= 44 \times 21 \times 21 = 19404 \text{ m}^3$$

- (iv) Given, radius of *Pradakshina Path* (r) = 25 m

$$\therefore \text{Perimeter of path} = 2\pi r$$

$$= \left(2 \times \frac{22}{7} \times 25\right) \text{ m}$$

$$\therefore \text{Distance covered by priest} = 14 \times 2 \times \frac{22}{7} \times 25$$

$$= 2200 \text{ m}$$

- (v) \therefore Radius of *Anda* (r) = 21 m

$$\therefore \text{Curved surface area of } Anda = 2\pi r^2$$

$$= 2 \times \frac{22}{7} \times 21 \times 21 = 2772 \text{ m}^2$$

9. We have, radius of each coin = 3.5 cm

$$= \frac{35}{10} \text{ cm} = \frac{7}{2} \text{ cm}$$

$$\text{Thickness of each coin} = 0.5 \text{ cm} = \frac{1}{2} \text{ cm}$$

$$\text{So, height of cylinder made by Meera} (h_1) = 12 \times \frac{1}{2} = 6 \text{ cm}$$

and height of cylinder made by Dhara (h_2)

$$= 8 \times \frac{1}{2} = 4 \text{ cm}$$

- (i) (b) : Curved surface area of cylinder made by Meera

$$= 2 \times \frac{22}{7} \times \frac{7}{2} \times 6 = 132 \text{ cm}^2$$

- (ii) (b) : Required ratio

$$= \frac{\text{Curved surface area of cylinder made by Meera}}{\text{Curved surface area of cylinder made by Dhara}}$$

$$= \frac{2\pi rh_1}{2\pi rh_2} = \frac{h_1}{h_2} = \frac{6}{4} = \frac{3}{2} \text{ i.e., } 3:2$$

- (iii) (a) : Volume of cylinder made by Dhara $= \pi r^2 h_2$

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 4 = 154 \text{ cm}^3$$

(iv) (c) : Required ratio

$$= \frac{\text{Volume of cylinder made by Meera}}{\text{Volume of cylinder made by Dhara}}$$

$$= \frac{\pi r^2 h_1}{\pi r^2 h_2} = \frac{h_1}{h_2} = \frac{6}{4} = \frac{3}{2} \text{ i.e., } 3:2$$

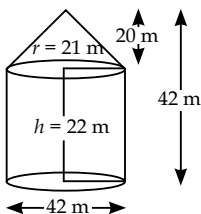
(v) (a) : When two coins are shifted from Meera's cylinder to Dhara's cylinder, then length of both cylinders become equal.
So, volume of both cylinders become equal.

10. (i) (c) : Required area of canvas = Curved surface area of cone + Curved surface area of cylinder

$$= \pi r l + 2\pi r h = \pi r (l + 2h)$$

$$= \frac{22}{7} \times 21 (29 + 44) = 4818 \text{ m}^2$$

$$\left[\because l = \sqrt{r^2 + h_1^2} = \sqrt{(21)^2 + (20)^2} \right. \\ \left. = \sqrt{841} = 29 \text{ m} \right]$$



(ii) (b) : Area of floor = πr^2

$$= \frac{22}{7} \times 21 \times 21 = 1386 \text{ m}^2$$

Number of persons that can be accommodated in the

$$\text{tent} = \frac{1386}{126} = 11$$

(iii) (d) : Since, cost of 100 m^2 of canvas = ₹ 425

\therefore Cost of 1 m^2 of canvas = ₹ 4.25

Thus, cost of 4818 m^2 of canvas = ₹ 20476.50

(iv) (c) : Volume of tent = Volume of cone + Volume of

$$\text{cylinder} = \frac{1}{3} \pi r^2 h_1 + \pi r^2 h = \pi r^2 \left(\frac{1}{3} h_1 + h \right)$$

$$= \frac{22}{7} \times (21)^2 \left[\frac{20}{3} + 22 \right] = \frac{9702}{7} \times \frac{86}{3} = 39732 \text{ m}^3$$

(v) (a) : Required number of persons

$$= \frac{\text{Volume of tent}}{\text{Space required by one person}} = \frac{39732}{1892} = 21$$

11. (i) Curved surface area of two identical cylindrical

$$\text{parts} = 2 \times 2\pi r h = 2 \times 2 \times \frac{22}{7} \times \frac{2.5}{2} \times 5$$

$$= 78.57 \text{ cm}^2$$

(ii) Volume of big cylindrical part = $\pi r^2 h$

$$= \frac{22}{7} \times \frac{4.5}{2} \times \frac{4.5}{2} \times 12 = 190.93 \text{ cm}^3$$

(iii) Volume of two hemispherical ends = $2 \times \frac{2}{3} \pi r^3$

$$= \frac{2 \times 2}{3} \times \frac{22}{7} \times \left(\frac{2.5}{2} \right)^3 = 8.18 \text{ cm}^3$$

(iv) Curved surface area of two hemispherical ends

$$= 2 \times 2\pi r^2 = 2 \times 2 \times \frac{22}{7} \times \frac{2.5}{2} \times \frac{2.5}{2} = 19.64 \text{ cm}^2$$

(v) Difference of volume of bigger cylinder to two small hemispherical ends = $190.93 - 8.18 = 182.75 \text{ cm}^3$

12. Radius of the sphere (r) = $\frac{18}{2} \text{ cm} = 9 \text{ cm}$

Radius of the cylinder (R) = $\frac{36}{2} \text{ cm} = 18 \text{ cm}$

Let us assume that the water level in the cylinder rises by h cm.

After the sphere is completely submerged,

Volume of the sphere = Volume of water raised in the cylinder

$$\Rightarrow \frac{4}{3} \pi r^3 = \pi R^2 h \Rightarrow \frac{4}{3} \pi (9)^3 = \pi (18)^2 \times h$$

$$\Rightarrow h = \frac{4 \times 9 \times 9 \times 9}{3 \times 18 \times 18} \Rightarrow h = 3$$

Thus, the water level in the cylinder rises by 3 cm.

13. Let l , r and h be the slant height, radius and height of the conical top respectively.

$$\therefore l^2 = r^2 + h^2 = 3^2 + 4^2 = 25 = 5^2 \Rightarrow l = 5 \text{ m}$$

Curved surface area of cylindrical part = $2\pi r h$

$$= 2\pi(3)(10) = 60\pi \text{ m}^2$$

Curved surface area of conical part = $\pi r l = \pi(3)(5)$

$$= 15\pi \text{ m}^2$$

\therefore Curved surface area of pillar

= Curved surface area of cylindrical part + Curved surface area of conical part = $60\pi + 15\pi = 75\pi \text{ m}^2$

14. Volume of one cube = 64 cm^3

$$\Rightarrow (\text{Edge})^3 = 64 \text{ cm}^3 \Rightarrow \text{Edge} = 4 \text{ cm}$$

Length of the cuboid (l) = $5 \times \text{Edge} = 5 \times 4 = 20 \text{ cm}$

breadth (b) = 4 cm and height (h) = 4 cm

\therefore Surface area of cuboid = $2(lb + bh + hl)$

$$= 2[20 \times 4 + 4 \times 4 + 4 \times 20] = 2 \times 176 = 352 \text{ cm}^2$$

Volume of the cuboid = $l \times b \times h$

$$= 20 \times 4 \times 4 = 320 \text{ cm}^3$$

15. Radius of the

hemisphere and cylinder, r

$$= \frac{42}{2} = 21 \text{ cm}$$

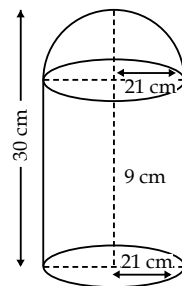
Height of the cylinder, h

$$= 30 - 21 = 9 \text{ cm}$$

\therefore Internal surface area of the vessel = Curved surface area of cylinder + Curved surface area of hemisphere

$$= 2\pi r h + 2\pi r^2 = 2\pi r (h + r)$$

$$= 2 \times \frac{22}{7} \times 21(9 + 21) = 3960 \text{ cm}^2$$



16. We know that, capacity of cylindrical vessel $= \pi r^2 h \text{ cm}^3$
and capacity of hemisphere $= \frac{2}{3} \pi r^3 \text{ cm}^3$

From the figure, capacity of the cylindrical vessel

$$= \pi r^2 h - \frac{2}{3} \pi r^3 = \frac{1}{3} \pi r^2 [3h - 2r]$$

17. Given that, side of a solid cube $(a) = 7 \text{ cm}$

Height of conical cavity $(h) = 7 \text{ cm}$

Radius of conical cavity $(r) = 3 \text{ cm}$

Now, volume of cube

$$= a^3 = (7)^3 = 343 \text{ cm}^3$$

Volume of conical cavity

$$= \frac{1}{3} \pi \times r^2 \times h = \frac{1}{3} \times \frac{22}{7} \times 3 \times 3 \times 7$$

$$= 66 \text{ cm}^3$$

\therefore Volume of remaining solid

= Volume of cube - Volume of conical cavity

$$= 343 - 66 = 277 \text{ cm}^3$$

18. Here, radius of cylindrical portion $(r) =$ Radius of conical portion $(r) = \frac{105}{2} \text{ m}$

Height of cylindrical portion $(h) = 3 \text{ m}$

Slant height of conical portion $(l) = 53 \text{ m}$

Total canvas used in making the tent

= Curved surface area of cylindrical portion + Curved surface area of conical portion

$$= 2\pi rh + \pi rl = 2 \times \frac{22}{7} \times \frac{105}{2} \times 3 + \frac{22}{7} \times \frac{105}{2} \times 53$$

$$= 990 + 8745 = 9735 \text{ m}^2$$

19. Total curved surface

area of hollow cylinder

$$= 2\pi RH + 2\pi rH = 1320$$

$$\Rightarrow 2 \times \frac{22}{7} \times 14(8 + r) = 1320$$

$$\Rightarrow 88(8 + r) = 1320$$

$$\Rightarrow 8 + r = \frac{1320}{88} \Rightarrow 8 + r = 15 \Rightarrow r = 7$$

\therefore Internal diameter $= 2r = 14 \text{ cm}$

20. Radius of cone $(r) = 7 \text{ cm} =$ Radius of hemisphere

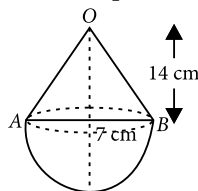
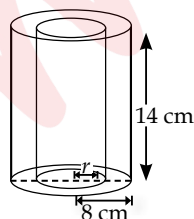
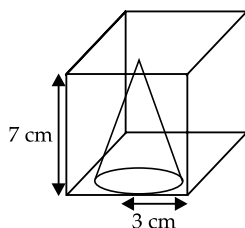
Height of cone $(h) = 14 \text{ cm}$

\therefore Volume of solid

= Volume of cone + volume

of hemisphere

$$= \frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3 = \frac{\pi r^2}{3} [h + 2r]$$



$$= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times [14 + (2 \times 7)]$$

$$= \frac{22}{3} \times 7 \times 28 = \frac{4312}{3} = 1437.33 \text{ cm}^3$$

21. Diameter of hemisphere = Edge of cube = 7 cm

Radius of hemisphere

$$(r) = \frac{7}{2} \text{ cm}$$

Required surface area =

surface area of cube - area of

top of hemisphere + curved

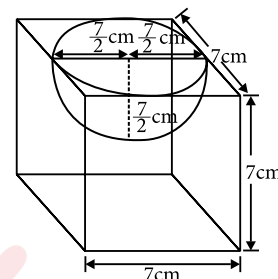
surface area of hemisphere

$$= 6a^2 - \pi r^2 + 2\pi r^2 = 6a^2 + \pi r^2$$

$$= 6(7)^2 + \pi \left(\frac{7}{2}\right)^2$$

$$= 6 \times 49 + \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$$

$$= 294 + 38.5 = 332.5 \text{ cm}^2$$



22. Given, ice-cream cone is the combination of a hemisphere and a cone.

Also, radius of hemisphere, $r = 5 \text{ cm}$

\therefore Volume of hemisphere $= \frac{2}{3} \pi r^3$

$$= \frac{2}{3} \times \frac{22}{7} \times (5)^3 = \frac{5500}{21} = 261.90 \text{ cm}^3$$

Now, radius of the cone = 5 cm

and height of the cone, h

= height of ice-cream cone - radius of hemisphere

$$= 10 - 5 = 5 \text{ cm}$$

\therefore Volume of the cone $= \frac{1}{3} \pi r^2 h$

$$= \frac{1}{3} \times \frac{22}{7} \times (5)^2 \times 5 = \frac{2750}{21} = 130.95 \text{ cm}^3$$

Now, total volume of ice-cream cone =

volume of hemisphere + volume of cone

$$= 261.90 + 130.95 = 392.85 \text{ cm}^3$$

Since, $\frac{1}{6}$ part is left unfilled with ice-cream.

\therefore Required volume of ice-cream

$$= 392.85 - 392.85 \times \frac{1}{6} = 392.85 - 65.475 = 327.4 \text{ cm}^3$$

