CHAPTER **5**



Arithmetic Progressions

SOLUTIONS

1. (c): Since,
$$\frac{1}{x+2}$$
, $\frac{1}{x+3}$, $\frac{1}{x+5}$ are in A.P.

$$\therefore \frac{1}{x+3} - \frac{1}{x+2} = \frac{1}{x+5} - \frac{1}{x+3}$$

$$\Rightarrow \frac{x+2-x-3}{(x+3)(x+2)} = \frac{x+3-x-5}{(x+5)(x+3)}$$

$$\Rightarrow \frac{-1}{(x+3)(x+2)} = \frac{-2}{(x+5)(x+3)} \Rightarrow \frac{-1}{x+2} = \frac{-2}{x+5}$$

$$\Rightarrow$$
 $-x-5=-2x-4$ \Rightarrow $-x+2x=-4+5$ \Rightarrow $x=1$

2. (d): Given A.P. is
$$5, \frac{19}{4}, \frac{9}{2}, \frac{17}{4}, \dots$$

Here,
$$a = 5$$
, $d = \frac{19}{4} - 5 = -\frac{1}{4}$

$$\therefore$$
 10th term, $a_{10} = a + (10 - 1)d$

$$=5+9\left(-\frac{1}{4}\right)=\frac{20-9}{4}=\frac{11}{4}$$

3. (d): Since, alternate terms of an A.P. also forms an A.P.

So,
$$(x - y) - (x + y) = (2x + 3y) - (x - y)$$

$$\Rightarrow -2y = x + 4y \Rightarrow -2y - 4y = x \Rightarrow x = -6y$$

4. (c): Given A.P. is 25, 50, 75, 100,

Here, a = 25, d = 25 and $a_k = 1000$

Now, $a_k = 1000$

$$\Rightarrow$$
 $a + (k-1)d = 1000 \Rightarrow 25 + (k-1)25 = 1000$

$$\Rightarrow$$
 25 + 25k - 25 = 1000 \Rightarrow 25k = 1000 \Rightarrow k = 40

5. (d) : Let *d* be the same common difference of two A.P.s.

Given, first term of 1^{st} A.P., a = 8

First term of 2nd A.P., $a_1 = 3$

Now, 30^{th} term of 1^{st} A.P. = a + 29d = 8 + 29d

Also, 30^{th} term of 2^{nd} A.P. = $a_1 + 29d = 3 + 29d$

:. Required difference = (8 + 29d) - (3 + 29d) = 5

6. Given, A.P. is $\sqrt{27}$, $\sqrt{48}$, $\sqrt{75}$,...

i.e., A.P. is $3\sqrt{3}$, $4\sqrt{3}$, $5\sqrt{3}$,...

Clearly, first term, $a = 3\sqrt{3}$

Second term, $a + d = 4\sqrt{3}$

$$\therefore$$
 Common difference, $d = 4\sqrt{3} - 3\sqrt{3} = \sqrt{3}$

7. Since, $\frac{7}{8}$, a, 3 are three consecutive terms of an A.P.

So,
$$a - \frac{7}{8} = 3 - a \implies 2a = 3 + \frac{7}{8}$$

$$\Rightarrow$$
 $2a = \frac{24+7}{8} = \frac{31}{8} \Rightarrow a = \frac{31}{16}$

8. Given, common difference, d = -6

Let *a* be the first term of the A.P.

Given, $a_9 = 5$

$$\Rightarrow$$
 $a + (9 - 1) \times (-6) = 5 \Rightarrow a - 48 = 5 \Rightarrow a = 53$

Hence, first term of A.P. is 53.

9. Given, common difference, d = 3 be the first term of the A.P.

Now,
$$a_{15} - a_9 = [a + (15 - 1)d] - [a + (9 - 1)d]$$

= 14d - 8d = 6d = 6 \times 3 = 18

10. Let d be the common difference of the A.P.

Given, first term = a and nth term, a_n = b

$$\Rightarrow a + (n-1)d = b \Rightarrow (n-1)d = b - a \Rightarrow d = \frac{b-a}{n-1}$$

11.
$$\frac{1}{yz}$$
, $\frac{1}{zx}$ and $\frac{1}{xy}$ are in A.P.

$$\Rightarrow \frac{1}{zx} - \frac{1}{yz} = \frac{1}{xy} - \frac{1}{zx} \Rightarrow \frac{y - x}{xyz} = \frac{z - y}{xyz}$$

$$\Rightarrow y-x=z-y \Rightarrow y=\frac{x+z}{2}$$

 \therefore x, y and z are in A.P.

12. Given that, a = 4 and $d = \frac{4}{3}$

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$S_{22} = \left(\frac{22}{2}\right)\left[(2)(4) + (22 - 1)\left(\frac{4}{3}\right)\right] = (11)(8 + 28) = 396$$

13. Given, $a_n = 2n + 5$

$$a_1 = 2(1) + 5 = 7, a_2 = 2(2) + 5 = 9,$$

$$a_3 = 2(3) + 5 = 11, a_4 = 2(4) + 5 = 13$$

$$S_4 = a_1 + a_2 + a_3 + a_4 = 7 + 9 + 11 + 13 = 40$$

14. Let a and d are respectively the first term and common difference of the given A.P.

Given,
$$a_4 = a + 3d = 11$$
 ...(i)

Also,
$$a_5 + a_7 = 34$$
 [Given]

$$\Rightarrow$$
 $[a + 4d] + [a + 6d] = 34$

$$\Rightarrow$$
 2a + 10d = 34 \Rightarrow 2(11 - 3d) + 10d = 34 [Using (i)]

$$\Rightarrow$$
 22 - 6d + 10d = 34 \Rightarrow 4d = 12 \Rightarrow d = 3

15. The first 10 multiples of 3 are 3, 6, 9, 12, 15, 18, 21, 24, 27, 30

It is an A.P. with first term, a = 3 and common difference, d = 3

 \therefore Sum of first 10 multiplies of 3 = S_{10}

$$= \frac{10}{2} \{2 \times 3 + (10 - 1) \times 3\}$$

$$\left[\because S_n = \frac{n}{2} \{2a + (n - 1)d\} \right]$$
$$= 5(6 + 27) = 5 \times 33 = 165$$

16. Here A.P. is $\sqrt{6}$, $\sqrt{24}$, $\sqrt{54}$, $\sqrt{96}$,... then

$$a = \sqrt{6}$$
, $d = \sqrt{24} - \sqrt{6} = 2\sqrt{6} - \sqrt{6} = \sqrt{6}$.

$$S_n = \frac{n}{2} [2a + (n-1)d] = \frac{n}{2} [2\sqrt{6} + (n-1)\sqrt{6}]$$
$$= \frac{n}{2} [\sqrt{6} n + \sqrt{6}] = \frac{\sqrt{6}n(n+1)}{2}$$

17. Here the smallest 3-digit number divisible by 7 is 105. So, the number of bacteria taken into consideration is 105, 112, 119,, 994

So, first term (a) = 105, d = 7 and last term = 994

(i) (c):
$$t_5 = a + 4d = 105 + 28 = 133$$

(ii) (b): Let n samples be taken under consideration. \therefore Last term = 994

$$\Rightarrow a + (n-1)d = 994 \Rightarrow 105 + (n-1)7 = 994 \Rightarrow n = 128$$

(iii) (a): Total number of bacteria in first 10 samples

=
$$S_{10} = \frac{10}{2} [2(105) + 9(7)] = 1365$$

(iv) (a): t_7 from end = $(128 - 7 + 1)^{th}$ term from beginning = 122^{th} term = 105 + 121(7) = 952

(v) (c):
$$t_{50} = 105 + 49 \times 7 = 448$$

18. Geeta's A.P. is -5, -2, 1, 4, ...

Here, first term $(a_1) = -5$ and common difference $(d_1) = -2 + 5 = 3$

Similarly, Madhuri's A.P. is 187, 184, 181, ...

Here first term $(a_2) = 187$ and common difference $(d_2) = 184 - 187 = -3$

(i)
$$t_{34} = a_2 + 33d_2 = 187 + 33(-3) = 88$$

(ii) Required sum = 3 + (-3) = 0

(iii)
$$t_{19} = a_1 + 18d_1 = (-5) + 18(3) = 49$$

(iv)
$$S_{10} = \frac{n}{2} [2a_1 + (n-1)d_1] = \frac{10}{2} [2(-5) + 9(3)] = 85$$

(v) Let n^{th} terms of the two A.P.'s be equal.

$$\therefore -5 + (n-1)3 = 187 + (n-1)(-3)$$

$$\Rightarrow$$
 6($n-1$) = 192 \Rightarrow $n=33$

19. Number of pairs of shoes in 1^{st} , 2^{nd} , 3^{rd} row, ... are 3, 5, 7, ...

So, it forms an A.P. with first term a = 3, d = 5 - 3 = 2

(i) (d): Let *n* be the number of rows required.

$$\therefore S_n = 120$$

$$\Rightarrow \frac{n}{2}[2(3)+(n-1)2]=120$$

$$\Rightarrow n^2 + 2n - 120 = 0 \Rightarrow n^2 + 12n - 10n - 120 = 0$$

$$\Rightarrow$$
 $(n+12)(n-10)=0 \Rightarrow n=10$

So, 10 rows required to put 120 pairs.

(ii) (b): No. of pairs in 17^{th} row = t_{17} = 3 + 16(2) = 35 No. of pairs in 10^{th} row = t_{10} = 3 + 9(2) = 21

$$\therefore$$
 Required difference = 35 – 21 = 14

(iii) (c) : Here
$$n = 15$$

$$\therefore t_{15} = 3 + 14(2) = 3 + 28 = 31$$

(iv) (a): No. of pairs in
$$30^{th}$$
 row = t_{30} = 3 +29(2) = 61

(v) (c): No. of pairs in
$$5^{th}$$
 row = t_5 = 3 + 4(2) = 11
No. of pairs in 8^{th} row = t_8 = 3 + 7(2) = 17

$$\therefore$$
 Required sum = 11 + 17 = 28

20. Here
$$S_n = 0.1n^2 + 7.9n$$

(i)
$$S_{n-1} = 0.1(n-1)^2 + 7.9(n-1)$$

= $0.1n^2 + 7.7n - 7.8$

(ii)
$$S_1 = t_1 = a = 0.1(1)^2 + 7.9(1) = 8 \text{ cm}$$

= Diameter of core

So, radius of the core = 4 cm

(iii)
$$S_2 = 0.1(2)^2 + 7.9(2) = 16.2$$

(iv) Required diameter =
$$t_2 = S_2 - S_1 = 16.2 - 8 = 8.2$$
 cm

(v) As
$$d = t_2 - t_1 = 8.2 - 8 = 0.2$$
 cm

So, thickness of tissue = $0.2 \div 2 = 0.1$ cm = 1 mm

21. Here, first term a = 7

Common difference, d = 13 - 7 = 6

Let the given A.P. contains *n* terms, then

$$a_n = 187$$
 (: Given) $\Rightarrow a + (n-1)d = 187$

$$\Rightarrow$$
 7 + (n - 1)6 = 187 \Rightarrow (n - 1)6 = 180

$$\Rightarrow$$
 $n-1=30 \Rightarrow n=30+1=31$

Thus, the given A.P. contains 31 terms.

Here n = 31 (odd number)

$$\therefore \quad \text{Middle term} = \frac{1}{2}(n+1)^{\text{th}}.$$

$$=\frac{1}{2}(31+1)^{th} = \left(\frac{1}{2} \times 32\right)^{th} = 16^{th}$$

Hence, middle term, a_{16}

$$= a + 15d = 7 + 15 \times 6 = 7 + 90 = 97$$

22. The given A.P. is 27, 23, 19,..., -65.

Here, first term, a = 27, common difference, d = 23 - 27 = -4, last term, l = -65

Now, n^{th} term from the end = l - (n - 1)d

$$\therefore$$
 11th term from the end = -65 -(11 - 1)(-4)

$$= -65 - (10) (-4) = -65 + 40 = -25$$

Hence, the 11th term from the end is -25.

OR

Given, A.P. is 115, 110, 105, ...

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Here, a = 115, d = 110 - 115 = -5

Let n^{th} term of the given A.P. be the first negative term.

i.e.,
$$a_n < 0 \Rightarrow a + (n-1)d < 0$$

$$\Rightarrow$$
 115 + (n - 1)(-5) < 0

$$\Rightarrow$$
 115 - 5n + 5 < 0 \Rightarrow 120 - 5n < 0

$$\Rightarrow$$
 $5n > 120 \Rightarrow n > 24 \Rightarrow n \ge 25$

25th term of the given A.P. will be the first negative term.

23. Let a = 2 be the first term and d be the common difference of the A.P.

Given, 10th term of the A.P. is 47.

$$\therefore a_{10} = 2 + (10 - 1)d \qquad [\because a_n = a + (n - 1)d]$$

$$\Rightarrow 47 = 2 + 9d \Rightarrow 9d = 45 \Rightarrow d = 5$$

$$\Rightarrow$$
 47 = 2 + 9d \Rightarrow 9d = 45 \Rightarrow d = 5

Now,
$$S_{15} = \frac{15}{2} [2a + (15 - 1)d] \left[\because S_n = \frac{n}{2} [2a + (n - 1)d] \right]$$

$$= \frac{15}{2}[2 \times 2 + 14 \times 5] = \frac{15}{2}[4 + 70] = \frac{15}{2} \times 74 = 15 \times 37 = 555$$

Hence, the sum of 15 terms of the given A.P. is 555.

24. Given A.P. is 3, 7, 11, 15,

Here,
$$a = 3$$
, $d = 7 - 3 = 4$

Let sum of n terms is 406.

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$\Rightarrow$$
 406 = $\frac{n}{2}$ [2(3) + (n-1)(4)]

$$\Rightarrow$$
 406 = $n[1 + 2n] \Rightarrow 2n^2 + n - 406 = 0$

$$\Rightarrow$$
 $2n^2 + 29n - 28n - 406 = 0$

$$\Rightarrow$$
 $n(2n + 29) - 14(2n + 29) = 0 \Rightarrow $(n - 14)(2n + 29) = 0$$

$$\Rightarrow$$
 $n = 14$ [Since, n can't be a fraction]

25. Given, $S_n = 2n^2 + 3n$

We know that, $a_n = S_n - S_{n-1}$

$$\therefore a_{16} = S_{16} - S_{15} = [2(16)^2 + 3(16)] - [2(15)^2 + 3(15)]$$
$$= [2(256) + 3(16)] - [2(225) + 3(15)]$$

$$= [512 + 48] - [450 + 45] = 560 - 495 = 65$$

26. Sum of all natural numbers from 1 to 1000 which are not divisible by
$$5 = \text{(Sum of all natural numbers from 1 to 1000, } S_n) - \text{(Sum of all natural numbers from 1 to 1000 which are divisible by 5 , S_n)$$

Now, all the natural numbers from 1 to 1000 are 1, 2, 3, ..., 1000, which is an A.P. where a = 1, l = 1000and n = 1000

$$S_n = \frac{n}{2}[a+l]$$

$$= \frac{1000}{2}[1+1000] = 500 \times 1001 = 500500 \qquad ...(i)$$

Again, all the natural numbers from 1 to 1000 which are divisible by 5 are 5, 10, 15,, 1000, which is also an A.P. where, first term, a = 5, last term, l = 1000 and common difference, d = 5

$$a_n = a + (n-1)d \implies 1000 = 5 + (n-1)5$$

$$\Rightarrow$$
 5n = 1000 \Rightarrow n = 200

$$S'_n = \frac{n}{2}[a+l] = \frac{200}{2}[5+1000] = 100 \times 1005 = 100500$$

3

$$\therefore$$
 Required sum = $S_n - S'_n = 500500 - 100500 = 400000$

27. Given,
$$a = 100$$

Let *d* be the common difference of the A.P.

According to the question,

$$100 + (100 + d) + (100 + 2d) + (100 + 3d) + (100 + 4d) + (100 + 5d) = 5[(100 + 6d) + (100 + 7d) + (100 + 8d) + (100 + 9d) + (100 + 10d) + (100 + 11d)]$$

$$\Rightarrow$$
 600 + 15*d* = 5 (600 + 51*d*)

$$\Rightarrow$$
 120 + 3d = 600 + 51d \Rightarrow -48d = 480 \Rightarrow d = -10

28. Let *a* and *d* be the first term and common difference of the A.P.

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

Consider,
$$S_{10} - S_5 = \frac{10}{2} [2a + 9d] - \frac{5}{2} [2a + 4d]$$

= $5(2a + 9d) - 5(a + 2d)$
= $5[2a + 9d - a - 2d] = 5(a + 7d)$... (i)

Also,
$$S_{15} = \frac{15}{2} [2a + 14d] = 15(a + 7d) = 3[5(a + 7d)]$$

= 3 $(S_{10} - S_5)$ (From (i))

OR

Let *a* be the first term and *d* be the common difference of given A.P. Then

$$(p+q)^{\text{th}}$$
 term, $a_{p+q} = a + (p+q-1)d$...(i)

and
$$(p-q)^{\text{th}}$$
 term, $a_{p-q} = a + (p-q-1)d$...(ii)

.. Sum of
$$(p+q)^{th}$$
 and $(p-q)^{th}$ terms = $a_{p+q} + a_{p-q}$
= $[a + (p+q-1)d] + [a + (p-q-1)d]$ [Using (i) and (ii)]

=
$$2a + (p + q - 1 + p - q - 1)d$$

= $2a + (2p - 2)d = 2 \times [a + (p - 1)d] = 2 \times p^{th}$ term of the A.P.

Here, first term, a = 8 and common difference (d) = 10 - 8 = 2If the given A.P. has a total 60 terms, then

$$a_{60} = a + 59d$$
 [:: $a_n = a + (n-1)d$]
= 8 + 59 × 2 = 8 + 118 = 126

Sum of the last 10 terms of the given A.P.

$$= a_{51} + a_{52} + ... + a_{60} = (a + 50d) + (a + 51d) + ... + 126$$

$$= (8 + 100) + (8 + 102) + ... + 126 = 108 + 110 + ... + 126$$

$$= \frac{10}{2}[108 + 126] \qquad \left[\because \quad S_n = \frac{n}{2} (\text{First term + Last term}) \right]$$

$$= 5 \times 234 = 1170$$

30. Let the four parts be (a - 3d), (a - d), (a + d), (a + 3d). Sum of the numbers = 56

$$\Rightarrow$$
 $(a-3d) + (a-d) + (a+d) + (a+3d) = 56$

$$\Rightarrow$$
 4a = 56 \Rightarrow a = 14

Also,
$$\frac{(a-3d)(a+3d)}{(a-d)(a+d)} = \frac{5}{6}$$
 [Given] $\Rightarrow \frac{a^2-9d^2}{a^2-d^2} = \frac{5}{6}$

$$\Rightarrow$$
 6(196 - 9 d^2) = 5(196 - d^2) [: $a = 14$]

⇒
$$6 \times 196 - 54d^2 = 5 \times 196 - 5d^2$$

⇒ $49d^2 = 6 \times 196 - 5 \times 196 \Rightarrow 49d^2 = 196$
⇒ $d^2 = 4 \Rightarrow d = \pm 2$
∴ Required four parts are $(14 - 3 \times 2), (14 - 2), (14 + 2), (14 + 3 \times 2)$

or
$$[(14-3(-2)), (14+2), (14+2), [(14+3(-2)].$$

31. The given sequence is 12000, 16000, 20000,, which is an A.P.

Here first term, a = 12000, common difference, d = 4000, $S_n = 1000000$

Let the man saves ₹ 1000000 in n years.

Now,
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 1000000 = \frac{n}{2} [2 \times 12000 + (n-1)4000]$$

$$\Rightarrow 1000 = \frac{n}{2} [24 + 4n - 4] \Rightarrow 1000 = \frac{n}{2} \times 4(n+5)$$

$$\Rightarrow 500 = n^2 + 5n \Rightarrow n^2 + 5n - 500 = 0$$

\Rightarrow n^2 + 25n - 20n - 500 = 0 \Rightarrow (n + 25)(n - 20) = 0

$$\Rightarrow$$
 $n = 20$ (as n can't be negative)

∴ Man saves ₹ 1000000 in 20 years.

OR

Total amount of ten prizes = ₹1600 Let the value of first prize be ₹ x According to the question, prizes are x, x – 20, x – 40 ... to 9 terms Here, a = x, d = –20 and d = 10

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 1600 = \frac{10}{2} [2x + (10-1)(-20)] = 10(x-90)$$

$$\Rightarrow 160 = x - 90 \Rightarrow x = 160 + 90 = 250$$

Hence, amount of each prize (in ₹) are 250, 230, 210, ..., 70.

32. Let *a* and *d* are respectively the first term and common difference of an A.P.:, a, a + d, a + 2d,...

Given, 14th term of an A.P. is twice its 8th term.

$$\begin{array}{l} \therefore \quad a_{14} = 2a_8 \Rightarrow \ a + (14-1)d = 2[a+(8-1)d] \\ \Rightarrow \quad a + 13d = 2a + 14d \Rightarrow 2a - a = (13-14)d \\ \Rightarrow \quad a = -d \\ \text{Also, } a_6 = -8 \\ \Rightarrow \quad a + (6-1)d = -8 \Rightarrow -d + 5d = -8 \\ \Rightarrow \quad 4d = -8 \Rightarrow d = -2 \\ \text{From (i), } a = -(-2) = 2 \\ \end{array}$$

Therefore, the A.P. is 2, 2 + (-2), 2 + 2(-2), 2 + 3(-2),...i.e., 2, 0, -2, -4,...

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{20} = \frac{20}{2} [2 \times 2 + (20 - 1)(-2)]$$

$$= 10[4 - 38] = 10(-34) = -340$$

33. Here, 8 and 20 are the first term and common difference respectively of an A.P.

$$S_n = \frac{n}{2} [2(8) + (n-1)20] = 8n + 10n^2 - 10n$$
$$= 10n^2 - 2n \qquad ...(i)$$

Also, -30 and 8 are the first term and common difference respectively of another A.P.

$$S_{2n} = \frac{2n}{2} [2(-30) + (2n-1)8]$$

$$= -60n + 16n^2 - 8n = 16n^2 - 68n \qquad ...(ii)$$

According to the question, $S_n = S_{2n}$

$$\Rightarrow$$
 16n² - 68n = 10n² - 2n [From (i) and (ii)]

$$\Rightarrow$$
 $16n^2 - 10n^2 - 68n + 2n = 0$

$$\Rightarrow$$
 $6n^2 - 66n = 0 \Rightarrow 6n(n - 11) = 0$

$$\Rightarrow$$
 Either $n - 11 = 0$ or $n = 0 \Rightarrow n = 11$ or $n = 0$

$$\therefore$$
 $n = 0$ is not possible.

Hence, value of n is 11.

OR

Consider the sequence, 2, 5, 8, 11,, x, which is an A.P. Here, a = 2, d = 3, $a_n = x$

Here,
$$a = 2$$
, $a = 3$, $a_n = x$

$$\therefore a_n = a + (n-1)d \Rightarrow x = 2 + (n-1)3$$

$$\Rightarrow x = 2 + 3n - 3 \Rightarrow x + 1 = 3n \Rightarrow n = \frac{x+1}{3}$$

$$\therefore S_n = \frac{n}{2}[a+l] \Rightarrow 345 = \frac{x+1}{3 \times 2}[2+x][\text{Given}, S_n = 345]$$

$$\Rightarrow (x+1)(x+2) = 2070 \Rightarrow x^2 + 3x - 2068 = 0$$

$$\Rightarrow x = \frac{-3 \pm \sqrt{9 + 8272}}{2} = \frac{-3 \pm \sqrt{8281}}{2} = \frac{-3 \pm 91}{2} = 44,-47$$

Since, the given A.P. is an increasing A.P. with a = 2 and d = 3, so x can't be negative.

$$\therefore$$
 $x = 44$

34. Let a = 8 years be the first term of the A.P.

i.e., age of the youngest boy participating in a painting competition.

Common difference, d *i.e.*, age difference of the participants = 4 months (given)

$$= \frac{4}{12} \text{ year} = \frac{1}{3} \text{ year}$$

Let n be the total number of participants in the painting competition and S_n denotes the sum of ages of all the participants. Then, S_n = 168 years (given)

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 168 = \frac{n}{2} \left[2 \times 8 + (n-1) \left(\frac{1}{3} \right) \right]$$

$$\Rightarrow 336 = n \left[16 + (n-1) \left(\frac{1}{3} \right) \right]$$

$$\Rightarrow 336 \times 3 = n [48 + (n-1)] \Rightarrow 1008 = 48n + n(n-1)$$

$$\Rightarrow 1008 = 48n + n^2 - n \Rightarrow n^2 + 47n - 1008 = 0$$

$$\Rightarrow n^2 + 63n - 16n - 1008 = 0 \Rightarrow n(n+63) - 16(n+63) = 0$$

$$\Rightarrow (n-16) (n+63) = 0$$

$$\Rightarrow \text{Either } n - 16 = 0 \text{ or } n+63 = 0$$

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- \Rightarrow Either n = 16 or n = -63
- \Rightarrow n = 16, rejecting n = -63 as n can't be negative.
- \therefore Age of eldest participant is a_{16} .

Now,
$$a_{16} = 8 + (16 - 1) \times \frac{1}{3}$$
 [: $a_n = a + (n - 1)d$]
= $8 + \frac{15}{3} = 8 + 5 = 13$ years

Hence, the total number of participants are 16 and the age of the eldest participant is 13 years.

35. Original cost of house = ₹2200000

Amount paid in cash = ₹400000

Balance to be paid = ₹(2200000 – 400000) = ₹1800000 Amount paid in each installment = ₹100000

.. Number of installments = 18

Interest paid with 1st installment =
$$1800000 \times \frac{10}{100}$$

= ₹ 180000

Interest paid with 2nd installment =
$$1700000 \times \frac{10}{100}$$

= ₹ 170000

and so on

Interest paid with last installment =
$$100000 \times \frac{10}{100}$$

= ₹ 10000

Total interest paid = (180000 + 170000 + + 10000), which is an A.P. with first term, a = 180000,

last term, l = 10000.

$$= \frac{18}{2} [180000 + 10000] \qquad \left[\because S_n = \frac{n}{2} (a+l) \right]$$

- = 9[190000] = ₹ 1710000
- : Total cost of house for Ronit

OR

Since, the A.P. consists of 37 terms, so 19th term is the middle term.

Let $a_{19} = a$ and d be the common difference of the A.P. The A.P. is ; a - 18d, a - 17d,..., a - d, a, a + d,..., a + 17d, a + 18d

Sum of the three middle most terms = 225

$$\Rightarrow (a-d) + a + (a+d) = 225$$

$$\Rightarrow 3a = 225 \Rightarrow a = 75 \qquad \dots(i)$$

Sum of the three last terms = 429

$$\Rightarrow$$
 $(a + 18d) + (a + 17d) + (a + 16d) = 429$

$$\Rightarrow$$
 3a + 51d = 429 \Rightarrow a + 17d = 143

$$\Rightarrow$$
 17d = 143 - a = 143 - 75 (Using (i))

$$\Rightarrow 17d = 68 \Rightarrow d = \frac{68}{17} = 4$$

Now, first term = $a - 18d = 75 - 18 \times 4 = 3$

:. The A.P. is 3, 7, 11, ..., 147.

MtG BEST SELLING BOOKS FOR CLASS 10







































