Linear Inequalities

SOLUTIONS

EXERCISE - 6.1

1. Given inequality is 24x < 100 Dividing both sides by 24, we get

NCERT FOCUS

$$x < \frac{100}{24} = \frac{25}{6}$$

- (i) x is a natural number, then the set {1, 2, 3, 4} satisfies this inequality.
- (ii) *x* is an integer, then the set $\{..., -4, -3, -2, -1, 0, 1, 2, 3, 4\}$ satisfies this inequality.
- 2. Given inequality is -12x > 30Dividing both sides by -12, we get $30 \quad 5$
- $x < -\frac{30}{12} = -\frac{5}{2}$

(i) This inequality is not true for any natural number.

- (ii) Set of integers that satisfy this inequality is $\{..., -5, -4, -3\}$.
- **3.** Given inequality is 5x 3 < 7

Transposing 3 to R.H.S., we get 5x < 7 + 3 or 5x < 10Dividing both sides by 5, we get x < 2

(i) When x is an integer, $\{\dots, -2, -1, 0, 1\}$ satisfies this inequality.

- (ii) When *x* is real number, the solution set is $(-\infty, 2)$.
- **4.** Given inequality is 3x + 8 > 2
- Transposing 8 to R.H.S., we get $3x \ge 2 8 \Rightarrow 3x \ge -6$ Dividing both sides by 3, we get $x \ge -2$ (i) When *x* is an integer, the solution is $\{-1, 0, 1, 2, 3, ...\}$
- (ii) When *x* is a real number, the solution is $(-2, \infty)$.
- 5. The inequality is 4x + 3 < 5x + 7Transposing 5x to L.H.S. and 3 to R.H.S., we get
- 4x 5x < 7 3 or -x < 4
- Dividing both sides by -1, we get x > -4
- \therefore The solution set is (- 4, ∞).
- 6. The inequality is 3x 7 > 5x 1

Transposing 5x to L.H.S. and -7 to R.H.S., we get 3x - 5x > -1 + 7 or -2x > 6

- Dividing both sides by -2, we get x < -3
- \therefore The solution set is $(-\infty, -3)$.

7. The inequality is $3(x - 1) \le 2(x - 3)$ or $3x - 3 \le 2x - 6$ Transposing 2x to L.H.S. and -3 to R.H.S., we get $3x - 2x \le -6 + 3 \implies x \le -3$ \therefore The solution set is $(-\infty, -3]$. 8. The inequality is $3(2 - x) \ge 2(1 - x)$ or $6 - 3x \ge 2 - 2x$

Transposing -2x to L.H.S. and 6 to R.H.S., we get

 $-3x + 2x \ge 2 - 6$ or $-x \ge -4$

Multiplying both sides by –1, we get, $x \le 4$

- \therefore The solution set is $(-\infty, 4]$.
- 9. The inequality is $x + \frac{x}{2} + \frac{x}{3} < 11$ Simplifying, $\frac{6x + 3x + 2x}{6} < 11$ or $\frac{11x}{6} < 11$ Multiplying both sides by $\frac{6}{11}$, we get x < 6
- \therefore The solution set is (- ∞ , 6).
- **10.** The inequality is $\frac{x}{3} > \frac{x}{2} + 1$

Transposing $\frac{x}{2}$ to L.H.S., we get

$$\frac{x}{3} - \frac{x}{2} > 1$$

Simplifying, $\frac{2x-3x}{6} > 1$ or $-\frac{x}{6} > 1$

Multiplying both sides by -6, we get x < -6 \therefore The solution set is $(-\infty, -6)$.

11. The inequality is $\frac{3(x-2)}{5} \le \frac{5(2-x)}{3}$

Multiply both sides by the L.C.M. of 5, 3 *i.e.*, by 15. $3 \times 3(x - 2) \le 5 \times 5(2 - x)$ or $9(x - 2) \le 25(2 - x)$ Simplifying, $9x - 18 \le 50 - 25x$ Transposing -25x to L.H.S. and -18 to R.H.S., we get $9x + 25x \le 50 + 18$ or $34x \le 68$ Dividing both sides by 34, we get, $x \le 2$

- \therefore Solution set is $(-\infty, 2]$.
- 12. The inequality is $\frac{1}{2}\left(\frac{3x}{5}+4\right) \ge \frac{1}{3}(x-6)$

or,
$$\frac{1}{2}\left(\frac{3x+20}{5}\right) \ge \frac{1}{3}(x-6)$$

Multiplying both sides by 30, we get $3(3x + 20) \ge 10(x - 6)$ or, $9x + 60 \ge 10x - 60$ Transposing 10x to L.H.S. and 60 to R.H.S., we get $9x - 10x \ge -60 - 60$ or $-x \ge -120$ Multiplying both sides by -1, we get, $x \le 120$ \therefore The solution set is $(-\infty, 120]$. **13.** The inequality is 2(2x + 3) - 10 < 6(x - 2)Simplifying, 4x + 6 - 10 < 6x - 12 or 4x - 4 < 6x - 12Transposing 6x to L.H.S. and -4 to R.H.S., we get 4x - 6x < -12 + 4 or -2x < -8Dividing both sides by -2, we get, x > 4 \therefore The solution set is $(4, \infty)$. **14.** The inequality is $37 - (3x + 5) \ge 9x - 8(x - 3)$

Simplifying, $37 - 3x - 5 \ge 9x - 8x + 24$ or $32 - 3x \ge x + 24$

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Transposing x to L.H.S. and 32 to R.H.S., we get $-3x - x \ge 24 - 32$ or $-4x \ge -8$ Dividing both sides by – 4, we get, $x \le 2$ \therefore The solution set is $(-\infty, 2]$. **15.** The inequality is $\frac{x}{4} < \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$ Multiplying each term by the L.C.M. of 4, 3, 5, i.e., by 60, we get 15x < 100x - 40 - 84x + 36 or 15x < 100x - 84x - 40 + 36or 15x < 16x - 4Transposing 16x to L.H.S., we get $15x - 16x \le -4$ or $-x \le -4$ Multiplying both sides by -1, we get, x > 4The solution set is $(4, \infty)$. *.*... **16.** The inequality is $\frac{(2x-1)}{3} \ge \frac{(3x-2)}{4} - \frac{(2-x)}{5}$ Multiplying each term by L.C.M. of 3, 4, 5, i.e., by 60 $\frac{(2x-1)}{3} \times 60 \ge \frac{(3x-2)}{4} \times 60 - \frac{(2-x)}{5} \times 60$ $20(2x - 1) \ge (3x - 2) \times 15 - (2 - x) \times 12$ or $40x - 20 \ge 45x - 30 - 24 + 12x$ or $40x - 20 \ge 57x - 54$ or Transposing 57x to L.H.S. and -20 to R.H.S., we get $40x - 57x \ge -54 + 20$ or $-17x \ge -34$ Dividing both sides by –17, we get, $x \le 2$ \therefore The solution set is $(-\infty, 2]$. **17.** The inequality is 3x - 2 < 2x + 1Transposing 2x to L.H.S. and -2 to R.H.S., we get 3x - 2x < 1 + 2 or x < 3____ The solution set is $(-\infty, 3)$. *.*... **18.** The inequality is $5x - 3 \ge 3x - 5$ Transposing 3x to L.H.S. and -3 to R.H.S., we get $5x - 3x \ge -5 + 3$ or $2x \ge -2$ Dividing both sides by 2, we get $x \ge -1$ \therefore The solution set is $[-1, \infty)$. **19.** The inequality is 3(1 - x) < 2(x + 4)Simplifying, 3 - 3x < 2x + 8Transposing 2x to L.H.S. and 3 to R.H.S., we get -3x - 2x < 8 - 3 or -5x < 5-∞ <u>-</u>1 0 Dividing both sides by -5, we get x > -1 \therefore The solution set is $(-1, \infty)$. **20.** The inequality is $\frac{x}{2} \ge \frac{(5x-2)}{3} - \frac{(7x-3)}{5}$ Multiply each term by L.C.M. of 2, 3, 5, i.e., by 30 $\frac{x}{2} \times 30 \ge \frac{(5x-2)}{3} \times 30 - \frac{(7x-3)}{5} \times 30$ or $15x \ge 10(5x - 2) - 6(7x - 3)$ or $15x \ge 50x - 20 - 42x + 18$ or $15x - 8x \ge -2$ or $7x \ge -2$

Dividing both sides by 7, we get

$$x \ge -\frac{2}{7} \xrightarrow[-\infty]{} (-\frac{2}{7})$$

$$\therefore \text{ The solution set is } \left[-\frac{2}{7}, \infty\right]$$

21. Let Ravi gets *x* marks in third unit test.

$$\therefore$$
 Average marks obtained by Ravi = $\frac{70+75+x}{3}$

$$\therefore \quad \frac{70+75+x}{3} \ge 60 \text{ or } \frac{145+x}{3} \ge 60$$

Multiplying both sides by 3, we get $145 + x \ge 180$

Transposing 145 to R.H.S., we get

 $x \ge 180 - 145 \implies x \ge 35$

- ... Ravi should get atleast 35 marks in the third unit test.
- 22. Let Sunita obtained *x* marks in the fifth examination.∴ Average marks of 5 examinations

$$=\frac{87+92+94+95+x}{5}=\frac{368+x}{5}$$

This average must be atleast 90.



Multiplying both sides by 5, we get $368 + x \ge 450$

Transposing 368 to R.H.S., we get $x \ge 450 - 368 \Rightarrow x \ge 82$ \therefore Sunita should obtain atleast 82 marks in the fifth examination.

23. Let *x* be the smaller of the two odd positive integers. Then the other integer is x + 2. We should have x + 2 < 10 and x + (x + 2) > 11 or,

or
$$x < 8$$
 and $x > \frac{9}{2}$

Hence, if one number is 5 (odd number), then the other is 7. If the smaller number is 7, then the other is 9. Hence, possible pairs are (5, 7) and (7, 9).

24. Let *x* be the smaller of the two positive even integers then the other one is x + 2. We should have x > 5 and x + x + 2 < 23 or 2x + 2 < 23

or
$$2x < 21$$
 or $x < \frac{21}{2}$

Thus, the value of x may be 6, 8, 10 (even integers). Hence, the pairs are (6, 8), (8, 10), (10, 12).

25. Let the shortest side measures *x* cm.

The longest side will be 3x cm.

Third side will be (3x - 2) cm.

According to the problem,

 $x + 3x + 3x - 2 \ge 61$

or $7x - 2 \ge 61$ or $7x \ge 63$ or $x \ge 9$

Hence, the minimum length of the shortest side is 9 cm.

26. Let *x* be the length of the shortest piece of board, then x + 3 is the length of second piece and 2x is the length of third piece.

Thus, $x + (x + 3) + 2x \le 91$ or $4x + 3 \le 91$ or $4x \le 88$ or $x \le 22$ According to the problem, $2x \ge (x+3) + 5$ or $x \ge 8$

: Atleast 8 cm but not more than 22 cm are the possible lengths for the shortest board.

NCERT MISCELLANEOUS EXERCISE

We have, $2 \le 3x - 4 \le 5$ 1. Adding 4, we get $2 + 4 \le 3x - 4 + 4 \le 5 + 4$ or, $6 \le 3x \le 9$ Dividing each side by 3, we have, $2 \le x \le 3$. Thus, the solution is [2, 3].

- 2. We have, $6 \le -3(2x 4) \le 12$ $\Rightarrow \frac{6}{3} \le -(2x-4) < \frac{12}{3}$ (Dividing each side by 3) $\Rightarrow 2 \leq -(2x-4) \leq 4 \Rightarrow 2 \leq -2x+4 \leq 4$ \Rightarrow 2 - 4 \leq -2x + 4 - 4 \leq 4 - 4 (Subtracting 4)
- $\Rightarrow -2 \leq -2x < 0$ $\Rightarrow \frac{-2}{2} \ge \frac{-2x}{2} > 0$
- (Dividing each side by -2) $\Rightarrow 1 > r > 0$

Hence, x is less than or equal to 1 and greater than 0 *i.e.*, $x \in (0, 1]$.

3. We have, $-3 \le 4 - \frac{7x}{2} \le 18$

Subtracting 4, we get

 $-3-4 \le 4 - \frac{7x}{2} - 4 \le 18 - 4$ or $-7 \le \frac{-7x}{2} \le 14$ Multiplying each side by $-\frac{2}{7}$, we get

$$-7 \times \left(-\frac{2}{7}\right) \ge \frac{-7}{2} x \times \left(-\frac{2}{7}\right) \ge 14 \times \left(-\frac{2}{7}\right)$$
$$\Rightarrow 2 \ge x \ge -4 \text{ or } -4 \le x \le 2$$

 \therefore *x* is less than or equal to 2 and greater than or equal to -4 *i.e.*, $x \in [-4, 2]$

4. We have, $-15 < 3\frac{(x-2)}{5} \le 0$ $-15 \times 5 < \frac{3(x-2)}{5} \times 5 \le 0 \times 5$ [Multiplying by 5] $\Rightarrow -75 < 3(x-2) \le 0$ $\Rightarrow \frac{-75}{3} < x - 2 \le \frac{0}{3}$ [Dividing each side by 3] \Rightarrow -25 < x - 2 ≤ 0 or -25 + 2 < x - 2 + 2 ≤ 0 + 2 [Adding 2] \Rightarrow -23 < $x \le 2$

Hence, *x* is less than or equal to 2 and greater than -23, *i.e.*, $x \in (-23, 2]$.

 $-12 < 4 - \frac{3x}{-5} \le 2$ 5.

Subtracting 4 from each side, we get

$$-12 - 4 < 4 - \frac{3x}{-5} - 4 \le 2 - 4$$

$$\Rightarrow -16 < \frac{3x}{5} \le -2$$

Multiplying each side by 5/3, we get

$$-16 \times \frac{5}{3} < \frac{3}{5}x \times \frac{5}{3} \le -2 \times \frac{5}{3}$$

$$\Rightarrow -\frac{80}{3} < x \le -\frac{10}{3} \text{ or } x \in \left(-\frac{-80}{3}, -\frac{-10}{3}\right).$$

6. We have, $7 \le \frac{3x+11}{2} \le 11$
Multiplying each side by 2, we get
 $7 \times 2 \le \left(\frac{3x+11}{2}\right) \times 2 \le 11 \times 2 \text{ or } 14 \le 3x + 11 \le 22$
Subtracting 11, we get
 $14 - 11 \le 3x + 11 - 11 \le 22 - 11$
or $3 \le 3x \le 11$
Dividing by 3, we get
 $1 \le x \le \frac{11}{3}$
i.e., x is greater than or equal to 1 and less than or equal
to $\frac{11}{3}$ *i.e.*, $x \in \left[1, \frac{11}{3}\right].$
7. (i) $5x + 1 > -24 \Rightarrow 5x > -24 - 1$ or $5x > -25$
Dividing by 5, we get $x > -5$
 $\longrightarrow -5 - 4 - 3 - 2 - 1 = 0 = 1$
(ii) $5x - 1 < 24$
Adding 1, we get $5x < 25$
Dividing by 5, we get $x < 5$
 $\longrightarrow -5 - 4 - 3 - 2 - 1 = 0 = 1 = 2 = 3 = 4 = 5$
From (i) and (ii), we get
 $-5 < x < 5 \text{ or } x \in (-5, 5)$
 $\longrightarrow -5 - 4 - 3 - 2 - 1 = 0 = 1 = 2 = 3 = 4 = 5 = 5$
(i) $2(x - 1) < x + 5 \text{ or } 2x - 2 < x + 5 = 3 = 2x - x < 5 + 2 \Rightarrow x < 7$
 $\longrightarrow -1 = 0 = 1 = 2 = 3 = 4 = 5 = 7 = 5$
(ii) $3(x + 2) > 2 - x \text{ or } 3x + 6 > 2 - x = 3 = 3x + x > 2 - 6 = 3 = 4x > -4 \Rightarrow x > -1$
 $\longrightarrow -1 = 0 = 1 = 2 = 3 = 5 = 5$

From (i) and (ii), we get $-1 \le x \le 7$ i.e., $x \in (-1, 7)$ 9. (i) 3x - 7 > 2(x - 6) or 3x - 7 > 2x - 12

 $-\infty$ \bigcirc -5 -4 -3 -2 -1 0 1 2 3 4 5

 $\Rightarrow 3x - 2x > -12 + 7$

(ii) 6 - x > 11 - 2x $\Rightarrow -x + 2x > 11 - 6$

 $\Rightarrow x > -5$

$$\Rightarrow x > 5$$

$$\xrightarrow{-\infty} \underbrace{ \circ}_{5 \ 6 \ 7 \ 8 \ 9 \ 10} \xrightarrow{\infty} \infty$$

From (i) and (ii), we get x > 5 satisfies both the inequalities x > -5 and x > 5. Solution set is $(5, \infty)$ *.*... $-\infty \longleftrightarrow 1 2 3 4 5 6$ **10.** (i) $5(2x - 7) - 3(2x + 3) \le 0$ \Rightarrow 10x - 35 - 6x - 9 \leq 0 $\Rightarrow 4x - 44 \le 0$ $4x \le 44 \implies x \le 11$ \Rightarrow 0 2 4 6 8 10 12 (ii) $2x + 19 \le 6x + 47$ \Rightarrow 2x - 6x \leq 47 - 19 \Rightarrow - 4x \leq 28 Dividing both sides by - 4, we get, $x \ge -7$ - $\infty \xleftarrow{} -8 -6 -4 -2 0 2 4 \infty$ From (i) and (ii), the solution is $-7 \le x \le 11$ *i.e.*, $x \in [-7, 11]$ **11.** We have, $F = \frac{9}{5}C + 32$ but 68 < F < 77

$$\therefore \quad 68 < \frac{9}{5}C + 32 < 77$$

Subtracting 32 from each side, we get

$$68 - 32 < \frac{9}{5}C + 32 - 32 < 77 - 32$$

⇒ 36 < $\frac{9}{5}C < 45$

Multiplying each side by 5/9, we get

 $36 \times \frac{5}{9} < C < 45 \times \frac{5}{9}$ $\Rightarrow 20 < C < 25$

- ∴ Required temperature is between 20°C and 25°C.
- **12.** Let the 2% boric acid solution be *x* litres.
- \therefore Mixture is (640 + *x*) litres.
- (i) Now, 2% of x + 8% of 640 > 4% of (640 + x)

or
$$\frac{2x}{100} + \frac{8 \times 640}{100} > \frac{4}{100}(640 + x)$$

$$\Rightarrow 2x + 5120 > 2560 + 4x$$

$$\Rightarrow 5120 - 2560 > 4x - 2x$$

$$\Rightarrow 2x < 2560 \text{ or } x < 1280 \dots (1)$$

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(ii) 2% of x + 8% of 640 < 6% of (640 + x) $\frac{2x}{100} + \frac{8 \times 640}{100} < \frac{6}{100} (640 + x)$ or 2x + 5120 < 3840 + 6x \Rightarrow \rightarrow 5120 - 3840 < 6x - 2x4x > 1280 or x > 320 \Rightarrow ... (2) From (1) and (2), we have 320 < x < 1280Thus, the quantity to be added, should be greater than 320 litres and less than 1280 litres. **13.** Let *x* litres water is added to 45% solution of acid. 25% of $(1125 + x) < \frac{1125 \times 45}{100}$ (i) [:: Amount of acid in resulting mixture = 45% of 1125] $\frac{1125 + x}{4} < \frac{1125 \times 9}{20}$ or $5(1125 + x) < 10125 \implies 5625 + 5x < 10125$ \Rightarrow \Rightarrow 5x < 10125 - 5625 $\Rightarrow x < \frac{4500}{5} \Rightarrow x < 900$... (1) (ii) Further, 30% of $(1125 + x) > \frac{1125 \times 45}{100}$

or
$$\frac{30}{100} \times (1125 + x) > \frac{1125 \times 9}{20}$$

$$\Rightarrow \quad 6(1125 + x) > 1125 \times 9 \Rightarrow 6750 + 6x > 10125$$

$$\Rightarrow 6x > 10125 - 6750 \Rightarrow 6x > 3375$$
$$\Rightarrow x > \frac{3375}{6} \Rightarrow x > 562.5$$

From (1) and (2), we have 562.5 < *x* < 900

Thus, the quantity of water to be added should be greater than 562.5 litres and less than 900 litres.

... (2)

14. We have,
$$IQ = \frac{MA}{CA} \times 100$$

We are given that $80 \le IQ \le 140$ Putting the value of IQ in it, we get

 $80 \leq \frac{MA}{CA} \times 100 \leq 140$ Also we have, CA = 12 years $80 \leq \frac{MA}{12} \times 100 \leq 140$ Multiplying each side by 12, we get $12 \times 80 \leq MA \times 100 \leq 140 \times 12 \text{ or } 960 \leq 100 \times MA \leq 1680$ Dividing each side by 100, we get $9.6 \leq MA \leq 16.8$ Hence, mental age is greater than or equal to 9.6 years and less than or equal to 16.8 years.

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