

Oscillations

 **TRY YOURSELF**

ANSWERS

1. A motion can be periodic and not oscillatory. For example, uniform circular motion is periodic but not oscillatory.

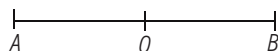
2. A periodic motion repeats after a definite time interval T .
So, $y(t) = y(t + T) = y(t + 2T)$ etc.

3. It is the position of the body where the force acting on it is zero.

4. Distance travelled by oscillator is one time period,
 $x = AO + OB + BO + OA = 4AO$

Amplitude of motion = AO

\therefore Required ratio, $\frac{4AO}{AO} = \frac{4}{1} = 4:1$



5. $\omega = 2\pi n$, where n is frequency and ω is angular frequency.

We know that, $n = \frac{1}{T}$

$$\therefore \omega = \frac{2\pi}{T}$$

6. π or 180° .

7. Velocity : $v(t) = \frac{d}{dt} x(t) = -\omega A \sin(\omega t + \phi)$

8. At the extreme positions.

$$9. \frac{\text{Kinetic energy}}{\text{Total energy}} = \frac{\frac{1}{2} m \omega^2 [A^2 - A^2/4]}{\frac{1}{2} m \omega^2 A^2} = \frac{3}{4}$$

10. No, the total mechanical energy of a harmonic position, is independent of time.

11. (i) Minimum at extreme position (ii) maximum at mean position.

12. The time period of a simple pendulum is

$$T = 2\pi \sqrt{\frac{l}{g}} \quad \text{or} \quad l = \frac{gT^2}{4\pi^2}$$

The time period of a simple pendulum, which ticks seconds, is 2 s.

$$\therefore l = \frac{(9.8 \text{ m s}^{-2})(2 \text{ s})^2}{4\pi^2} = 1 \text{ m}$$

13. The component of weight ($mg \sin\theta$) keeps the pendulum in motion.

14. (i) Gravity (ii) Weight of different column.

$$15. T = 2\pi \sqrt{\frac{l}{g}}$$

If initial length l is 100 cm then after 64% increment, the new length l' is 169 cm.

$$\therefore T = 2\pi \sqrt{\frac{100}{g}} = T' = 2\pi \sqrt{\frac{169}{g}}$$

$$\text{Now, } \frac{T}{T'} = \frac{10}{13}$$

$$\text{change in time period} = \frac{T' - T}{T} \times 100$$

$$= \frac{13 - 10}{10} \times 100 = 30\%$$

16. The time period remains same in both the cases.

17. Time period of oscillation of loaded spring, $T = 2\pi \sqrt{\frac{m}{k}}$, where m is the mass of the load attached and k is the spring constant.

18. The force constant of a spring is the change in the force it exerts divided by the change in deflection of spring.

19. When a spring of force constant k is cut into n equal parts, the force constant of each part would be nk .

Here, $n = 3$, \therefore The force constant of each part would be $3k$.

20. In first case, $T_1 = 1.5 \text{ s}$, $m = m \text{ Kg}$

$$\text{As } T = 2\pi \sqrt{\frac{m}{K}} \Rightarrow 1.5 = 2\pi \sqrt{\frac{m}{K}} \quad \dots(i)$$

In second case

$$T_2 = 1.5 + 1 = 2.5, \text{ mass} = (m + 3) \text{ Kg}$$

$$\text{Then, } 2.5 = 2\pi \sqrt{\frac{m+3}{K}} \quad \dots(ii)$$

Dividing (ii) by (i), we get

$$\frac{2.5}{1.5} = \frac{m+3}{\sqrt{m}} \quad \text{or} \quad \frac{5^2}{3^2} = \frac{m+3}{m} \Rightarrow m = 1.69 \text{ kg.}$$

