

Current Electricity



ANSWERS

Topic 1

1. We can first calculate drift velocity of the electrons from the given data

$$I = Anev_d$$

$$3 = 2 \times 10^{-6} \times 8.5 \times 10^{28} \times 1.6 \times 10^{-19} v_d$$

$$v_d = 0.11 \times 10^{-3} \text{ m s}^{-1}$$

Now time taken by an electron to drift a length of 3 m with drift speed is

$$t = \frac{l}{v_d} = 27.27 \times 10^3 \text{ s.}$$

Topic 2

1. As $R_2 = R_1 [1 + \alpha(t_2 - t_1)]$
 $\therefore 117 = 100 [1 + 1.7 \times 10^{-4}(t - 27)]$
 or $17 = 1.7 \times 10^{-2}(t - 27)$
 or $1000 = t - 27$ or $t = 1027^\circ\text{C}$.

2. We know the relation, $R = \rho \frac{l}{A}$
 $5 = \rho \frac{15}{6 \times 10^{-7}}$
 \therefore Resistivity, $\rho = \frac{30 \times 10^{-7}}{15} = 2 \times 10^{-7} \Omega \text{ m}$

3. $T_1 = 27.5^\circ\text{C}$, $R_1 = 2.1 \Omega$, $T_2 = 100^\circ\text{C}$ and $R_2 = 2.7 \Omega$

Using the relation,

$R_2 = R_1 [1 + \alpha(T_2 - T_1)]$, we have

Temperature coefficient of resistivity of silver,

$$\alpha = \frac{R_2 - R_1}{R_1(T_2 - T_1)} = \frac{2.7 - 2.1}{2.1 \times (100 - 27.5)} = \frac{0.6}{152.25}$$

$$= 3.94 \times 10^{-3} \text{ or } 0.0039^\circ\text{C}^{-1}$$

4. At room temperature 27°C , the resistance of the heating element.

$$R_{27^\circ} = \frac{230}{3.2} = 71.875 \Omega$$

At the steady temperature $t^\circ\text{C}$, the resistance.

$$R_t = \frac{230}{2.8} = 82.143 \Omega$$

Now, $R_2 = R_1 [1 + \alpha(t_2 - t_1)]$

or $82.143 = 71.875 [1 + 1.7 \times 10^{-4}(t - 27)]$

or $0.0840 \times 10^4 = t - 27$

or $840 = t - 27$ or $t = 867^\circ\text{C}$.

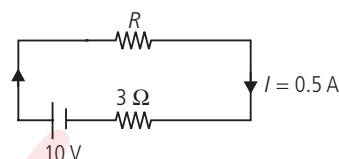
Topic 3

1. $I = \frac{E}{R+r}$
 $0.5 = \frac{10}{R+3}$
 $R+3 = 20$
 $R = 17 \Omega$

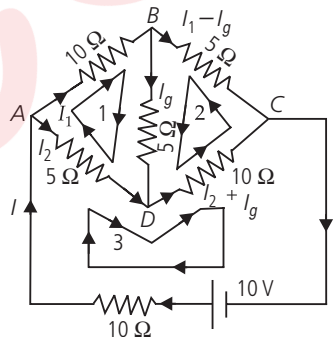
Terminal voltage of the battery

$$V = E - Ir$$

$$V = 10 - 0.5 \times 3 = 8.5 \text{ V}$$



2. Let us first distribute the current in different branches. Now, equations for different loops using Kirchhoff's IInd law,



Loop 1

$$\Sigma E = \Sigma IR$$

$$10I_1 + 5I_g - 5I_2 = 0 \quad \text{or} \quad 2I_1 + I_g - I_2 = 0 \quad \dots(i)$$

Loop 2

$$\Sigma E = \Sigma IR$$

$$5I_g + 10[I_2 + I_g] - 5[I_1 - I_g] = 0$$

$$10I_2 + 20I_g - 5I_1 = 0 \quad \text{or} \quad 2I_2 + 4I_g - I_1 = 0 \quad \dots(ii)$$

Loop 3

$$5I_2 + 10(I_2 + I_g) + 10I = 10$$

$$15I_2 + 10I_g + 10I = 10$$

$$\text{or} \quad 3I_2 + 2I_g + 2I = 2 \quad \dots(iii)$$

Solving equations (i) and (ii)

$$2I_1 + I_g - I_2 = 0$$

$$[-I_1 + 4I_g + 2I_2 = 0] \times 2$$

$$\text{or} \quad 9I_g + 3I_2 = 0 \quad \text{or} \quad I_2 = -3I_g \quad \dots(iv)$$

In the loop ABCDA

$$10I_1 + 5[I_1 - I_g] - 10[I_2 + I_g] - 5I_2 = 0$$

$$15I_1 - 15I_2 - 15I_g = 0 \quad \text{or} \quad I_1 - I_2 - I_g = 0 \quad \dots(v)$$

Solving equations (ii) and (v)

$$2I_2 + 4I_g - I_1 = 0 \quad \text{or} \quad 2(I_1 - I_2 - I_g = 0)$$

$$\text{or} \quad 2I_g + I_1 = 0 \quad \text{or} \quad I_1 = -2I_g$$

Now using the result of (iv) and (vi) in equation (iii)

$$3I_2 + 2I_g + 2I = 2$$

$$-3[3I_g] + 2I_g + 2I = 2 \quad \text{or} \quad 2I - 7I_g = 2$$

Using Kirchhoff's law, $I = I_1 + I_2$

$$I = -5I_g$$

So, equation (vii)

$$2[-5I_g] - 7I_g = 2 \quad \text{or} \quad -17I_g = 2$$

$$\text{So, finally } I_g = -2/17 \text{ A} \quad \text{and} \quad I = \frac{+10}{17} \text{ A}$$

$$\text{Also } I_1 = \frac{4}{17} \text{ A}, \quad I_2 = \frac{6}{17} \text{ A}$$

$$\text{Current in branch } AB = \frac{4}{17} \text{ A}$$

$$\text{Current in branch } AD = \frac{6}{17} \text{ A}$$

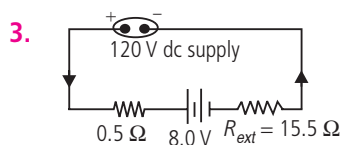
$$\text{Current in branch } BD = \frac{-2}{17} \text{ A}$$

$$\text{Current in branch } BC = \frac{6}{17} \text{ A}$$

...(vi)

$$\text{Current in branch } DC = \frac{4}{17} \text{ A}$$

...(vii)



During charging, the electric current is sent into the 8.0 V battery.

The current in the circuit

$$I = \frac{E_1 - E_2}{R_{\text{ext}} + r} = \frac{120 - 8}{15.5 + 0.5} \quad \text{or} \quad I = \frac{112}{16} = 7 \text{ A}$$

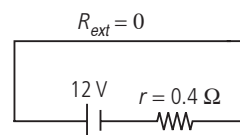
Now, terminal voltage of the battery during charging

$$V = E + Ir = 8 + 7(0.5) = 11.5 \text{ V}$$

A series resistance is joined in the charging circuit to limit the excessive current so that charging is slow and permanent.

4. The maximum current will be obtained when no external resistance is offered by wire joining the two terminals.

$$I = \frac{E}{R_{\text{ext}} + r} \Rightarrow I = \frac{12}{0.4} = 30 \text{ A}$$



$$(\because R_{\text{ext}} = 0)$$

