

EXAM DRILL

Circles

SOLUTIONS

1. (d) : Since, tangent is perpendicular to the radius through the point of contact.

$$\therefore OA \perp AP$$

\therefore By Pythagoras theorem, in right angle $\triangle AOP$

$$OA^2 = OP^2 - AP^2 = 10^2 - 8^2 = 36 \Rightarrow OA = 6 \text{ cm}$$

$$\therefore OB = OA = 6 \text{ cm} \quad [\text{Radii of the same circle}]$$

2. (c) : We know that length of tangents drawn from an external point to the circle are equal.

$$\therefore BR = BP = 5 \text{ cm}, AR = AQ = 3 \text{ cm}$$

$$\text{and } QC = PC = 7 - 3 = 4 \text{ cm}$$

$$\text{So, } BC = BP + PC = 5 + 4 = 9 \text{ cm}$$

3. (c) : Since, tangent is perpendicular to the radius through the point of contact.

$$\therefore \angle OTP = 90^\circ$$

$$\text{In } \triangle OTP, OP^2 = OT^2 + PT^2 \quad [\text{By Pythagoras theorem}]$$

$$\Rightarrow 10^2 = 6^2 + PT^2 \Rightarrow PT^2 = 100 - 36 = 64 \Rightarrow PT = 8 \text{ cm}$$

4. (c) : $CR = CQ = 3 \text{ cm}$, $BQ = BP = 5 \text{ cm}$, $AS = AP = 6 \text{ cm}$ and $DS = DR = 4 \text{ cm}$

$$\therefore \text{Perimeter of quadrilateral } ABCD = [(6 + 5) + (5 + 3) + (3 + 4) + (4 + 6)] \text{ cm} = (11 + 8 + 7 + 10) \text{ cm} = 36 \text{ cm}.$$

5. We have, $\angle AOB + \angle APB = 180^\circ$

$[\because \angle AOB \text{ and } \angle APB \text{ are supplementary}]$

$$\Rightarrow \angle APB = 180^\circ - 107^\circ = 73^\circ$$

6. Since, $AB \parallel PR$ and $QOL \perp AB$ ($\because OQ \perp PR$)

$\therefore OL$ bisects chord AB .

$\therefore \triangle AQB$ is isosceles.

$$\Rightarrow \angle LQA = \angle LQB$$

$$\text{But, } \angle LQB = 90^\circ - 67^\circ = 23^\circ$$

$$\therefore \angle AQB = \angle LQA + \angle LQB = 2(23^\circ) = 46^\circ$$

7. We have, $AB = 7 \text{ cm}$, $BC = 9 \text{ cm}$ and $CA = 6 \text{ cm}$

$$\text{Now, } AR = AP = r \text{ (say)} \quad [\text{Radii of the same circle}]$$

$$BP = BQ = x \text{ (say)}$$

$$CR = CQ = y \text{ (say)}$$

$$\therefore r + x = 7 \quad \dots(i)$$

$$x + y = 9 \quad \dots(ii)$$

$$y + r = 6 \quad \dots(iii)$$

Subtracting (ii) from (i), we get

$$r - y = -2 \quad \dots(iv)$$

Adding (iii) and (iv), we get

$$2r = 4 \Rightarrow r = 2 \text{ cm}$$

8. Since, tangents drawn from an external point are equal.

$$\therefore BQ = BR \quad [\text{Tangents from } B] \quad \dots(i)$$

$$CQ = CP \quad [\text{Tangents from } C] \quad \dots(ii)$$

$$\text{Now, } BC + BQ = CQ = 11 \quad [\text{Using (ii)}]$$

$$\Rightarrow 7 + BQ = 11$$

$$\Rightarrow BQ = 11 - 7 = 4 \text{ cm}$$

$$\therefore BR = 4 \text{ cm}$$

[Using (i)]

9. We have, $\angle OAT = 90^\circ$ [\because Tangent is perpendicular to the radius through the point of contact.]

In right angle $\triangle OAT$,

$$\frac{AT}{OT} = \cos 30^\circ \Rightarrow \frac{AT}{8} = \frac{\sqrt{3}}{2}$$

$$\Rightarrow AT = 4\sqrt{3} \text{ cm}$$

10. Two parallel tangents of a circle can be drawn only at the end points of the diameter.

In figure, $l_1 \parallel l_2$

$$\Rightarrow \text{Distance between } l_1 \text{ and } l_2, AB$$

$$= \text{Diameter of the circle}$$

$$= 2 \times r = 2 \times 9 = 18 \text{ cm}$$

11. Given, $BC = 4.5 \text{ cm}$

$$BC = CP \quad [\because \text{Tangents drawn from an external point are equal.}]$$

$$\Rightarrow CP = 4.5 \text{ cm}$$

$$\text{Now, } AC = CP = 4.5 \text{ cm} \quad [\because \text{Tangents from an external point are equal.}]$$

$$\therefore AB = AC + BC = 4.5 + 4.5 = 9 \text{ cm}$$

12. Since, tangent is perpendicular to the radius through the point of contact.

$$\therefore \angle OPT = 90^\circ$$

$$\therefore \angle OPQ = 90^\circ - 50^\circ = 40^\circ$$

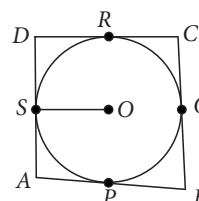
$$\text{Also, } OP = OQ$$

[Radii of same circle]

$$\Rightarrow \angle OQP = \angle OPQ = 40^\circ$$

$$\therefore \angle POQ = 180^\circ - (40^\circ + 40^\circ) = 100^\circ.$$

13. (i) (b) :



Here, OS is the radius of circle.

Since radius at the point of contact is perpendicular to tangent.

$$\text{So, } \angle OSA = 90^\circ$$

(ii) (d) : Since, length of tangents drawn from an external point to a circle are equal.

$$\therefore AS = AP, BP = BQ,$$

$$CQ = CR \text{ and } DR = DS$$

$$\dots(1)$$

(iii) (a) : $AP = AS = AD - DS = AD - DR$ (Using (1))
 $= 11 - 7 = 4$ cm

(iv) (b) : In quadrilateral OQCR,
 $\angle QCR = 60^\circ$ (Given)
 And $\angle OQC = \angle ORC = 90^\circ$
 [Since, radius at the point of contact is perpendicular to tangent.]

$$\therefore \angle QOR = 360^\circ - 90^\circ - 90^\circ - 60^\circ = 120^\circ$$

(v) (c) : From (1), we have $AS = AP$, $DS = DR$,
 $BQ = BP$ and $CQ = CR$

Adding all above equations, we get

$$AS + DS + BQ + CQ = AP + DR + BP + CR$$

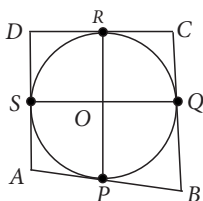
$$\Rightarrow AD + BC = AB + CD$$

14. (i) (a) : Here, $OA^2 = OD^2 + AD^2$

$$\Rightarrow AD = \sqrt{25 - 9} = 4$$
 cm

As OD bisects AB, then

$$AB = 2AD = 2 \times 4 = 8$$
 cm



(ii) (c) : Here, $PB^2 + OB^2 = OP^2 = PA^2 + OA^2$

$$\text{Then } PB^2 + 9 = 144 + 25 \Rightarrow PB^2 = 160$$

$$\Rightarrow PB = 4\sqrt{10}$$
 cm

(iii) (b) : Here, $OP^2 - PB^2 = OB^2$ and $OP^2 - PA^2 = OA^2$

$$\therefore OB = \sqrt{100 - 64} = \sqrt{36} = 6$$
 cm

$$\text{and } OA = \sqrt{100 - 36} = \sqrt{64} = 8$$
 cm

$$\therefore AB = OA - OB = 8 - 6 = 2$$
 cm

(iv) (d) : Here, in right angled $\triangle OBD$, $OB = 5$ cm and
 $OD = 3$ cm.

$$\therefore BD = \sqrt{25 - 9} = \sqrt{16} = 4$$
 cm

Since, chord BP is bisected by radius OD.

$$\therefore BP = 2BD = 8$$
 cm

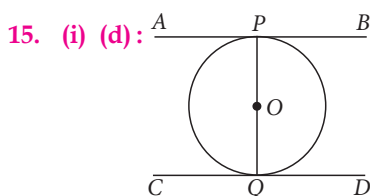
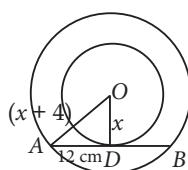
(v) (a) : Let x be the radii of smaller circle.

$$\text{Now, } OA^2 = OD^2 + AD^2$$

$$\Rightarrow (x + 4)^2 = x^2 + 12^2$$

$$\Rightarrow 8x + 16 = 144$$

$$\Rightarrow x = 16$$
 cm



Two tangents of a circle are parallel only when they are drawn at ends of a diameter.

So, PQ is the diameter of the circle.

(ii) (b)

(iii) (d)

(iv) (a) : Here, the two circles have a common point of contact T and PQ is the tangent at T. So, PQ is the tangent to both the circles.

(v) (a)

16. (i) (d) : We have, $AP = AQ$, $BP = BD$, $CQ = CD$... (i)
 [∵ Tangents drawn from an external points are equal in length]

$$\text{Now, } AB + BC + AC = 7 + 5 + 8 = 20$$
 cm

$$\Rightarrow AB + BD + CD + AC = 20$$
 cm

$$\Rightarrow AP + AQ = 20$$
 cm $\Rightarrow 2AP = 20$ cm $\Rightarrow AP = 10$ cm

(ii) (c) : Let $AF = AE = x$ cm

[∵ Tangents drawn from an external point to a circle are equal in length]

$$\text{Given, } BD = FB = 9$$
 cm, $CD = CE = 3$ cm

$$\text{In } \triangle ABC, AB^2 = AC^2 + BC^2$$

$$\Rightarrow (AF + FB)^2 = (AE + EC)^2 + (BD + CD)^2$$

$$\Rightarrow (x + 9)^2 = (x + 3)^2 + 12^2$$

$$\Rightarrow 18x + 81 = 6x + 9 + 144$$

$$\Rightarrow 12x = 72 \Rightarrow x = 6$$
 cm

$$\therefore AB = 6 + 9 = 15$$
 cm

(iii) (b) : Here, $AP = AS = 4$ cm

$$\therefore DS = DR = 10 - 4 = 6$$
 cm

And $BP = BQ = 2$ cm. So, $CR = CQ = 5 - 2 = 3$ cm

$$\text{So, } CD = DR + CR = 6 + 3 = 9$$
 cm

(iv) (d) : Here $\angle OAP = 90^\circ$

In $\triangle AOP$ and $\triangle BOP$

$$\angle OAP = \angle OBP \text{ [} 90^\circ \text{ each]}$$

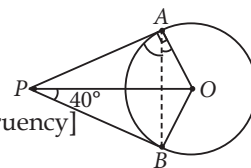
$$OA = OB \text{ [Radii of circle]}$$

$PA = PB$ [Tangents drawn from an external point are equal]

$$\therefore \triangle AOP \cong \triangle BOP \text{ [By SAS congruency]}$$

$$\therefore \angle APO = \angle OPB \text{ [C.P.C.T]} = 40^\circ$$

$$\therefore \angle BPA = 40^\circ + 40^\circ = 80^\circ$$



(v) (c) : For bigger circle, $PA = PB$... (i)

[∵ Tangents drawn from an external point are equal in length]

Similarly, for smaller circle, $PB = PC$... (ii)

From (i) and (ii), we get

$$PA = PB = PC = 7$$
 cm

17. ∵ PQ is a diameter

[Given]

$$\therefore \angle QOR + \angle ROP = 180^\circ$$

[Linear pair]

$$\Rightarrow \angle QOR = 180^\circ - 70^\circ = 110^\circ$$

Also, $OQ = OR$

[Radii of same circle]

$$\Rightarrow \angle RQO = \angle ORQ$$

[∵ Angles opposite to equal sides of triangle are equal.]

$$= \frac{180^\circ - 110^\circ}{2} = \frac{70^\circ}{2} = 35^\circ$$

... (i)

Also, $QP \perp PT$ [∵ Tangent is perpendicular to the radius through the point of contact]

$$\Rightarrow \angle QPT = 90^\circ$$

... (ii)

In ΔQPT , $\angle RQO + \angle QPT + x = 180^\circ$

$$\therefore x = 180^\circ - 90^\circ - 35^\circ = 55^\circ \quad [\text{Using (i) and (ii)}]$$

18. $PA = AM$ [Given]

$$\therefore \angle APM = \angle PMA \quad \dots(i)$$

Also, $\angle PMA = \angle MBA$ $\dots(ii)$

[By alternate segment theorem]

$$\Rightarrow \angle MPB = \angle MBP$$

[Using (i) and (ii)]

$$\Rightarrow MB = PM$$

$\dots(iii)$

$\therefore \Delta PMB$ is isosceles.

Now, we know that $PM^2 = PA \times PB$,

$$\therefore MB^2 = PA \times PB,$$

[From (iii)]

which means both statements 'A' and 'B' are true.

19. Since, tangents drawn from an external point are equal.

$$\therefore PA = PB = 24 \text{ cm.}$$

Also, $\angle OBP = 90^\circ$

[Since, tangent is perpendicular to the radius through the point of contact.]

In ΔPOB , we have

$$OP^2 = OB^2 + BP^2$$

[By Pythagoras theorem]

$$\Rightarrow 25^2 = OB^2 + 24^2$$

$$\Rightarrow OB^2 = 625 - 576 = 49 \Rightarrow OB = 7 \text{ cm}$$

20. Since tangent is perpendicular to the radius through the point of contact.

$$\therefore \angle OAP = 90^\circ$$

Now, in ΔOAP ,

$$\sin(\angle OPA) = \frac{OA}{OP} = \frac{r}{2r} = \frac{1}{2}$$

$$\Rightarrow \angle OPA = 30^\circ$$

$$\therefore \angle APB = 2(\angle OPA) = 2 \times 30^\circ = 60^\circ \quad \dots(i)$$

Also, $AP = PB$ $[\because \text{Tangents drawn from an external point are equal.}]$

$$\therefore \angle PAB = \angle PBA \quad \dots(ii)$$

In ΔPAB , $\angle PAB + \angle PBA + \angle APB = 180^\circ$

$$\Rightarrow 2\angle PAB = 180^\circ - 60^\circ = 120^\circ \quad [\text{Using (i) and (ii)}]$$

$$\Rightarrow \angle PAB = 60^\circ$$

Hence, $\angle PAB = \angle PBA = \angle APB = 60^\circ$

$$\therefore \Delta APB \text{ is an equilateral triangle.}$$

21. Since angle made by an arc at the centre of a circle is twice the angle subtended by the same arc at any point on the remaining part of the circle.

$$\therefore \angle AOQ = 2\angle ABQ$$

$$\Rightarrow \angle ABQ = \frac{1}{2} \times 78^\circ = 39^\circ$$

In ΔABT , $\angle BAT + \angle ABT + \angle ATB = 180^\circ$

$$\Rightarrow 90^\circ + 39^\circ + \angle ATB = 180^\circ$$

$$\Rightarrow \angle ATB = 51^\circ$$

$$\therefore \angle ATQ = 51^\circ$$

22. We have, $\angle APB = 50^\circ$

Now, $PA = PB$ $[\because \text{Tangents drawn from an external point are equal}]$

$$\Rightarrow \angle PAB = \angle PBA$$

In ΔPAB , $\angle PAB + \angle PBA + \angle APB = 180^\circ$

$$\Rightarrow 2\angle PAB = 180^\circ - 50^\circ \Rightarrow \angle PAB = \frac{130^\circ}{2} = 65^\circ$$

Now, $\angle OAB = 90^\circ - \angle PAB$ $[\because OA \perp AP \Rightarrow \angle OAP = 90^\circ]$
 $= 90^\circ - 65^\circ = 25^\circ$

23. From the figure, it is clear that O and Q are centres of smaller and bigger circle respectively.

$$\text{Now, } OT = OQ = \frac{1}{2}(PQ) = \frac{14}{2} = 7 \text{ cm}$$

$$\therefore OR = 7 + 14 = 21 \text{ cm}$$

$\angle OTR = 90^\circ$ $[\because \text{Tangent is perpendicular to the radius through the point of contact.}]$

In right ΔOTR ,

$$OT^2 + RT^2 = OR^2$$

[By Pythagoras theorem]

$$\Rightarrow (7)^2 + RT^2 = (21)^2 \Rightarrow RT^2 = 441 - 49 = 392$$

$$\Rightarrow RT^2 = 14 \times 14 \times 2 \Rightarrow RT = 14\sqrt{2} \text{ cm}$$

24. We have, $OA = OB$

[Radii of the same circle]

$$\Rightarrow \angle 3 = \angle 1 = 35^\circ$$

$[\because \text{Angles opposite to equal sides of a triangle are equal}]$

$$\text{But, } \angle 1 + \angle 2 + \angle 3 = 180^\circ$$

[By angle sum property]

$$\Rightarrow 35^\circ + 35^\circ + \angle 2 = 180^\circ$$

$$\Rightarrow \angle 2 = 180^\circ - 70^\circ = 110^\circ$$

$$\text{Also, } \angle 4 = \frac{1}{2}\angle 2$$

[Since angle made by an arc at the centre of a circle is twice the angle subtended by the same arc at any point on the remaining part of the circle.]

$$= \frac{1}{2} \times 110^\circ = 55^\circ$$

$$\Rightarrow \angle ACB = 55^\circ$$

$$\therefore \text{By alternate segment theorem, } \angle BAQ = \angle ACB = 55^\circ$$

25. We have, $OP \perp OQ$

Also, $OP \perp PT$ and $OQ \perp QT$

$[\because \text{Tangent is perpendicular to the radius through the point of contact}]$

$$\therefore \text{In quadrilateral } OPTQ, \angle P = \angle Q = \angle O = 90^\circ \quad \dots(i)$$

$$\text{Now, } \angle P + \angle Q + \angle O + \angle T = 360^\circ$$

$$\Rightarrow \angle T = 360^\circ - (90^\circ + 90^\circ + 90^\circ)$$

$$= 360^\circ - 270^\circ = 90^\circ$$

$\dots(ii)$

$$OP = OQ$$

[Radii of same circle] $\dots(iii)$

We have, $OPTQ$ is a square

Hence, PQ and OT are right bisectors of each other.

26. Given, a hexagon $ABCDEF$ circumscribes a circle.

Since, tangents from an external point are equal.

$$\therefore AQ = AP, QB = BR, CS = CR,$$

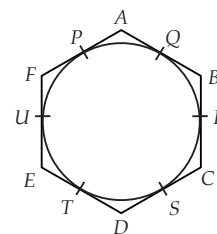
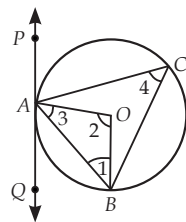
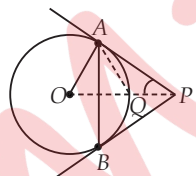
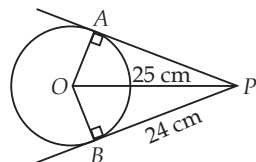
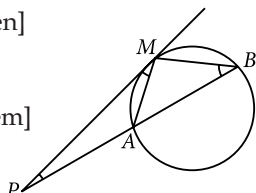
$$DS = DT, EU = ET, UF = FP$$

$$\text{Now, } AB + CD + EF = (AQ + QB) + (CS + SD) + (EU + UF)$$

$$= (AP + BR) + (CR + DT) + (ET + FP)$$

$$= (AP + FP) + (BR + CR) + (DT + ET)$$

$$= AF + BC + DE$$



OR

Join OC

Now, $OC \perp CD$ [\because Tangent is perpendicular to the radius through the point of contact]

$$\Rightarrow \angle 2 + \angle 3 = 90^\circ$$

$$\text{Also, } OC = OA \Rightarrow \angle 1 = 30^\circ$$

$$\text{Now, } \angle 1 + \angle 2 = 90^\circ$$

[Angle in a semicircle]

$$\therefore \angle 2 = 90^\circ - 30^\circ = 60^\circ$$

$$\Rightarrow \angle 3 = 30^\circ$$

$$\text{In } \triangle ACD, \angle ACD + \angle CAD + \angle 4 = 180^\circ$$

$$\Rightarrow (30^\circ + 60^\circ + 30^\circ) + 30^\circ + \angle 4 = 180^\circ \Rightarrow \angle 4 = 30^\circ$$

$$\text{In } \triangle BCD, \angle 3 = \angle 4 \therefore BC = BD.$$

27. $OP \perp AB$ [\because Tangent is perpendicular to the radius through the point of contact]
 $\therefore AP = BP$ [$\because AB$ is chord to larger circle and $OP \perp AB$]

$$\therefore AP = \frac{8}{2} = 4 \text{ cm } [\because AB = 8 \text{ cm}]$$

$$OP = \frac{6}{2} = 3 \text{ cm } [\because \text{Diameter of smaller circle} = 6 \text{ cm}]$$

$$\text{In right } \triangle OAP, OA^2 = OP^2 + AP^2 \\ = 3^2 + 4^2 = 9 + 16 = 25 \Rightarrow OA = 5 \text{ cm}$$

Thus, diameter of the larger circle is 10 cm.

28. Given, a circle with center O . AB is the diameter of this circle. HK is tangent to the circle at P . AH and BK are perpendicular to HK from A and B at H and K respectively.

Since, AH and HP are tangents from the external point H .

$$\therefore AH = HP$$

... (i)

Also, KB and KP are tangents from the external point K .

$$\therefore BK = KP$$

... (ii)

Adding (i) and (ii), we get

$$AH + BK = HP + KP = HK$$

... (iii)

$$AB \perp AH \text{ and } AB \perp BK$$

[\because Tangent is perpendicular to the radius through the point of contact]

$$\therefore \angle 1 = \angle 2 = 90^\circ$$

$$\text{Also, } AH \perp HK$$

$$\Rightarrow \angle 3 = 90^\circ$$

$$\text{and } BK \perp HK \Rightarrow \angle 4 = 90^\circ$$

$$\text{Thus, } \angle 1 = \angle 2 = \angle 3 = \angle 4 = 90^\circ$$

$$\therefore AHKB \text{ is a rectangle.}$$

$$\Rightarrow AB = HK$$

... (iv)

[\because Opposite sides of a rectangle are equal]

From (iii) and (iv), $AH + BK = AB$

29. Since, length of tangents drawn from an external point to a circle are equal.

$$\therefore QS = QT = 14 \text{ cm,}$$

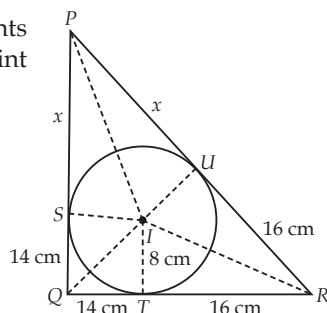
$$RU = RT = 16 \text{ cm.}$$

$$\text{Let, } PS = PU = x \text{ cm}$$

$$\text{Thus, } PQ = (x + 14) \text{ cm}$$

$$PR = (x + 16) \text{ cm}$$

$$\text{and } QR = 30 \text{ cm}$$



Now, Area of $\triangle PQR$

$$= \text{Area of } \triangle IQR + \text{Area of } \triangle IQP + \text{Area of } \triangle IPR$$

$$\Rightarrow 336 = \frac{1}{2} (14 + 16) \times 8 + \frac{1}{2} (14 + x) \times 8 + \frac{1}{2} (16 + x) \times 8$$

$$\Rightarrow 84 = 30 + 14 + x + 16 + x \Rightarrow 24 = 2x \Rightarrow x = 12$$

Hence, $PQ = 26 \text{ cm}$ and $PR = 28 \text{ cm}$

30. We have, $AB = 16 \text{ cm}$. Therefore, $AL = BL = 8 \text{ cm}$

In $\triangle OLB$, we have

$$OB^2 = OL^2 + LB^2 \Rightarrow 10^2 = OL^2 + 8^2$$

$$\Rightarrow OL^2 = 100 - 64 = 36 \Rightarrow OL = 6 \text{ cm}$$

Let $PL = x$ and $PB = y$. Then, $OP = (x + 6) \text{ cm}$

In \triangle 's PLB and OBP , we have

$$PB^2 = PL^2 + BL^2 \text{ and } OP^2 = OB^2 + PB^2$$

$$\Rightarrow y^2 = x^2 + 64 \text{ and } (x + 6)^2 = 100 + y^2$$

$$\Rightarrow (x + 6)^2 = 100 + x^2 + 64$$

[Substituting the value of y^2 in second equation]

$$\Rightarrow 12x = 128 \Rightarrow x = \frac{32}{3} \text{ cm}$$

$$\therefore y^2 = x^2 + 64 \Rightarrow y^2 = \left(\frac{32}{3}\right)^2 + 64 = \frac{1600}{9} \Rightarrow y = \frac{40}{3} \text{ cm}$$

$$\text{Hence, } PA = PB = \frac{40}{3} \text{ cm}$$

OR

$$DR = DS = 5 \text{ cm}$$

[\because Tangents drawn from an external point are equal]

$$AR = AD - DR = 23 - 5 = 18 \text{ cm}$$

$$AQ = AR = 18 \text{ cm}$$

[\because Tangents drawn from an external point are equal]

$$QB = AB - AQ = 29 - 18 = 11 \text{ cm}$$

$$QB = BP = 11 \text{ cm}$$

$$\text{Also, } \angle OQB = \angle OPB = 90^\circ$$

[\because Tangent at any point of circle is perpendicular to the radius through the point of contact]

$$\text{Also, } \angle B = 90^\circ$$

$$\text{So, } OQ = OP = \text{radius} = r$$

$$\therefore OQBP \text{ is a square.}$$

$$\Rightarrow r = OP = OQ = QB = 11 \text{ cm}$$

[Sides of a square]

Hence, radius (r) of the circle = 11 cm

31. In $\triangle APO$,

$\angle P = 90^\circ$ [\because Tangent and radius are perpendicular to each other]

$$OP = 5 \text{ cm, } AO = 13 \text{ cm}$$

In $\triangle APO$, by Pythagoras theorem

$$OA^2 = OP^2 + AP^2$$

$$\Rightarrow 13^2 = 5^2 + AP^2$$

$$\Rightarrow 169 - 25 = AP^2 \Rightarrow 12 = AP$$

Since, tangents from an external point to a circle are equal.

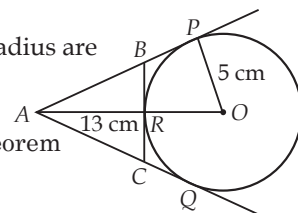
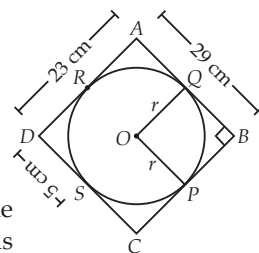
$$\therefore AP = AQ, BP = BR, CQ = CR$$

... (i)

$$\text{Perimeter of } \triangle ABC = AB + BC + AC$$

$$= AB + (BR + RC) + AC = AB + BP + CQ + AC \text{ [Using (i)]}$$

$$= AP + AQ = AP + AP = 2AP = 2 \times 12 = 24 \text{ cm}$$



32. Here, two circles are of radii $OP = 3$ cm and $O'P = 4$ cm.

These two circles intersect at P and Q .

Here, OP and $O'P$ are two tangents drawn at point P .

$\angle OPO' = 90^\circ$

[\because Tangent at any point of circle is perpendicular to radius through the point of contact]

Join OO' and PQ such that OO' and PQ intersect at point N .

In right angled $\triangle OPO'$,

$$(OO')^2 = (OP)^2 + (PO')^2$$

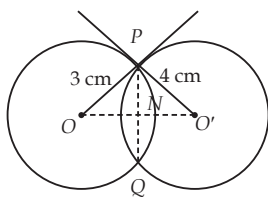
$$\Rightarrow (OO')^2 = (3)^2 + (4)^2 = 25$$

$$\Rightarrow OO' = 5 \text{ cm}$$

Also, $PN \perp OO'$

Let $ON = x$, then $NO' = 5 - x$

In right angled $\triangle ONP$,



$$(OP)^2 = (ON)^2 + (NP)^2$$

$$\Rightarrow (NP)^2 = 3^2 - x^2 = 9 - x^2$$

and in right angled $\triangle PNO'$,

$$(PO')^2 = (PN)^2 + (NO')^2$$

$$\Rightarrow (4)^2 = (PN)^2 + (5 - x)^2$$

$$\Rightarrow (PN)^2 = 16 - (5 - x)^2$$

From (i) and (ii), we have

$$9 - x^2 = 16 - (5 - x)^2$$

$$\Rightarrow 7 + x^2 - (5 - x)^2 = 0$$

$$\Rightarrow 7 + x^2 - (25 + x^2 - 10x) = 0$$

$$\Rightarrow 10x = 18 \Rightarrow x = 1.8 \text{ cm}$$

Again, in right angled $\triangle OPN$,

$$OP^2 = (ON)^2 + (NP)^2$$

$$\Rightarrow 3^2 = (1.8)^2 + (NP)^2$$

$$\Rightarrow (NP)^2 = 9 - 3.24 = 5.76$$

$$\Rightarrow NP = 2.4 \text{ cm}$$

\therefore Length of common chord,

$$PQ = 2PN = 2 \times 2.4 = 4.8 \text{ cm}$$

[By Pythagoras theorem]

...(i)

[By Pythagoras theorem]

...(ii)

[By Pythagoras theorem]

